



Carbonization Law of Fly Ash Concrete under Freeze-Thaw Cycles Based on Image-Pro Plus

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<https://doi.org/10.18280/acsm.440604>

ABSTRACT

Received: 15 June 2020

Accepted: 27 September 2020

Keywords:

IPP, freeze-thaw cycles, ratio of carbonized area (RCA), fly ash concrete, carbonization depth

To understand the influence of freeze-thaw on the carbonization performance of concrete in severe cold areas, this paper conducted experiments to explore the carbonization law of fly ash concrete under freeze-thaw cycles. First, carbonization tests were conducted under different freeze-thaw cycles and fly ash contents; then PS (Photoshop) and IPP (Image-Pro Plus) were adopted to measure the carbonized area and calculate the ratio of carbonized area (RCA). The experimental results showed that, when the fly ash content was between 10% and 30%, RCA increased slowly; when the fly ash content was 20%, the convergence point showed up; when the fly ash content was 0, the air-entrained fly ash concrete had the best resistance to carbonation. With the help of PS and IPP, this paper calculated the RCA more accurately and found that, the freeze-thaw cycles can aggravate carbonization, and there is a linear relationship between carbonization depth and RCA. The research findings in this paper can provide a reference for the durability evaluation and design of concrete structures in severe cold areas.

1. INTRODUCTION

Carbonization is one of the important factors affecting the durability of concrete. Since the early 1960s, China has begun to make great efforts in the study of concrete durability and made great research progress. It is usually believed that concrete undergoes carbonization under general atmospheric environmental conditions, which will cause corrosion of steel bars and ultimately result in insufficient structural durability of the concrete. In cold or severe cold areas, the concrete suffers from freeze-thaw cycles and causes internal cracks or surface peeling off, which will provide favorable conditions for the diffusion of carbon dioxide into its interior, and this is different from the carbonization of concrete under single carbonization condition. Fly ash is a kind of industrial waste residue, now as fly ash concrete is being applied and promoted, its durability problem has become increasingly prominent, which mainly manifested as poor resistance to carbonization and frost, and it is seriously affecting the service life of concrete [1-3].

As for the durability of fly ash concrete under the action of single carbonization or freeze-thaw factor, domestic and foreign scholars have made extensive discussions [4-8] and obtained research results mainly concerning aspects such as the concrete carbonization process and its influencing factors, the prediction of concrete carbonization rate and depth under different fly ash replacement rate, the relationship between fly ash content and carbonization speed, the relationship between carbonization depth and concrete strength, and the damage constitutive model of fly ash concrete under freeze-thaw cycles, etc., and some of these research results have already been applied and promoted in actual projects.

However, the actual environmental conditions of in-service concrete generally contain not only one single condition, Xiao and Gou [9] summarized other conditions that can affect the carbonization performance of concrete, one common condition is the coexistence of freeze-thaw and carbonization, therefore, research on the carbonization performance of concrete under freeze-thaw cycles seems to be particularly important. Some researchers studied the durability of fly ash concrete under the coupling conditions of freeze-thaw and carbonization. For example, Mao et al. analyzed the degradation mechanism of the alternate effects of freeze-thaw and carbonization, and discussed the carbonization depth, the relative dynamic modulus of elasticity, and the mass loss changes; and the mathematical expression of the damage coefficient of composite material $k(F)$ pointed out that the damage of concrete caused by the coupling effect is more serious than that by a single factor [10-13]; Li et al. [14] pointed out that carbonization can improve the frost resistance of concrete to a certain extent within a reasonable range. Rao et al. used computer tomography (CT) and scanning electron microscope (SEM) to study the microscopic characteristics of fly ash concrete under the alternating effects of freeze-thaw and carbonization [15, 16]. Kuosa et al. studied the durability of concrete and high ductility ecological cement base with the coupling of freeze-thaw and carbonization taken into consideration [17, 18].

Generally speaking, there is few researches on the carbonization law of fly ash concrete under freeze-thaw cycles, and there are even fewer studies concerning the carbonization performance of air-entrained fly ash concrete under freeze-thaw cycles. In addition, for concrete damaged by freeze-thaw, the carbonization status of its carbonized fracture surface is

different from the carbonized fracture surface of concrete without freeze-thaw damage, and the carbonation depth measurement method is not accurate enough to study the carbonation law of concrete. Therefore, it is necessary to use a new carbonation indicator to study and analyze the carbonation law of air-entrained fly ash concrete under multiple freeze-thaw cycles.

In order to find a new carbonization indicator to accurately characterize the carbonization performance of concrete, and to obtain the carbonization law of air-entrained concrete under different fly ash contents and different freeze-thaw cycles, this paper designed 5 different kinds of high-performance concrete with different fly ash contents, and carried out freeze-thaw cycle and carbonation tests on them. With the help of IPP and PS, the RCA values of the concrete test pieces were accurately calculated in the paper, and the influence of fly ash content on the carbonization resistance of the concrete was analyzed, the research findings showed that, there's a linear relationship between carbonization depth and the RCA. The research in this paper has practical significance for the design of the durability of hydraulic concrete in severe cold areas.

The content of the paper mainly consisted of four parts: an overview of the experiments, the calculation method for RCA based on IPP, the experimental results and analysis, and the conclusions.

2. EXPERIMENT OVERVIEW

2.1 Preparation of test pieces

The experiment designed 5 types of fly ash concrete with different fly ash contents of 0%, 10%, 20%, 30%, and 40%, and the water-binder ratio was 0.4. The design process of the mix ratios was in accordance with the requirements of *Specification for Mix Proportion design of Ordinary Concrete* (JGJ 55-2011), and the specific mix ratios are shown in Table 1. The experiments used Quzhai (brand name) P.O 42.5 Ordinary Portland Cement, Grade-II fly ash supplied by Baoding mixing plant of Hebei Construction Group, local

gravel of Baoding (particle size 5-20mm, continuous gradation), local river sand of Baoding (fineness modulus 2.78), polycarboxylic water reducing agent, PC-2 type liquid rosin pyrolytic polymer air-entraining agent, and tap water. The slump range was 180mm~200mm, and the extension range was 450mm-550mm.

To figure out the influence of freeze-thaw cycles on the carbonization law of fly ash concrete, this study designed the contrast tests (carbonization only, CO mode) and the FC cycle tests (cyclic freeze-thaw first and carbonization later, FC mode).

2.2 Experiment methods and procedures

The freeze-thaw cycle tests adopted the fast freeze-thaw method, and the equipment was a Najjiuwang (brand name) NJW-HDK-9 microcomputer automatic concrete fast freeze-thaw device; the carbonization tests adopted the fast carbonization method, and the equipment was a CABR-HTX12 type concrete carbonization test box. The tests were carried out in accordance with the *Standard for Test Methods of Long-term Performance and Durability of Ordinary Concrete* (GB/T 50082-2009).

The abbreviations of the symbols and the basic conditions of the experiments are shown in Table 2.

Table 2 was obtained based on the Fick's law of diffusion, and Li et al. [19] and Lin and Ou [20]'s studies about the calculation method of the number of test cycles in different regions, and the provisions of the anti-freeze grade. The influence of relative humidity, temperature and sunshine difference on the carbonization of concrete was ignored, the analysis was mainly based on the Fick's law of diffusion, rapid carbonization time/natural carbonization time = CO₂ concentration of fast carbonization/CO₂ concentration of natural carbonization, the CO₂ concentration of the experiment box of fast carbonization and the CO₂ concentration under natural conditions were respectively 20% and 0.03973%. It can be calculated that F50-C3 and F100-C7 were approximately equivalent to the carbonization time under natural conditions of 4.25 years and 9.75 years, respectively.

Table 1. Mix ratios of fly ash concrete

Group	Cement (Kg)	Fly ash (Kg)	Fly ash content (%)	Water (Kg)
A	407.25	0.00	0	162.90
B	366.53	40.73	10	162.90
C	325.80	81.45	20	162.90
D	285.08	122.18	30	162.90
E	244.35	162.90	40	162.90
Group	Sand (Kg)	Gravel (Kg)	Water reducing agent content (%)	Air-entraining agent content (%)
A	710.67	1159.513	0.300	0.030
B	705.26	1150.683	0.390	0.085
C	699.85	1141.853	0.410	0.110
D	694.43	1133.023	0.445	0.160
E	689.02	1124.193	0.480	0.190

Table 2. Symbol abbreviations and experimental conditions

Symbol	F50-C3	F100-C7
Meaning	In each test cycle, the test pieces were subject to freeze-thaw for 50 times first and fast carbonization for 3 days later.	In each test cycle, the test pieces were subject to freeze-thaw for 100 times first and fast carbonization for 7 days later.
Number of test cycles	4	4
Simulated geographic location	Qinghai-Tibet area	Northeast area
Average annual freeze-thaw cycles	140 cycles	121 cycles
CO ₂ concentration	0.03973%	0.03973%
Equivalent time	17 years	39 years

3. CALCULATION METHOD OF RCA BASED ON IPP

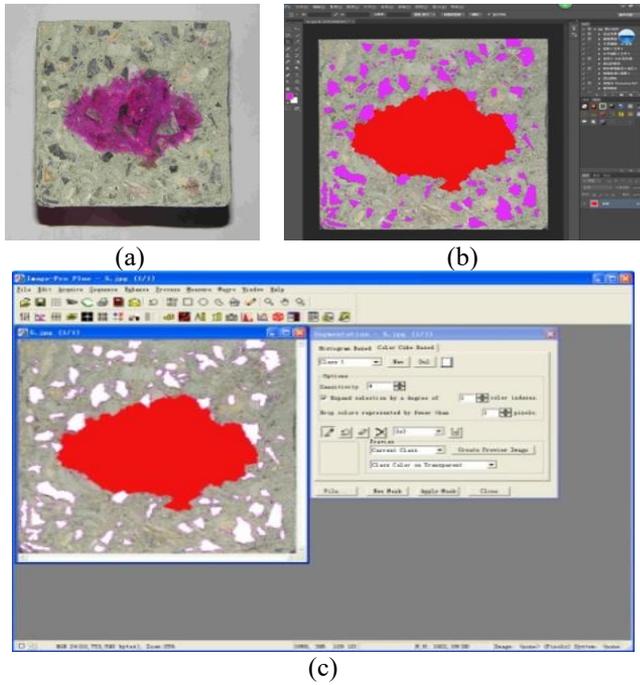


Figure 1. Images of carbonized area measured by IPP

The images were first processed by PS, and the equivalent carbonized area values were then measured by IPP. In this paper, the RCA is denoted as δ , the total measured area is A , the non-carbonized area is A_f , the area of coarse aggregate in the carbonized area is A_{cg} , the carbonized area is A_t , and there is $A = A_f + A_{cg} + A_t$. The specific measurement and calculation steps of RCA are:

(1) The fracture surface was treated with phenolphthalein solution and then placed in a container with a white inner surface, after the color had changed (A_f), pictures were taken by a high-definition digital camera, and original images were obtained (Figure 1a).

(2) The original images were processed by PS to reduce the errors, the coarse aggregate A_f (the part on the fracture surface whose color hadn't changed) and the other parts A_t were colored in different colors (Figure 1b).

(3) A_f, A_t, A_{cg} were measured by IPP (Figure 1c).

(4) The RCA was calculated as: $\delta = A_t / A \times 100\% = A_t / (A_f + A_{cg} + A_t) \times 100\%$.

As shown in the figures, the left and right sides of the test pieces were wrapped with paraffin wax, and the upper and lower sides were not processed.

4. EXPERIMENTAL RESULTS AND ANALYSIS

4.1 Influence of freeze-thaw on RCA

The experiments on the RCA for the two simulated regions of Qinghai-Tibet and Northeast were divided into two groups. The Qinghai-Tibet test groups adopted the CO (carbonization-only) mode and the F50-C3 mode, and the Northeast test groups adopted the CO mode and the F100-C7 mode. The experimental data are shown in Table 3 and Table 4, respectively.

According to Tables 3 and 4, for concrete test pieces with different fly ash contents in the two simulated regions of Qinghai-Tibet and Northeast, the curves of RCA (under different modes) with carbonization age were plotted, as shown in Figures 2 and 3.

Table 3. RCA of fly ash concrete under CO and F50-C3 modes

Group	Fly ash content	Mode	Test piece No.	Carbonization age(d)			
				3	6	9	12
A	0	CO	A2-1	0.019	0.043	0.068	0.096
		F50-C3	A2-3	0.048	0.091	0.115	0.166
B	10%	CO	B2-1	0.116	0.126	0.131	0.150
		F50-C3	B2-3	0.123	0.154	0.177	0.206
C	20%	CO	C2-1	0.155	0.170	0.185	0.196
		F50-C3	C2-3	0.170	0.185	0.206	0.234
D	30%	CO	D2-1	0.177	0.201	0.228	0.254
		F50-C3	D2-3	0.178	0.217	0.267	0.311
E	40%	CO	E2-1	0.205	0.277	0.294	0.317
		F50-C3	E2-3	0.240	0.315	0.361	0.393

Table 4. RCA of fly ash concrete under CO and F100-C7 modes

Group	Fly ash content	Mode	Test piece No.	Carbonization age(d)			
				7	14	21	28
A	0	CO	A2-4	0.048	0.082	0.119	0.157
		F100-C7	A2-6	0.058	0.089	0.137	0.196
B	10%	CO	B2-4	0.137	0.166	0.198	0.220
		F100-C7	B2-6	0.159	0.189	0.203	0.243
C	20%	CO	C2-4	0.171	0.195	0.216	0.246
		F100-C7	C2-6	0.196	0.216	0.257	0.289
D	30%	CO	D2-4	0.201	0.235	0.239	0.279
		F100-C7	D2-6	0.235	0.265	0.301	0.357
E	40%	CO	E2-4	0.213	0.267	0.305	0.355
		F100-C7	E2-6	0.265	0.317	0.365	0.453

According to the curves in Figures 2 and 3, the values of RCA under the CO mode and FC mode all increased with the increase of carbonization age, and the sizes of the increment varied with the fly ash content and the experiment mode; for concrete test pieces with a same fly ash content, the FC mode curves were always above the CO mode curves, indicating that the RCA values of FC mode were higher than those of CO mode, the freeze-thaw cycles had an adverse effect on the carbonization of fly ash concrete, that is, freeze-thaw had aggravated the carbonization. Horizontal comparisons of the RCA values of concrete test pieces with different fly ash contents showed that, regardless of the FC mode or the CO mode, as the content of fly ash increased, the RCA increased as well, indicating that the higher the fly ash content, the greater the RCA value, and this trend was also true for the images in Figure 3.

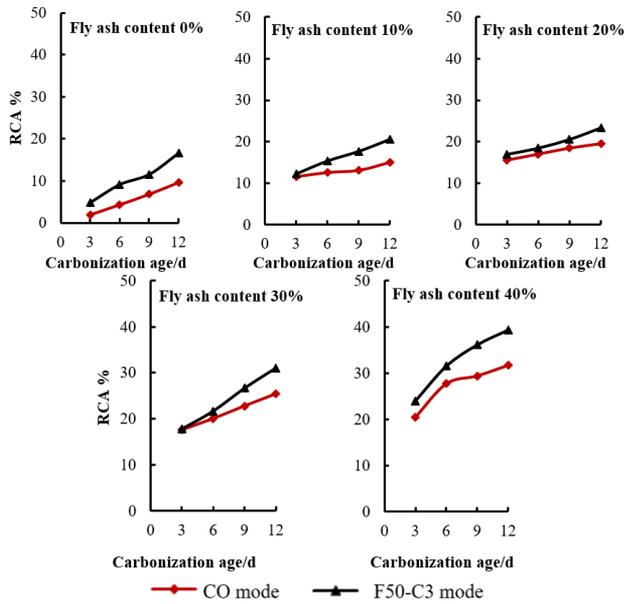


Figure 2. RCA-carbonization age curves of concrete test pieces with different fly ash contents under CO and F50-C3 modes

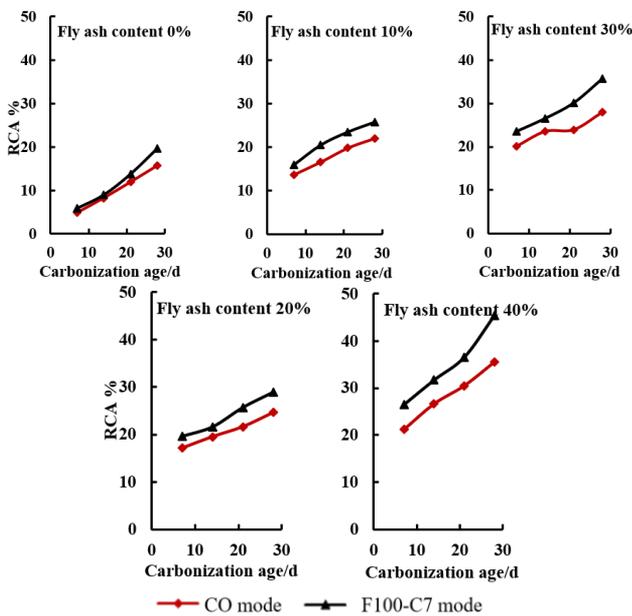


Figure 3. RCA-carbonization age curves of concrete test pieces with different fly ash contents under CO and F100-C7 modes

4.2 Influence of fly ash content on RCA

Figures 4, 5, and 6 showed the RCA-fly ash content relationship under CO mode, F50-C3 mode (Qinghai-Tibet), and F100-C7 mode (Northeast), wherein “FCxd” represents that the test pieces were subject to freeze-thaw cycles first and carbonized for x days later.

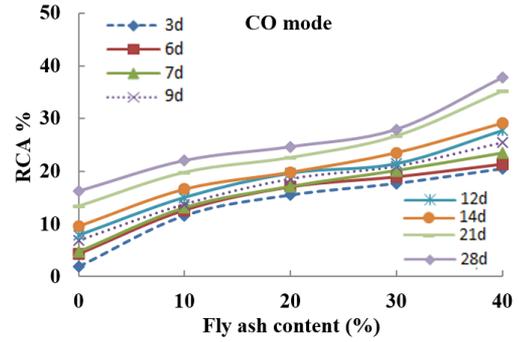


Figure 4. Relationship between RCA and fly ash content under CO mode

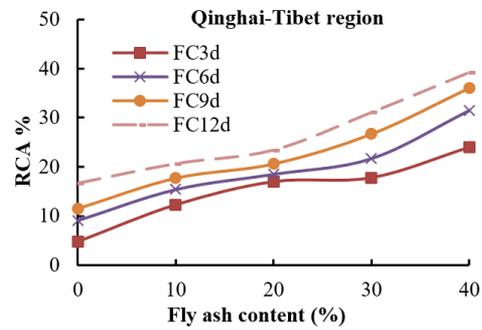


Figure 5. Relationship between RCA and fly ash content under F50-C3 mode

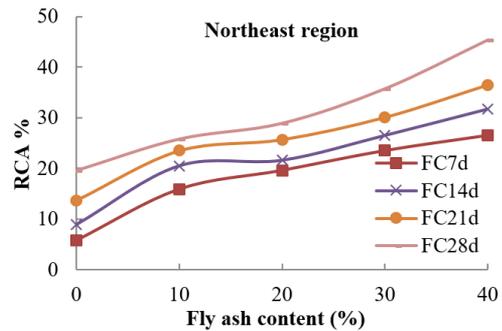


Figure 6. Relationship between RCA and fly ash content under F100-C7 mode

According to Figures 4, 5 and 6, RCA values of CO and FC modes all increased with the increase of fly ash content, and the curves showed a trend of convergence first and divergence later. When the content of fly ash was 20%, the curve reached the convergence point. When the fly ash content was 0, the concrete had the best carbonization resistance. When the fly ash content was between 10% and 30%, the RCA increased slowly. When the content of fly ash was between 10% and 20%, the RCA of fly ash concrete with older carbonization age increased slowly. When the content of fly ash was between 20% and 30%, the RCA of fly ash concrete with younger carbonization age increased slowly.

4.3 Relationship between CRA and carbonization depth

The carbonation depth of concrete under the CO and FC modes were measured, the data is shown in Table 5 and Table 6.

Carbonization depth and RCA can be regarded as two indicators of the carbonation resistance of concrete, and the two have a certain correlation. Figures 7 and 8 respectively show the relationship between carbonization depth and RCA under the CO and FC modes and under different fly ash contents. It can be seen from the figure that, regardless of the

CO or FC mode, overall, the carbonization depth and the RCA showed a linear relationship, which can be expressed as $D=k\delta+b$, wherein D represents the carbonization depth, δ represents the RCA, and b is a constant. Under the CO mode, the value of coefficient k was between 30 and 35, the relationship between carbonization depth and RCA can be approximately expressed as $D=32\delta$; under the FC mode, the value of coefficient k was between 19 and 31, the relationship between carbonization depth and RCA can be approximately expressed as $D=27.5\delta-0.1$.

Table 5. Carbonation depth of fly ash concrete under CO and F50-C3 modes

Group	Fly ash content	Mode	Test piece No.	Carbonization age(d)			
				3	6	9	12
A	0	CO	A2-1	0.5	1.3	2.0	2.9
		F50-C3	A2-3	0.3	1.8	2.5	3.8
B	10%	CO	B2-1	3.2	3.5	4.1	4.5
		F50-C3	B2-3	3.2	3.8	4.9	5.5
C	20%	CO	C2-1	4.6	5.2	5.7	6.0
		F50-C3	C2-3	4.8	5.4	5.9	6.3
D	30%	CO	D2-1	5.0	6.5	6.8	7.1
		F50-C3	D2-3	5.2	6.5	7.0	7.5
E	40%	CO	E2-1	6.1	6.8	8.0	8.7
		F50-C3	E2-3	6.1	7.3	8.5	9.7

Table 6. Carbonation depth of fly ash concrete under CO and F100-C7 modes

Group	Fly ash content	Mode	Test piece No.	Carbonization age (d)			
				7	14	21	28
A	0	CO	A2-4	1.4	2.6	3.9	4.4
		F100-C7	A2-6	1.8	3.1	4.5	5.3
B	10%	CO	B2-4	4.5	5.3	6.6	7.5
		F100-C7	B2-6	5.2	6.1	7.1	7.8
C	20%	CO	C2-4	5.5	6.4	7.2	8.0
		F100-C7	C2-6	5.9	7.1	8.3	8.9
D	30%	CO	D2-4	6.2	7.5	8.0	9.2
		F100-C7	D2-6	6.8	7.8	8.6	10.0
E	40%	CO	E2-4	6.7	8.1	9.0	10.3
		F100-C7	E2-6	7.1	8.8	9.6	11.2

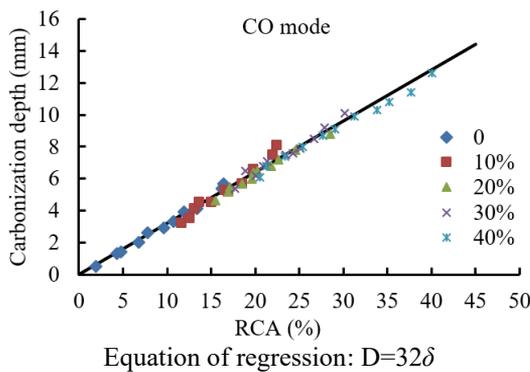


Figure 7. Relationship between carbonization depth and RCA under CO mode

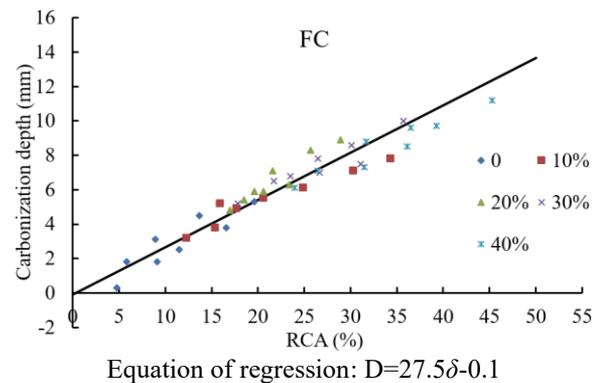


Figure 8. Relationship between carbonization depth and RCA under FC mode

5. CONCLUSIONS

(1) With the help of PS and IPP, this paper accurately measured the carbonized area of concrete and calculated the RCA (ratio of carbonized area), which was then taken as an indicator to characterize the concrete's resistance to carbonization, especially after the test pieces had been subject

to freeze-thaw cycles.

(2) Freeze-thaw cycles can aggravate carbonization, and the carbonization resistance of concrete under CO mode was better than that under the FC mode.

(3) When fly ash content was between 10% and 30%, RCA increased slowly; when fly ash content was 20%, the convergence point showed up; when fly ash content was 0, the

air-entrained fly ash concrete had the best resistance to carbonation.

(4) Regardless of CO or FC mode, there's a linear relationship between carbonization depth and RCA, which can be expressed as $D=32\delta$ and $D=27.5\delta-0.1$, respectively, and the formulas were in good agreement with the experimental results.

ACKNOWLEDGEMENTS

This research in this paper was supported by Project of Baoding City Science & Technology: Study on durability of fly ash Concrete under Coupling Effect of Freeze-thaw and Carbonation (Grant No.: 2011ZG013); the Technology Foundation of Agricultural University of Hebei (No. LG201808); the Provincial Nature Science Foundation of Hebei Province: Study on concrete structure durability based on multi-factor coupling effect (Grant No.: E2015204111); and the Key Project of Provincial Education Department of Hebei Province: Study on durability of existing concrete structures underloading (Grant No.: ZD2016037).

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