



## Nonlinear Predictive Direct Power Control Based on Space Vector Modulation of 3-Phase 3-Level Solar PV Integrated Unified Power Quality Conditioner

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### ABSTRACT

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#### Keywords:

*harmonic extraction, photovoltaic generator (PVG), unified power quality conditioner (UPQC), feedback linearisation controller, space vector modulation (SVM), predictive direct power control (PDPC)*

This paper presents a hybrid feedback linearisation-based predictive direct power control strategies of the unified power quality conditioner (UPQC) combined with a photovoltaic generator (PVG) using space vector modulation technique for power quality enhancement. The PVG-UPQC is acting as a universal conditioner for power quality enhancement and renewable energy integration simultaneously, and it mitigates harmonics in both voltage and current caused by nonlinear loads in addition to reactive power compensation. The PVG-UPQC is made up of a dc bus powered by the photovoltaic generator that connects shunt and series active power filters. The shunt filter functions as a current source and compensates for current harmonics. The series filter compensates for voltage harmonics and fluctuations such voltage sag/swell by acting as a voltage source. In order to enhance the performances of PVG-UPQC, a hybrid control method based on FL-PDPC combined with a three-level SVM controller is proposed. The aims are to deliver compensation signals faster and more accurately under a variety of load conditions, as well as eliminate voltage and current harmonics while maintaining good dynamic response. The performance of the suggested control scheme is validated by extensive simulation results obtained by Matlab/Simulink for a sensitive nonlinear load. These results are compared with those obtained with a linear PI controller proves the superiority and effectiveness of FL-PDPC controller.

## 1. INTRODUCTION

Because of the increased usage of power electronic equipment in recent years, power quality has deteriorated owing to harmonic generations [1]. At IEEE-519 and IEC-555, the standards and terminology have been thoroughly specified for power quality. The overall harmonic distortion permitted should be less than 5% according to these rules [2].

With the use of passive filters, the aforementioned issues can be partially overcoming [3-6]. However, this type of filter would not resolve random fluctuations in the load current and voltage waveforms. On the contrary, compensating devices, such as Static Var-Compensator (SVC), Parallel Active-Filter (PAF), Series Active-Filter (SAF) and hybrid filters are suggested to ensure power quality [7]. However, because they can only tackle one or two power quality issues, their capabilities are typically restricted. Recent studies have demonstrated that unified power quality conditioners, which include series and shunt active filters, may tackle the majority of power quality issues at the same time [8].

The UPQC can keep the load end-voltage constant and prevent voltage sags/swells from entering the system [9]. In addition, the UPQC could also effectively supply the load's reactive power requirements and suppress produced load harmonic currents, preventing them from propagating back to the utility, causing voltage and current distortion to other customers [10].

Different control approaches for the UPQC have been proposed. Koroglu et al. [10] have applied a linear control using PI controller. The control of the UPQC connected to a wind system by PI controller is suggested in Refs. [11, 12], the controller used in these papers is a conventional PI regulator, based on the kind of regulator the results demonstrated are not sufficient and the duration of the simulation can't prove its robustness. An intelligent controller has been applied in Refs. [13, 14]. A four-wire topology of the UPQC controlled by PI has been studied by Prathyusha and Venkatesh [15], and da Silva et al. [16]. In Ref. [17] a power quality enhancement in solar power with grid connected system using UPQC has been established. Otherwise, the system does not prove the performances of the controller under nonlinear variations in addition to the high value of the THD that reached 4.66%.

This paper has two objectives. Firstly, to develop a feedback linearisation-SVM controller for the PVG-UPQC to improve power quality. Secondly, to compare the suggested controller's performance with a PI controller to ensure the suggested controller through a varied simulation results for a nonlinear load.

The remaining part of the article is organised in the following manner: in section II, the design of different parts of the PVG-UPQC is detailed, while simulation results under different scenarios and their analysis are given in section III and the final section represents the conclusion of the present work.

## 2. CONTROL DESIGN

Figure 1 depicts the basic operation of the suggested control approach for the PVG-UPQC associated with a nonlinear load. A three-level Space Vector Modulator generates the switch control signals. The proposed controllers provide voltage references for the SVM. The instantaneous PQ theory for

currents and PQ-PLL for voltages are used to establish the harmonic references [17-19]. Compensation goals include voltage and current harmonics mitigation, reactive power compensation and DC bus regulation during the bidirectional active power exchange between the PV generator, two active filters and power system grid. A detailed description of the different parts of UPQC is given hereafter.

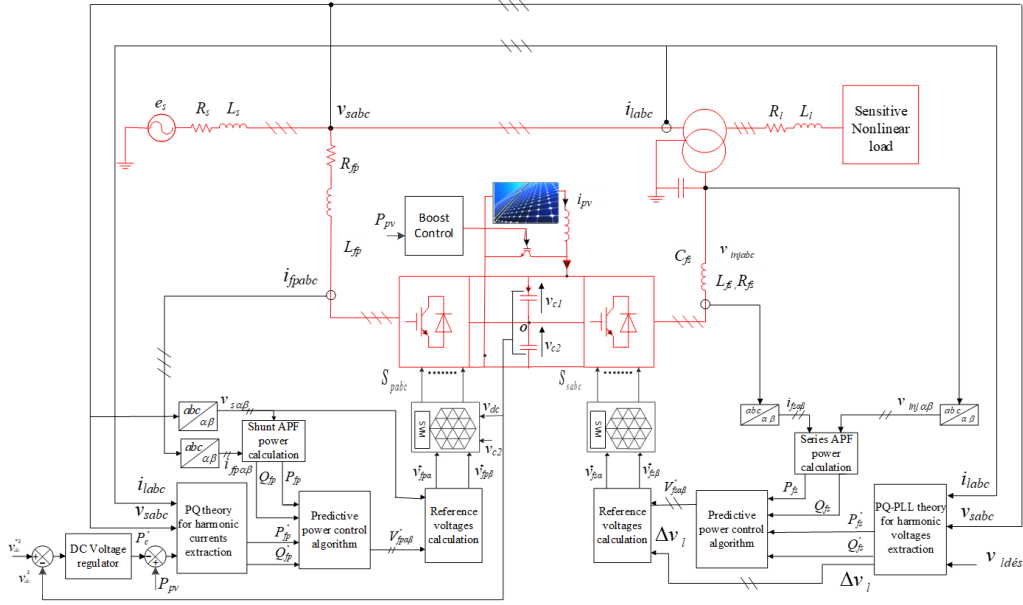


Figure 1. Feedback linearization - PDPC control scheme of the PVG-UPQC

### 2.1 Mathematical model of GPV-UPQC

The PVG-UPQC's dynamic model is described by a differential equation defined in  $\alpha$ - $\beta$  stationary frame. The latter is presented in Eqns. (1) and (3);

The parallel filter model is governed by the following equation.

$$\begin{aligned} \frac{di_{fp\alpha}}{dt} &= -\frac{R_{fp}}{L_{fp}} i_{fp\alpha} - \frac{v_{s\alpha}}{L_{fp}} + \frac{v_{fp\alpha}}{L_{fp}} \\ \frac{di_{fp\beta}}{dt} &= -\frac{R_{fp}}{L_{fp}} i_{fp\beta} - \frac{v_{s\beta}}{L_{fp}} + \frac{v_{fp\beta}}{L_{fp}} \end{aligned} \quad (1)$$

The powers at the output of the parallel filter are given as follows:

$$\begin{bmatrix} P_{fp} \\ Q_{fp} \end{bmatrix} = \begin{bmatrix} v_{fp\alpha} & v_{fp\beta} \\ v_{fp\beta} & -v_{fp\alpha} \end{bmatrix} \begin{bmatrix} i_{fp\alpha} \\ i_{fp\beta} \end{bmatrix} \quad (2)$$

From (1) and (2) and by applying the Lie derivative method, the derivative of powers is given as:

$$\begin{aligned} \frac{dP_{fp}}{dt} &= \frac{1}{L_{fp}} (-R_{fp} P_{fp} + V_{fp\alpha}) \\ \frac{dQ_{fp}}{dt} &= \frac{1}{L_{fp}} (-R_{fp} Q_{fp} + V_{fp\beta}) \end{aligned} \quad (3)$$

where,

$$\begin{aligned} V_{fp\alpha} &= v_{s\alpha} v_{fp\alpha} + v_{s\beta} v_{fp\beta} - (v_{s\alpha}^2 + v_{s\beta}^2) \\ V_{fp\beta} &= -v_{s\beta} v_{fp\alpha} + v_{s\alpha} v_{fp\beta} \end{aligned} \quad (4)$$

It can be also written in the form (5).

$$\dot{x}_p = f_p(x_p) + g_p(x_p)u_p \quad (5)$$

where:

$$\begin{aligned} f_p(x_p) &= \begin{bmatrix} -\frac{R_{fp}}{L_{fp}} x_{p1} \\ -\frac{R_{fp}}{L_{fp}} x_{p2} \end{bmatrix}, \quad g_p(x_p) = \begin{bmatrix} \frac{1}{L_{fp}} & 0 \\ 0 & \frac{1}{L_{fp}} \end{bmatrix}, \\ x_p &= \begin{bmatrix} P_{fp} \\ Q_{fp} \end{bmatrix}, \quad u_p = \begin{bmatrix} V_{fp\alpha} \\ V_{fp\beta} \end{bmatrix}, \quad y_p = \begin{bmatrix} y_{p1} \\ y_{p2} \end{bmatrix} = \begin{bmatrix} h_{p1} \\ h_{p2} \end{bmatrix} \end{aligned}$$

$V_{fp\alpha}$ ,  $P_{fp}$  and  $Q_{fp}$  are the voltages and active and reactive powers of the shunt filter respectively.

The DC-Bus is modeled as follows:

$$\frac{dv_{dc}^2}{dt} = \frac{2P_c}{C_{dc}} \quad (6)$$

It can be also expressed in the form of (7).

$$\dot{x}_{dc} = f_{dc}(x_{dc}) + g_{dc}(x_{dc})u_{dc} \quad (7)$$

where:  $f_{dc}(x_{dc}) = 0$ ,  $g_{dc}(x_{dc}) = \frac{2}{C_{dc}}$  and  $u_{dc}(x_{dc}) = P_c$ .

The series filter model is described by:

$$\begin{aligned} \frac{di_{fs\alpha}}{dt} &= -\frac{R_{fs}}{L_{fs}} i_{fs\alpha} - \frac{v_{inj\alpha}}{L_{fs}} + \frac{v_{fs\alpha}}{L_{fs}} \\ \frac{di_{fs\beta}}{dt} &= -\frac{R_{fs}}{L_{fs}} i_{fs\beta} - \frac{v_{inj\beta}}{L_{fs}} + \frac{v_{fs\beta}}{L_{fs}} \end{aligned} \quad (8)$$

As the previous system, the derivative of powers is given as:

$$\begin{aligned} \frac{dP_{fs}}{dt} &= \frac{1}{L_{fs}} (-R_{fs} P_{fs} + V_{fs\alpha}) \\ \frac{dQ_{fs}}{dt} &= \frac{1}{L_{fs}} (-R_{fs} Q_{fs} + V_{fs\beta}) \end{aligned} \quad (9)$$

where,

$$\begin{aligned} V_{fs\alpha} &= v_{inj\alpha} v_{fs\alpha} + v_{inj\beta} v_{fs\beta} - (v_{inj\alpha}^2 + v_{inj\beta}^2) \\ V_{fs\beta} &= -v_{inj\beta} v_{fs\alpha} + v_{inj\alpha} v_{fs\beta} \end{aligned} \quad (10)$$

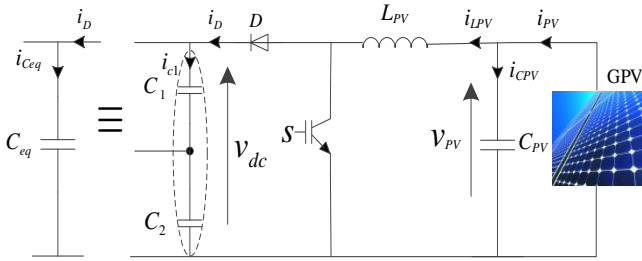
The series filter model is described by:

$$\dot{x}_s = f_s(x_s) + g_s(x_s)u_s \quad (11)$$

where:  $f_s(x_s) = \begin{bmatrix} \frac{1}{C_{fs}} x_{s1} \\ \frac{1}{C_{fs}} x_{s2} \end{bmatrix}$ ,  $g_s(x_s) = \begin{bmatrix} \frac{1}{L_{fs}} & 0 \\ 0 & \frac{1}{L_{fs}} \end{bmatrix}$ ,  $x_s = \begin{bmatrix} P_{fs} \\ Q_{fs} \end{bmatrix}$ ,  $u_s = \begin{bmatrix} V_{fs\alpha} \\ V_{fs\beta} \end{bmatrix}$ ,  $y_s = \begin{bmatrix} y_{s1} \\ y_{s2} \end{bmatrix} = \begin{bmatrix} h_{s1} \\ h_{s2} \end{bmatrix}$ .

$V_{fs\alpha}$ ,  $P_{fs}$  and  $Q_{fs}$  are the voltages and active and reactive powers of the series filter respectively.

The output of the photovoltaic generator (PVG) is connected to a boost converter, as represented in Figure 2.



**Figure 2.** Boost converter of the PV Generator.

The state space model for this converter is represented by the dynamic equations below:

$$\begin{aligned} \frac{dv_{pv}}{dt} &= \frac{1}{C_{pv}} i_{pv} - \frac{1}{C_{pv}} i_{Lpv} \\ \frac{di_{Lpv}}{dt} &= \frac{1}{L_{pv}} v_{pv} - \frac{1}{L_{pv}} v_{dc} \end{aligned} \quad (12)$$

with D is defined as duty cycle, the boost's average model becomes as follows:

$$\frac{di_{Lpv}}{dt} = \frac{1}{L_{pv}} v_{pv} - \frac{1}{L_{pv}} (1-D)v_{dc} \quad (13)$$

$$\frac{dv_{pv}}{dt} = \frac{1}{C_{pv}} i_{pv} - \frac{1}{C_{pv}} (1-D)i_{Lpv}$$

The equations can be put in the following form:

$$\dot{x}_b = f_b(x_b) + g_b(x_b)u_b \quad (14)$$

where:

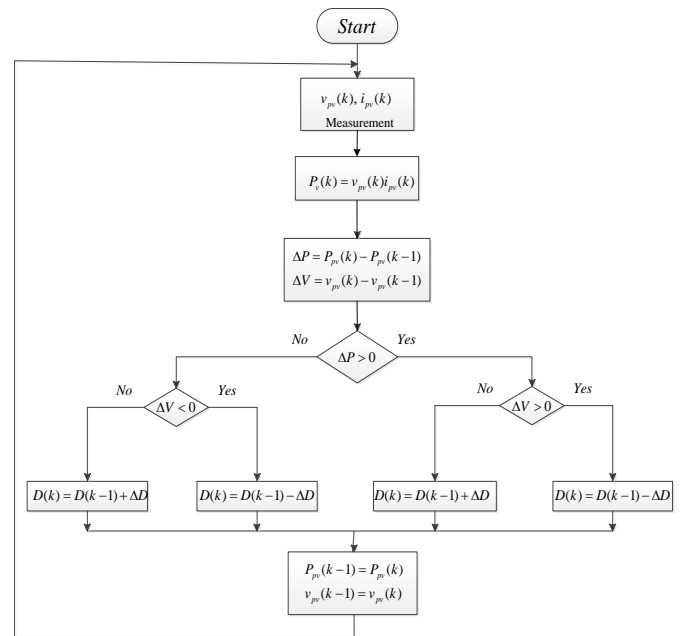
$$f_b(x_b) = \begin{bmatrix} \frac{1}{L_{pv}} v_{pv} \\ \frac{1}{C_{pv}} i_{pv} \end{bmatrix}, g_b(x_b) = \begin{bmatrix} -\frac{1}{L_{pv}} & 0 \\ 0 & -\frac{1}{C_{pv}} \end{bmatrix}, x_b = \begin{bmatrix} i_{Lpv} \\ v_{pv} \end{bmatrix}, u_b = \begin{bmatrix} v_{dc} \\ i_{Lpv} \end{bmatrix}, y_b = \begin{bmatrix} y_{b1} \\ y_{b2} \end{bmatrix} = \begin{bmatrix} h_{b1} \\ h_{b2} \end{bmatrix}$$

## 2.2 MPPT detection algorithm

The DC-DC boost converter is commonly utilised in solar PV units, amplifying and regulating the PV panel voltage at a given level while extracting maximum power. The boost converter is controlled by a Maximum Power Point Tracking (MPPT) controller [5].

In this study, the P&O detection algorithm is employed because of its simplicity of use and low-cost implementation [7]. The flowchart of P&O detection algorithm is presented in Figure 6.

The Perturb & Observe algorithm consists of changing the operating point of the PV generator by raising or reducing the duty cycle of the boost converter for the aim of measuring the output power before and after the perturbation. The algorithm perturbs the structure in the same direction as the power increases; otherwise, it perturbs the structure in the reverse direction. As shown in Figure 3.



**Figure 3.** P&O detection algorithm

There are four possible options that are presented during the tracking of the MPPT:

- if  $\Delta P > 0$  and  $\Delta V > 0$ ,  $V(k)$  is on the left of the MPP and  $V(k+1)$  will be located on a point with a higher voltage value in order to reach the MPP.

- if  $\Delta P > 0$  and  $\Delta V < 0$ ,  $V(k)$  is on the right of the MPP and  $V(k+1)$  will be located on a point with a lower voltage value in order to reach the MPP.

- if  $\Delta P < 0$  and  $\Delta V > 0$ ,  $V(k)$  is on the right of the MPP and  $V(k+1)$  will be located on a point with a lower voltage value in order to reach the MPP.

- if  $\Delta P < 0$  and  $\Delta V < 0$ ,  $V(k)$  is on the left of the MPP and  $V(k+1)$  will be located on a point with a higher voltage value in order to reach the MPP.

## 2.3 Harmonic identification

The identification strategy used to remove harmonics from perturbed waveforms has a big impact on the performance of the active filter [10, 19]. The methods employed for extracting harmonics are detailed in the following parts.

### 2.3.1 Harmonic currents identification using PQ-theory

The instantaneous power theory technique (PQ theory) is used in this study as illustrated in Figure 4.

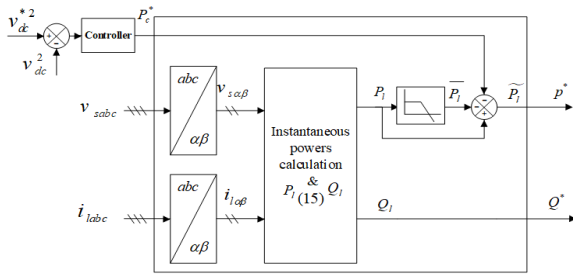
The load's instantaneous powers are computed as follows:

$$\begin{bmatrix} P_l \\ Q_l \end{bmatrix} = \begin{bmatrix} v_{s\alpha} & v_{s\beta} \\ v_{s\beta} & -v_{s\alpha} \end{bmatrix} \begin{bmatrix} i_{l\alpha} \\ i_{l\beta} \end{bmatrix} \quad (15)$$

The powers could be written in the following way:

$$\begin{cases} P_l = \bar{P}_l + \tilde{P}_l \\ Q_l = \bar{Q}_l + \tilde{Q}_l \end{cases} \quad (16)$$

For compensating reactive power and mitigating harmonics, the total reactive power ( $\bar{Q}_l$  and  $\tilde{Q}_l$  components) with the oscillatory component of active power ( $\tilde{P}_l$ ) are chosen as compensatory power references.



**Figure 4.** Harmonic currents extraction scheme using PQ theory

### 2.3.2 Harmonic voltages identification using PQ-PLL theory

It consists of two parts in which the first is to extract voltage harmonics, and it is similar to PQ theory for currents (17):

$$\begin{bmatrix} P_l \\ Q_l \end{bmatrix} = \begin{bmatrix} v_{l\alpha} & v_{l\beta} \\ v_{l\beta} & -v_{l\alpha} \end{bmatrix} \begin{bmatrix} i_{l\alpha} \\ i_{l\beta} \end{bmatrix} \quad (17)$$

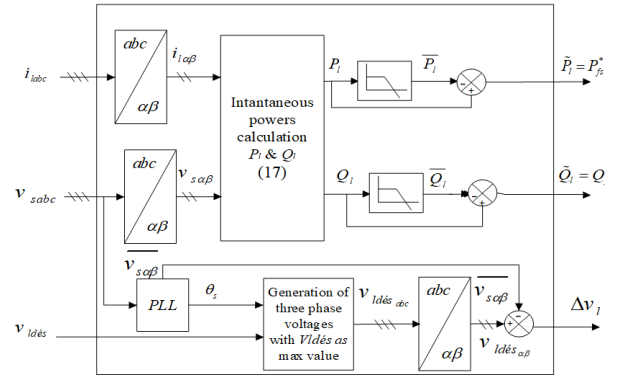
The instantaneous powers can be expressed in the following way:

$$\begin{cases} P_{fs}^* = \tilde{P}_l = P_l - \bar{P}_l \\ Q_{fs}^* = \tilde{Q}_l = Q_l - \bar{Q}_l \end{cases} \quad (18)$$

The second part is to calculate the voltage drop across the load as follows.

$$\begin{bmatrix} \Delta v_{l\alpha} \\ \Delta v_{l\beta} \end{bmatrix} = \begin{bmatrix} v_{des\alpha} \\ v_{des\beta} \end{bmatrix} - \begin{bmatrix} v_{s\alpha} \\ v_{s\beta} \end{bmatrix} \quad (19)$$

Figure 5 represents the schematic diagram of the PQ-PLL theory.



**Figure 5.** Harmonic voltages extraction scheme using PQ-PLL theory

## 2.4 Feedback Linearisation Controller (FLC) synthesis

Consider the nonlinear system represented in:

$$\begin{aligned} \dot{x} &= f(x) + \sum_{i=1}^p g_i(x)u_i, \quad i=1,2,\dots,p \\ y_i &= h_i(x) \end{aligned} \quad (20)$$

where,  $g(x)$  and  $f(x)$  are scalar functions.

The well-known method for forming the previous system's feedback linearisation law is shown in Figure 5 [20]. The problem of determining the system's vector relative degree (13) necessitates differentiation of each output signal until one of the input signals is explicitly included in the differentiation. We define  $r_j$  as the minimal integer for each output signal that has one input in  $y_j^{(r_j)}$  [9]:

$$y_j^{(r_j)} = L_f^{r_j} h_j(x) + \sum_{i=1}^p L_{g_i} (L_f^{r_j-1} h_j(x)) u_i, \quad j=1,2,\dots,p \quad (21)$$

where:  $L_f h_j$  and  $L_{g_i} (L_f^{r_j-1} h_j)$  represent the Lie derivatives of  $h$  with regard to  $f$  and  $g$ .

The global relative degree ( $r$ ) is equal to the total of all relative degrees calculated using (20). It should be less than or equal to the system's order:  $r = \sum_{j=1}^p r_j \leq n$ .

The formula (20) can be represented in its matrix form to obtain the expression of linearising law  $u$  that permits making the relationship between inputs and outputs linear:

$$[y_1^{r_1} \dots y_p^{r_p}]' = \zeta(x) + D(x)u \quad (22)$$

where:

$$\zeta(x) = \begin{bmatrix} L_f^{r_1} h_1(x) \\ L_f^{r_2} h_2(x) \\ \vdots \\ L_f^{r_p} h_p(x) \end{bmatrix}$$

$$D(x) = \begin{bmatrix} L_{g_1} L_f^{r_1-1} h_1 & L_{g_2} L_f^{r_1-1} h_1 & \dots & L_{g_p} L_f^{r_1-1} h_1 \\ L_{g_1} L_f^{r_2-1} h_2 & L_{g_2} L_f^{r_2-1} h_2 & \dots & L_{g_p} L_f^{r_2-1} h_2 \\ \vdots & \vdots & \dots & \vdots \\ L_{g_1} L_f^{r_p-1} h_p & L_{g_2} L_f^{r_p-1} h_p & \dots & L_{g_p} L_f^{r_p-1} h_p \end{bmatrix}$$

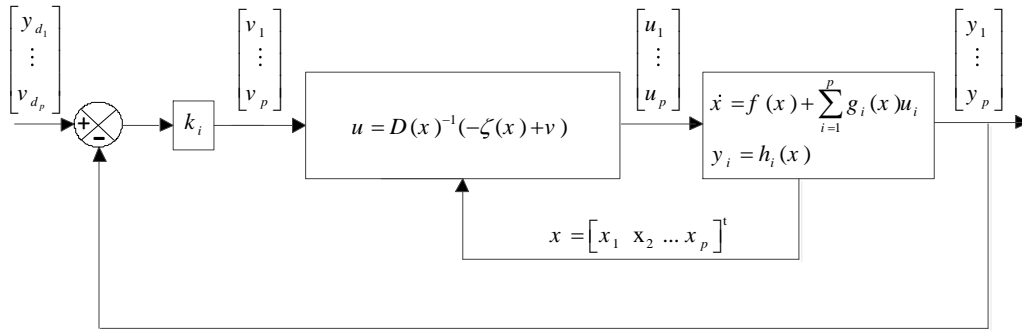
$D(x)$  is called the decoupling matrix system.

The linearizing control law has the following form [9]:

$$u = D(x)^{-1}(-\zeta(x) + v) \quad (23)$$

And

It is important to note that linearisation is only possible if the decoupling matrix  $D(x)$  is reversible. Figure 6 shows the linearised system's block diagram.



**Figure 6.** Block diagram of linearised MIMO system.

#### 2.4.1 Boost FLC synthesis

Each output derivative is given by:

$$\dot{y}_j = L_f h_j(x) + \sum_{i=1}^2 L_{g_i}(L_f h_j(x))u_i \quad j=1,2 \quad (24)$$

Then, the matrix form of (24) can be expressed as:

$$\begin{bmatrix} \dot{y}_{b1} \\ \dot{y}_{b2} \end{bmatrix} = \begin{bmatrix} \frac{1}{L_{pv}} x_{b1} \\ \frac{1}{C_{pv}} x_{b2} \end{bmatrix} + \begin{bmatrix} -\frac{1}{L_{pv}} & 0 \\ 0 & -\frac{1}{C_{pv}} \end{bmatrix} \begin{bmatrix} u_{b1} \\ u_{b2} \end{bmatrix} \quad (25)$$

The decoupling matrix is reversible ( $\det(D_b(x)) \neq 0$ ), then the linearizing control law can be given as:

$$u_b = \begin{bmatrix} u_{b1} \\ u_{b2} \end{bmatrix} = D_b(x_b)^{-1} [-\zeta_b(x_b) + \begin{bmatrix} v_{b1} \\ v_{b2} \end{bmatrix}] \quad (26)$$

By applying the linearisation law, we obtain the following decoupled linear system:

$$\begin{bmatrix} \dot{y}_{b1} \\ \dot{y}_{b2} \end{bmatrix} = \begin{bmatrix} v_{b1} \\ v_{b2} \end{bmatrix} \quad (27)$$

The control law utilised for tracking the reference is:

$$P_{dc}^* = \frac{C_{dc}}{2} v \quad (31)$$

$$v_{b1} = k_{b1}(i_{Lpv}^* - i_{Lpv}) + \frac{di_{Lpv}^*}{dt} \quad (28)$$

$$v_{b2} = k_{b2}(v_{pv}^* - v_{pv}) + \frac{dv_{pv}^*}{dt}$$

where,  $k_{b1}$  and  $k_{b2}$  are positive constants.

From (27) and (28), the control law is given by:

$$v_{dc}^* = v_{pv} + L_{pv}(k_{b1}(i_{Lpv}^* - i_{Lpv}) + \frac{di_{Lpv}^*}{dt}) \quad (29)$$

$$i_{Lpv}^* = i_{pv} + C_{pv}(k_{b2}(v_{pv}^* - v_{pv}) + \frac{dv_{pv}^*}{dt})$$

#### 2.4.2 DC voltage FLC synthesis

The design of the DC link voltage controller is based on (5).

The derivative of the output  $y=h = v_{dc}^2$  is computed as:

$$\dot{y} = L_f h(x) + L_g h(x)u = \frac{2}{C_{dc}} P_{dc} \quad (30)$$

The control  $P_{dc}$  is figured in (30); hence, its relative degree  $r=1$ . The relative degree of this output is equal to the order of the system which clearly corresponds to an exact linearisation [10].

The control is then determined by:

where:  $\dot{y} = v$

For the problem of trajectory tracking defined by  $v_{dc}^*(t)$ , the linearizing control law  $v$  is defined by:

$$v = k_{dc} (v_{dc}^{*2} - v_{dc}^2) + \frac{dv_{dc}^{*2}}{dt} \quad (32)$$

where,  $k_{dc}$  is a positive constant.

## 2.5 Predictive Direct Power Control (PDPC)

### 2.5.1 Parallel Powers PDPC synthesis

The suggested predictive DPC technique is based on a predictive control algorithm that makes instantaneous active and reactive powers equal to their reference values at each sampling period by computing the PVG-UPQC average voltage vector. As a result, as illustrated in Figure 7, instantaneous active and reactive power measurements and commands are employed as input data variables for the predictive control algorithm. At the beginning of each sampling period  $T_e$ , the PVG-UPQC average voltage vector  $V_{fp\alpha\beta}$ , which allows cancellation of instantaneous active and reactive power tracking errors at the end of the sampling period, is computed. Then, 3-level SVM technique is used to generate a sequence of switching states to achieve the control objective with constant switching frequency.

PDPC requires a predictive model of the instantaneous power behavior, which is described in the following steps.

If the sampling period  $T_e$  is infinitely small compared with the fundamental period. The discretization of the Eqns. (3) and (9) yields:

$$\begin{aligned} P_{fp}(k+1) - P_{fp}(k) &= \frac{T_e}{L_{fp}} (-R_{fp} P_{fp}(k) + V_{fp\alpha}(k)) \\ Q_{fp}(k+1) - Q_{fp}(k) &= \frac{T_e}{L_{fp}} (-R_{fp} Q_{fp}(k) + V_{fp\beta}(k)) \end{aligned} \quad (33)$$

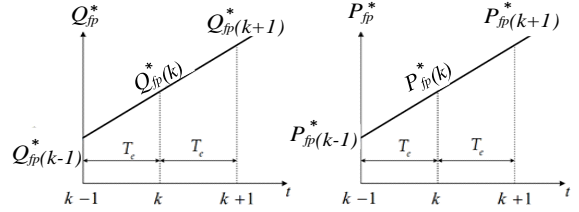
Since the control objective is to force active and reactive powers to be equal to their reference values at the next sampling period, Eq. (33) can be rewritten as follows:

$$\begin{aligned} P_{fp}^*(k+1) = P_{fp}(k+1) &= \frac{T_e}{L_{fp}} (-R_{fp} P_{fp}(k) + V_{fp\alpha}(k)) + P_{fp}(k) \\ Q_{fp}^*(k+1) = Q_{fp}(k+1) &= \frac{T_e}{L_{fp}} (-R_{fp} Q_{fp}(k) + V_{fp\beta}(k)) \\ &+ Q_{fp}(k) \end{aligned} \quad (34)$$

Using (34), the required GPV-UPQC average voltage is given by:

$$\begin{aligned} V_{fp\alpha}(k) &= R_{fp} P_{fp}(k) + \frac{L_{fp}}{T_e} (P_{fp}^*(k+1) - P_{fp}(k)) \\ V_{fp\beta}(k) &= R_{fp} Q_{fp}(k) + \frac{L_{fp}}{T_e} (Q_{fp}^*(k+1) - Q_{fp}(k)) \end{aligned} \quad (35)$$

By using a linear extrapolation, the instantaneous power references at the next sampling period ( $k+1$ ) can be estimated as shown in Figure 7.



**Figure 7.** Predictive value estimation of reference powers

The references for estimated power are as follows:

$$\begin{aligned} P_{fp}^*(k+1) &= 2P_{fp}^*(k) - P_{fp}^*(k-1) \\ Q_{fp}^*(k+1) &= 2Q_{fp}^*(k) - Q_{fp}^*(k-1) \end{aligned} \quad (36)$$

The discrete PDPC control law which provides the required PVG-UPQC average voltage vector to be applied during each sampling period is given by the following equation:

$$\begin{aligned} V_{fp\alpha}^*(k) &= R_{fp} P_{fp}^*(k) + \frac{L_{fp}}{T_e} (\Delta P_{fp}^*(k) + e_{P_{fp}}(k)) \\ V_{fp\beta}^*(k) &= R_{fp} Q_{fp}^*(k) + \frac{L_{fp}}{T_e} (\Delta Q_{fp}^*(k) + e_{Q_{fp}}(k)) \end{aligned} \quad (37)$$

where,  $e_{P_{fp}}(k)$  et  $e_{Q_{fp}}(k)$  are the actual active and reactive power tracking errors defined as:

$$\begin{aligned} e_{P_{fp}}(k) &= P_{fp}^*(k) - P_{fp}(k) \\ e_{Q_{fp}}(k) &= Q_{fp}^*(k) - Q_{fp}(k) \end{aligned} \quad (38)$$

$\Delta P_{fp}^*(k)$  et  $\Delta Q_{fp}^*(k)$  are the actual change in active and reactive power references given by:

$$\begin{aligned} \Delta P_{fp}^*(k) &= P_{fp}^*(k) - P_{fp}^*(k-1) \\ \Delta Q_{fp}^*(k) &= Q_{fp}^*(k) - Q_{fp}^*(k-1) \end{aligned} \quad (39)$$

Once the intermediate voltages  $V_{fp\alpha}^*$  and  $V_{fp\beta}^*$  are obtained, the reference voltages  $v_{fp\alpha}^*$  and  $v_{fp\beta}^*$  can be calculated using (4) as follows:

$$v_{fp\alpha}^* = \frac{v_{s\alpha}}{v_{s\alpha}^2 + v_{s\beta}^2} V_{fp\alpha}^* - \frac{v_{s\beta}}{v_{s\alpha}^2 + v_{s\beta}^2} V_{fp\beta}^* + v_{s\alpha} \quad (40)$$

and,

$$v_{fp\beta}^* = \frac{v_{s\beta}}{v_{s\alpha}^2 + v_{s\beta}^2} V_{fp\alpha}^* + \frac{v_{s\alpha}}{v_{s\alpha}^2 + v_{s\beta}^2} V_{fp\beta}^* + v_{s\beta} \quad (41)$$

### 2.5.2 Series powers PDPC synthesis

By the same manner, the control law used for tracking is given by:

$$\begin{aligned} V_{fs\alpha}^*(k) &= R_{fs} P_{fs}(k) + \frac{L_{fs}}{T_e} (\Delta P_{fs}^*(k) + e_{P_{fs}}(k)) \\ V_{fs\beta}^*(k) &= R_{fs} Q_{fs}(k) + \frac{L_{fs}}{T_e} (\Delta Q_{fs}^*(k) + e_{Q_{fs}}(k)) \end{aligned} \quad (42)$$





$$\begin{aligned} v_x^{A_i^s} t_x^{A_i^s} + v_y^{A_i^s} t_y^{A_i^s} + v_z^{A_i^s} t_z^{A_i^s} &= v_d^* T_s \\ t_x^{A_i^s} + t_y^{A_i^s} + t_z^{A_i^s} &= T_s \end{aligned} \quad (53)$$

where,  $t_x^{A_i^s}$ ,  $t_y^{A_i^s}$  and  $t_z^{A_i^s}$  are the vectors duration times and  $x$ ,  $y$  and  $z$  are the vertices of G, H and K respectively.

The projection of (53) in the frame is composed of two axes affecting  $60^\circ$  between them which leads to:

$$\begin{aligned} v_{x1}^{A_i^s} t_x^{A_i^s} + v_{y1}^{A_i^s} t_y^{A_i^s} + v_{z1}^{A_i^s} t_z^{A_i^s} &= v_1^* T_s \\ v_{x2}^{A_i^s} t_x^{A_i^s} + v_{y2}^{A_i^s} t_y^{A_i^s} + v_{z2}^{A_i^s} t_z^{A_i^s} &= v_2^* T_s \\ t_x^{A_i^s} + t_y^{A_i^s} + t_z^{A_i^s} &= T_s \end{aligned} \quad (54)$$

The coordinates of vertices G, H, N, K, M and L are given in the following equation [26]:

$$\begin{aligned} (v_{G1}^{A_i^s}, v_{G2}^{A_i^s}) &= (0, 0), & (v_{H1}^{A_i^s}, v_{H2}^{A_i^s}) &= (1, 0) \\ (v_{N1}^{A_i^s}, v_{N2}^{A_i^s}) &= (2, 0), & (v_{K1}^{A_i^s}, v_{K2}^{A_i^s}) &= (0, 1) \\ (v_{M1}^{A_i^s}, v_{M2}^{A_i^s}) &= (1, 1), & (v_{L1}^{A_i^s}, v_{L2}^{A_i^s}) &= (0, 2) \end{aligned} \quad (55)$$

By substituting the coordinates of  $v_x$ ,  $v_y$  and  $v_z$  given in (55) in (54), in each triangle, the on-duration time intervals are calculated and summarized in Table 1 [27].

For instance, in the second triangle, the substitution of vector coordinates  $v_x^{A_i^s} = v_G^{A_i^s}$ ,  $v_x^{A_i^s} = v_H^{A_i^s}$  and  $v_x^{A_i^s} = v_K^{A_i^s}$  in Eq. (54) gives the application times of these vectors as follows:

$$\begin{aligned} t_y^{A_i^s} &= (v_1^* - 1)T_s, t_z^{A_i^s} = (v_2^* - 1)T_s \\ t_x^{A_i^s} &= T_s - (t_y^{A_i^s} - t_z^{A_i^s}) \end{aligned} \quad (56)$$

**Table 1.** Duration time in each triangle of sector  $s$

Triangle number	Duration time intervals		
	$t_x^{A_i^s}$	$t_y^{A_i^s}$	$t_z^{A_i^s}$
$\Delta_1^s(G, H, K)$	$T_s - t_y^{A_i^s}$	$v_1^* T_s$	$v_2^* T_s$
$\Delta_2^s(M, K, H)$	$T_s - t_y^{A_i^s}$	$(1 - v_1^*) T_s$	$(1 - v_2^*) T_s$
$\Delta_3^s(H, N, M)$	$T_s - t_y^{A_i^s}$	$(v_1^* - 1) T_s$	$v_2^* T_s$
$\Delta_4^s(K, M, L)$	$T_s - t_y^{A_i^s}$	$v_1^* T_s$	$(v_2^* - 1) T_s$

## 2.7 Comparative PI controller design

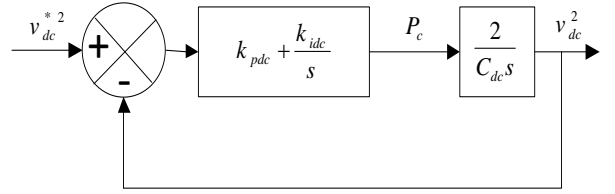
The suggested FL-SVM's performance is compared with that of the PI controller to illustrate its efficiency. As shown below, the design of the PI controller is detailed.

The role of the DC PI controller is to allow tracking the reference by controlling the active power flow between the PCC and the DC bus.

From the Eq. (6), the following transfer function is calculated:

$$\frac{v_{dc}^2(s)}{P_c(s)} = \frac{2}{C_{dc}s} \quad (57)$$

Figure 10 shows a closed-loop schematic of DC voltage regulation.



**Figure 10.** DC voltage Regulation.

The closed loop transfer function is given in:

$$G(s) = \frac{v_{dc}^2(s)}{v_{dc}^{*2}(s)} = \frac{\frac{2k_{pdc}}{C_{dc}}s + \frac{2k_{idc}}{C_{dc}}}{s^2 + \frac{2k_{pdc}}{C_{dc}}s + \frac{2k_{idc}}{C_{dc}}} \quad (58)$$

By the identification of (58) to a second order canonic transfer function (58):

$$H(s) = \frac{2\zeta\omega_n s + \omega_n^2}{s^2 + 2\zeta\omega_n s + \omega_n^2} \quad (59)$$

We can find:

$$\begin{aligned} k_{idc} &= C_{dc}\omega_n^2 / 2 \\ k_{pdc} &= \xi\omega_n C_{dc} \end{aligned} \quad (60)$$

$\omega_n = 2\pi f_n$  is the Natural pulsantance of the controller, and  $0 < \xi < 1$  is the damping factor for a good dynamic and acceptable oscillations, we choose  $f_n = 25\text{Hz}$   $\xi = 0.7$ .

By the same method, we can also obtain the PI coefficients of currents, voltages and Boost controllers as summarized in Table 2 below.

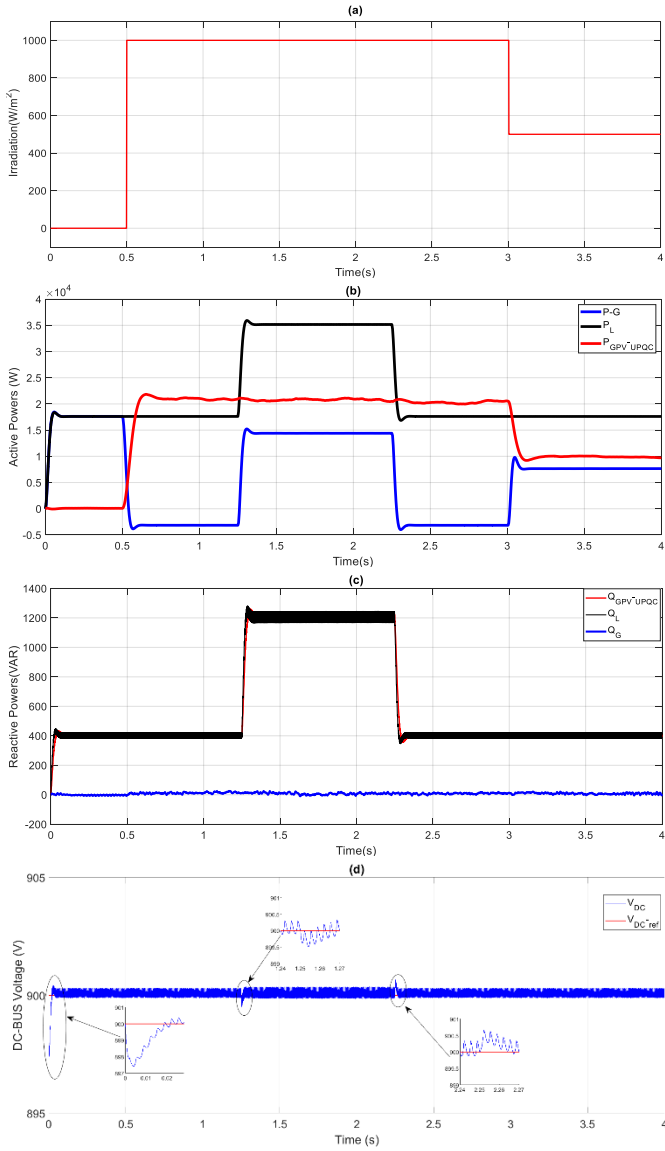
**Table 2.** PI parameters

Coefficients	Value
$k_{pdc}$	22.7
$K_{idc}$	109
$k_{pfp}$	3.5
$K_{ifp}$	355
$k_{pfs}$	0.3
$K_{ifs}$	10
$K_{ppv}$	0.45
$K_{ipv}$	4.6

## 3. RESULTS AND DISCUSSION

Harmonic current and voltage filtering, reactive power compensation and performance of the PVG-UPQC with the proposed control have been examined in Matlab/Simulink environment under nonlinear load variation and voltage sag/swell. The parameters used in the present study are shown in Table 3.





**Figure 11.** Simulation results under weather variation of the suggested controller. a): Variations of irradiations, b): Active power exchange of the PVG-UPQC under weather variations, c): Reactive power exchange of the PVG-UPQC under weather variations, d): DC-link voltage  $v_{dc}$

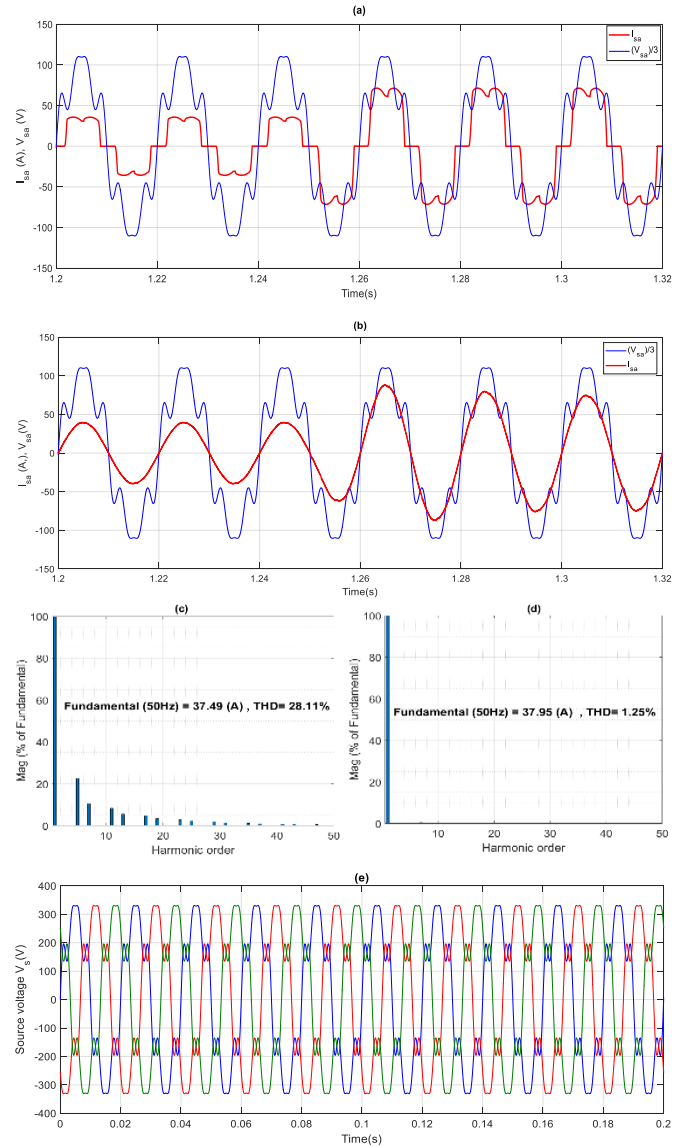
**Table 3.** System parameters

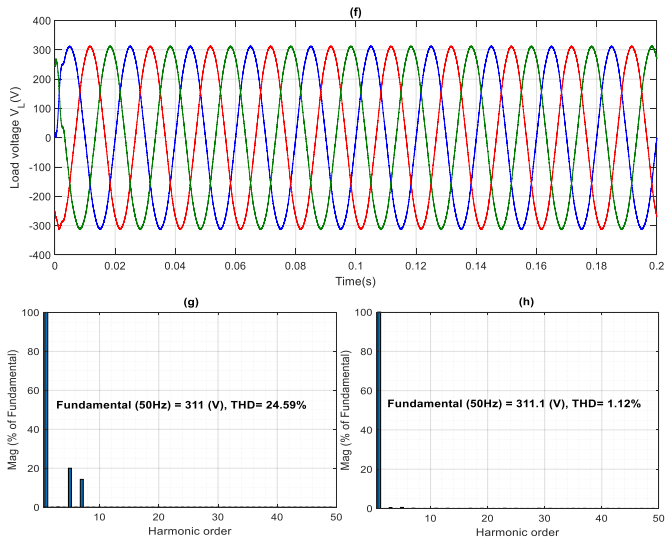
Parameter	value
RMS value of the source voltage	220 V
DC-link capacitor $C_{dc}$	8 mF
Source impedance $R_s, L_s$	3 m $\Omega$ , 2.6 $\mu$ H
Shunt filter impedance $R_{fp}, L_{fp}$	20 m $\Omega$ , 2.5 mH
Series filter impedance $R_{fs}, L_{fs}, C_{fs}$	1.5 $\Omega$ , 3 mH, 0.1 mF
boost converter parameters	5 mH, 55 mF
$L_{pv}, C_{pv}$	
Line impedance $R_l, L_l$	10 m $\Omega$ , 0.3 $\mu$ H
Diode rectifier load $R_d, L_d$	15 $\Omega$ , 2 mH
PV array $P_{pv}, V_{mp}, I_{mp}, I_{sc}, V_{oc}$	150W, 34.5V, 4.35A, 4.75A, 43.5V
DC-link voltage reference	900 V
Switching frequency $f_s$	12 kHz
$k_{p1} = k_{p2}$	1120
$k_{s1} = k_{s2}$	1150
$K_{b1} = k_{b2}$	1450
$k_{dc}$	250

Figure 11(a) illustrates the selected irradiation's profile when the temperature is adjusted to 25°C. Initially, there is no irradiation ( $t < 0.5s$ ), the PVG-UPQC is controlled just to filtrate harmonics and compensate reactive power, while the load is fed by the grid (17.5 kW). Then, irradiation is adjusted to reach 1000 W/m<sup>2</sup>, in this case the injected maximum power is about 21 kW, in this case, the produced power is higher than the power required by the load, so the PVG-UPQC is controlled to filtrate harmonics, compensate reactive power, feed the load and inject power to the grid between  $[t = 0.5s$  and  $t = 1.25s]$  (see Figure 11(b) and (c)). From these figures, it is obvious that throughout the simulation, the consumed active and reactive powers (respectively 17.5 kW and 400 VAR) are equal to the sum of those delivered by the PVG-UPQC and the grid.

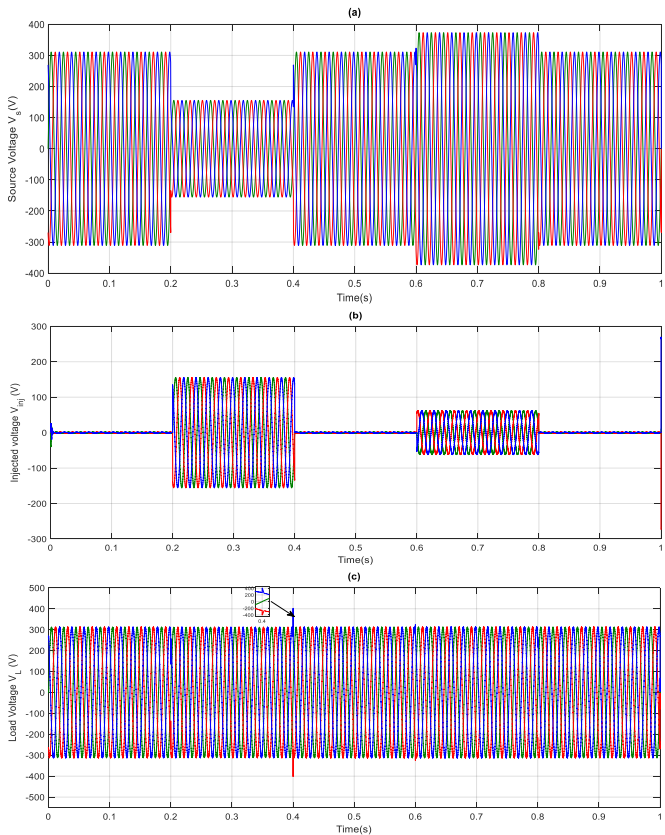
The load variation has a negligible effect on the DC-link voltage (about 2V), and it recovers in around 0.05s (see Figure 11(d)).

The dynamic behavior under an abrupt variation of load, by adding another load having the same value between  $[t = 1.25s$  and  $t = 2.25s]$  which is illustrated in Figures 12(a) and 12(b). It is clear to see that the grid current, after applying the control, is pure sinusoidal, moreover, even in this temporary state, the unity power factor goal is successfully reached.

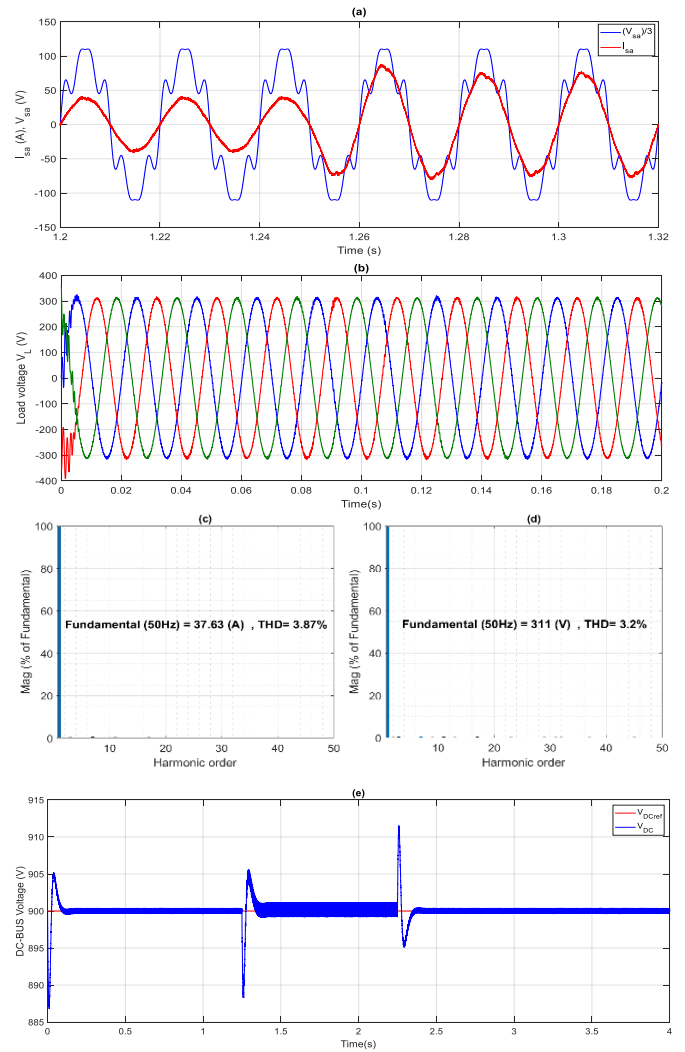




**Figure 12.** Simulation results under load variation of the suggested controller. a): A-phase source voltage with source current before compensation, b): A-phase source voltage with source current after compensation, c): Source current harmonic spectrum before compensation, d): Source current harmonic spectrum after compensation. e): Voltage of the load before compensation. f): Voltage of the load after compensation. g): Harmonic spectrum of load voltage before compensation, h): Load voltage harmonic spectrum after compensation



**Figure 13.** Simulation results during a sag and a swell test of the suggested controller. a): Perturbed source voltage profile. b): Compensation voltage during perturbation. c): Voltage of the load after compensation



**Figure 14.** Simulation results with PI controller. a): A-phase source voltage with source current after compensation, b): Voltage of the load after compensation. c): Source current harmonic spectrum after compensation, d): Load voltage harmonic spectrum after compensation. e): DC bus voltage vdc

From the sag and swell tests illustrated in Figures 13(a) and 13(b), it can be observed that the PVG-UPQC quickly injects equal positive voltage components in the case off sag which are phase-locked to the grid voltage, while in the case of voltage swell, the PVG-UPQC inject negative voltage components in opposite phase with the supply voltage to correct and maintain the load voltage close to its normal value (see Figure 13(c)).

In case of feedback control, the spectral analysis of AC grid current and the voltage of the load with and without compensation are presented in Figures 12(c) and (d), for current in Figures 12(g) and (h) for voltage. For linear control, the same spectrums are shown in Figures 14(c) and (d). It reveals that the UPQC decreases THD in the grid currents from 28.11% to 3.87% with the classic PI controller. whilst, with feedback linearisation based SVM controller, the current THD is decreased to 1.25%. The load voltage THD decreases from 24.59% to 3.2% with PI, while it is further decreased to 1.12% when feedback linearisation based SVM controller is applied which demonstrates the efficiency of the developed nonlinear controller.

The PVG-UPQC was tested with a sag and swell in the grid voltage, and the load voltage was again found quickly very close to a sinusoidal voltage. So, the PVG-UPQC is capable to deliver the required compensating voltage components to keep constant load voltage.

The absence of an overshoot in DC bus voltage response during load variation, rapidity and negligible THD, proves the superiority and the effectiveness of the feedback linearization based SVM controller compared to the traditional linear PI controller as presented in Table 4.

**Table 4.** Comparison of PI controller with FL-PDPC

Factor	PI controller	FL-PDPC controller
THDi (%)	3.87	1.25
THDv (%)	3.2	1.12
Charging of DC link (s)	0.11	0.05
Overshoot	+	-

#### 4. CONCLUSION

In the present paper, a control design of the PVG-UPQC was carried out including its mathematical model and harmonic extraction methods for both currents and voltages. Feedback linearisation combined with predictive DPC controller is derived to suppress currents and voltages harmonics. For the close power switches control, a three-level SVM technique were used due to its benefits in terms of a fixed frequency of implementation. Simulation results divulge that in all stages of the system operation, the load side voltages and source side currents are very close to a sinusoidal shape. These results show clearly that PVG-UPQC controlled by feedback linearisation-based PDPC offers much better performance compared to the traditional controllers' case.

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## NOMENCLATURE

$X_{fp}$	X related to the parallel filter
$X_{fs}$	X related to the series filter
$P$	Active Power (W)
$Q$	Reactive Power (VAR)
$i$	Electrical Current (A)
$v$	Electrical Voltage (V)

## Abbreviation

PVG	Photovoltaic Generator
UPQC	Unified Power quality Conditioner
SVM	Space Vector Modulation
DC	Direct Current
FL	Feedback Linearisation
THD	Total Harmonic Distortion