



Traffic Flow Prediction Using SPGAPSO-CKRVM Model

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ABSTRACT

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Traffic flow prediction is popular research of ITS. Traffic flow prediction models based on machine learning have recently been widely applied. In this study, we use machine learning algorithms, heuristic algorithms, and parallelization technology to propose a traffic flow prediction model based on Relevance Vector Machine called Genetic Algorithm and Particle Swarm Optimization based on spark parallelization optimized Combined kernel RVM (SPGAPSO-CKRVM). First, combined kernel functions are constructed based on common kernel functions. Second, a parameter optimization algorithm is proposed to optimize the parameters of combined kernel functions by Genetic Algorithm and Particle Swarm Optimization. To reduce time consumed by the parameter optimization algorithm, we parallel the parameter optimization algorithm by Spark. Finally, the proposed model is verified with the real data of Whitemud Drive in Canada. The experimental results indicate that SPGAPSO-CKRVM has greater accuracy than other prediction models and parallelization technology reduce time consumed by the parameter optimization algorithm significantly.

1. INTRODUCTION

The predecessor of Intelligent Traffic Systems (ITS) is Intelligent Vehicle Highway System (IVHS). ITS combines with advanced science and technology such as information technology, sensor technology, automatic control theory, operational research, and artificial intelligence to improve transportation industry. Applications and research of ITS involve highway, railway, civil aviation, water carriage and other modes of transportation [1-3]. Traffic flow prediction is a part of ITS. Travelers and government sectors can receive real-time traffic information and basis of decision for traffic congestion by accurate and reliable results of traffic flow prediction. Sensor systems installed on various road types provide traffic network flow, speed, lane occupancy and other information to realize short-term traffic flow prediction. How to improve the accuracy of traffic flow prediction has always been a research focus in ITS [4, 5]. Traffic flow prediction is a typical time series prediction problem [6]. Machine learning and deep learning provide significant solution for solving complicated time series prediction problems. At present, many machine learning and deep learning algorithms have been used to predict traffic flow, but the accuracy and efficiency of algorithms still have room for improvement. Relevance vector machine (RVM) has extremely short testing speed and excellent generalization ability [7]. RVM is widely used in traffic flow prediction due to periodicity, tidal nature and nonlinearity of traffic flow and demand for real-time prediction [4]. Based on the above reasons, this paper combines RVM, heuristic algorithms and parallelization technology to construct an accurate and efficient traffic flow prediction model called SPGAPSO-CKRVM. The main contributions of this paper are summarized as follows:

- First, we implement RVM based on common kernel functions and combined kernel functions. A new measurement called Peak Hours Accuracy is proposed to evaluate capability of kernel function in traffic flow prediction. According to the experimental results, we select a combined kernel function which combine Polynomial kernel and Gaussian kernel as the kernel function of RVM to realize prediction model.

- Second, for the parameter optimization of combined kernel functions, Genetic Algorithm (GA) and Particle Swarm Optimization (PSO) are used to build a hybrid parameter optimization algorithm in this paper. Because the parameter optimization algorithm is time-consuming, we use parallelization technology based on Spark to parallel parameter optimization algorithm to improve efficiency of algorithm. We name this traffic flow prediction model SPGAPSO-CKRVM. This is the first time to introduce Spark into parameter optimization of RVM.

- Third, we proved that SPGAPSO-CKRVM has better prediction accuracy and efficiency than traditional methods by analyzing experimental results.

The remainder of this paper is organized as follows: the related works are discussed in Section 2. Section 3 outlines the principle of RVM. Section 4 introduces traffic flow prediction model called SPGAPSO-CKRVM. Section 5 carries out experiments and analyzes the experimental results. Finally, Section 6 draws the conclusion.

2. RELATED WORK

There are two main types of research about traffic flow prediction. One type is driven by models. They predict traffic flow by using Auto Regression Moving Average Model

(ARMA) [8], Autoregressive Integrated Moving Average Model (ARIMA) [9], Kalman Filtering [10] and other models. These methods usually assume that time series data is generated by a linear process. So, they establish the relationship among time series data based on a linear relation. Therefore, although the calculation is simple, the accuracy is poor.

The second one such as Support Vector Machine (SVM), Recurrent Neural Network (RNN), RVM and other machine learning and deep learning algorithms is driven by data. Cao and Xu [11] proposed a traffic flow prediction method based on SVM optimized by PSO. It is proved that SVM combined with intelligent algorithms is suitable for prediction traffic flow. Tian et al. [12] proposed a novel approach based on Long Short-Term Memory (LSTM) to predict traffic flow. In addition, the multiscale temporal smoothing is employed to infer lost data in this approach. Fu et al. [13] used LSTM and Gated Recurrent Unit (GRU) to forecast traffic flow respectively. The experimental results show that GRU outperforms LSTM and is significantly better than ARIMA. In recent years, deep models based on deep learning gradually favored by scholars. The deep models improve capability by a new method which extracts the feature of traffic flow information before prediction traffic flow. CNN-LSTM is the most popular one among the deep models [14]. CNN-LSTM extracts the feature such as spatiotemporal feature and periodic feature by convolutional layer to generate a new feature data set. Then input it into LSTM for prediction traffic flow [15]. Liu et al. [16] proposed CNN-Bi-LSTM by replacing LSTM in CNN-LSTM with Bidirectional Long Short Memory Network(Bi-LSTM). CNN-LSTM has better accuracy than other deep learning algorithms based on RNN. Extracting feature by convolutional layer can be regarded as reducing dimensionality of data. So, CNN-LSTM has better efficiency than LSTM and GRU, but the advantage is not significant in traffic flow prediction.

RVM was proposed as a sparse probability model based on Bayesian frame in 2000. RVM has extremely short testing speed and prediction accuracy similar to SVM, LSTM and GRU. Therefore, RVM is often regarded as an optimized version of SVM. The parameter optimization of RVM kernel functions is an unavoidable problem for every research about RVM. Accuracy of RVM without parameter optimization is not ideal. For this problem, Jin and Hui [17] used GA to optimize RVM to prove that the intelligent algorithms improve capability of RVM. Shen et al. [18] proposed a hybrid algorithm called Chaos Simulated Annealing Algorithm (CSA) and used it to optimize RVM to predict traffic flow. This method has better prediction accuracy than model-driven methods such as seasonal auto regressive integrated moving average (SARIMA). Shen et al. [19] also used CSA to optimize RVM. By comparing with RVR-GA, SVR-GA, BPNN-GA and other algorithms, Shen et al. proved that their method has better capability. They only used the advantage that RVM has short testing time in their respective prediction models without considering the efficiency of parameter optimization algorithms of RVM. In previous research, for machine learning algorithms such as SVM and RVM, we found that the time consumed by the parameter optimization algorithm accounts for 80%-95% of the overall training time [4]. The efficiency of parameter optimization algorithms greatly affects the efficiency of overall algorithm.

Currently, the efficiency of parameter optimization algorithms in machine learning is researched less. Most of this

research focus on Grid Search (GS). Wu and Ning [20] used Hadoop to parallel GS and used it to optimize SVM. This method can only increase the efficiency of GS by 50%. Li et al. [21] paralleled GS by Spark, based on this design, proved that using of Spark parallelization technology can improve the efficiency of parameter optimization algorithms significantly without reducing its accuracy.

3. PRINCIPLE OF RELEVANCE VECTOR MACHINE

RVM is a supervised learning algorithm proposed by Micnacl E. Tipping in 2000. RVM has the advantages of SVM and overcomes the disadvantages of SVM such as support vectors too many to calculate slowly, long testing time, kernel functions must meet Mercer's theorem [7]. Micnacl E. Tipping realize RVM as a sparse model with Automatic Relevance Determination (ARD) to reflect the central features of data and reduce calculation in testing step. The basic mathematical model of RVM can be represented as:

$$y(x, \omega) = \sum_{i=1}^N \omega_i K(X, X_i) + \varepsilon_n \quad (1)$$

where, ω_i is weight of sample. ω_i is non-zero when X_i belongs to the relevance vector. $K(X, X_i)$ is kernel function of RVM. N is total number of samples. ε_n is Gaussian noise that follows Gaussian distribution $(0, \sigma^2)$. For $t_n=y(x, \omega)+\varepsilon_n$, since t_n is independently distributed, the likelihood function of training set as follows:

$$P(t|\omega, \sigma^2) \sim N(0, \sigma^2) \\ P(t|\omega, \sigma^2) = (2\pi\sigma^2)^{-\frac{N}{2}} \exp\left(-\frac{1}{2\sigma^2} \|t - \phi\omega\|^2\right) \quad (2)$$

If Eq. (2) is directly maximized by Structural Risk Minimization (SRM) will cause serious overfitting problems. Therefore, ω_i should be defined to satisfy the Gaussian prior probability distribution. It is as follows:

$$P(\omega|\alpha) = \prod_{i=0}^N N(\omega_i|0, \alpha_i^{-1}) \\ = \prod_{i=0}^N \sqrt{\frac{\alpha_i}{2\pi}} \exp\left(-\frac{\alpha_i}{2} \omega_i^2\right) \quad (3)$$

where, $\alpha=[\alpha_0, \alpha_1, \alpha_2, \dots, \alpha_N]^T$ is hyperparameter that determines the prior distribution of ω_i . The posterior distribution of ω_i can be calculated by Bayesian formula as follows:

$$P(\omega|t, \alpha, \sigma^2) = \frac{P(t|\omega, \sigma^2)P(\omega|\alpha)}{P(t|\alpha, \sigma^2)} \quad (4)$$

where, $P(\omega|t, \alpha, \sigma^2)$ follows Gaussian distribution. It's mean value and covariance can be represented as:

$$\mu = \sigma^{-2} \rho \phi^T t \quad (5)$$

$$\rho = (\sigma^{-2} \phi^T \phi + A)^{-1}, A=\text{diag}(\alpha_0, \alpha_1, \dots, \alpha_N) \quad (6)$$

For estimating weights of the model, the optimal value of

hyperparameters should be estimated firstly. Suppose α follows the Gamma Distribution, the likelihood distribution of hyperparameters can be represented as:

$$P(t|\alpha, \sigma^2) = \int P(t|\omega, \sigma^2) P(\omega|\alpha) d\omega \quad (7)$$

We can calculate an approximate solution (α_M, σ_M^2) by maximizing $P(t|\alpha, \sigma^2)$. Then, repeat Eq. 8 by MacKay [22] and update μ and ρ simultaneously until meet the convergence condition.

$$\alpha_i^{new} = \frac{\gamma_i}{\mu_i^2}, (\sigma^2)^{new} = \frac{\|t - \rho\mu\|^2}{N - \rho_i\gamma_i} \quad (8)$$

Most of α_i tend to infinity and ω_i corresponding to α_i tend to zero during the iteration. That is why RVM is a sparse probability model. Where, samples learned by non-zero ω_i called relevance vector. After the convergence process, we can estimate x_p by Eq. (9) and Eq. (10).

$$P(t_p|t, \alpha_M, \sigma_M^2) = N(t_p|y_p, \sigma_p^2) \quad (9)$$

$$y_p = \mu^T \phi(x_p), \sigma_p^2 = \sigma_M^2 + \phi(x_p)^T \rho \phi(x_p) \quad (10)$$

where, x_p is the data to be tested. y_p is predictive value of RVM.

RVM has same functional form as SVM and deal with nonlinear problems by Kernel Trick. But RVM has shorter testing time than SVM because it is a sparse probability model and the accuracy is similar to SVM. So RVM is more suitable for predicting traffic flow.

4. TRAFFIC FLOW PREDICTION MODEL BASED ON SPGAPSO-CKRVM

4.1 Combined kernel

In the current study, most of RVM used single kernel

$$X = \begin{bmatrix} \vec{x}_1 \\ \vec{x}_2 \\ \dots \\ \vec{x}_N \end{bmatrix} = \begin{bmatrix} x_1^{i-7n,j} & x_1^{i-7n+7,j} & \dots & x_1^{i-7,j} & x_1^{i,j-m} & \dots & x_1^{i,j-1} & x_1^{i,j} \\ x_2^{i-7n,j} & x_2^{i-7n+7,j} & \dots & x_2^{i-7,j} & x_2^{i,j-m} & \dots & x_2^{i,j-1} & x_2^{i,j} \\ \dots & \dots \\ x_N^{i-7n,j} & x_N^{i-7n+7,j} & \dots & x_N^{i-7,j} & x_N^{i,j-m} & \dots & x_N^{i,j-1} & x_N^{i,j} \end{bmatrix} \quad (13)$$

where, $(x_1^{i,j}, x_2^{i,j}, \dots, x_N^{i,j})^T$ is the prediction target. i represents the date. j represents the time points. $(x_{i,j-m}, x_{i,j-m-1}, \dots, x_{i,j-1})$ represents the traffic volume at m time points before the j^{th} time point in the i^{th} day. $(x_{i-7n,j}, x_{i-7n+7,j}, \dots, x_{i-7,j})$ represents the traffic volume at the j^{th} time point in n days before the i^{th} day. The reason for this is, the traffic volume at a certain time is often affected by the traffic volume at the same time in the previous n weeks. m is often called ‘‘training step’’ or ‘‘time-window’’. m and n are positive integers. According to the experimental data we used, we set $m=10, n=3$.

4.3 Parameter optimization algorithm of RVM based on combined kernel

Parameter optimization problem of RVM based on combined kernel is different from general parameter optimization problem of RVM. λ in the combined kernel function as shown in Eq. (11) and Eq. (12) is also

functions such as Linear kernel, Polynomial kernel, Gaussian kernel, Sigmoid kernel, and Laplace kernel to complete the mapping process in feature space. Where, Linear kernel and Polynomial kernel have better capability in single-dimensional and low-dimensional problems. Gaussian kernel and Sigmoid kernel are used widely in high-dimensional problems and classification problems. Single kernel functions have poor capability when the samples are large and distributed unevenly in the high-dimensional space [23, 24]. So, we combine single kernel functions to construct a combined kernel function. Combined kernel functions as shown in the Eq. (11) and Eq. (12).

$$f(x, x_i) = \exp\left(-\frac{\|x - x_i\|^2}{2\sigma^2}\right) \lambda + (1-\lambda)[\gamma(xx_i + 1)^d + c] \quad (11)$$

$$f(x, x_i) = \exp\left(-\frac{\|x - x_i\|}{2\sigma^2}\right) \lambda + (1-\lambda)[\gamma(xx_i + 1)^d + c] \quad (12)$$

There is no need to prove availability of the combined kernel functions shown in Eq. (11) and Eq. (12), because kernel functions of RVM do not need to meet Mercer’s theorem. The combined kernel functions make RVM get local learning ability of Gaussian kernel and Laplace kernel and generalization of Polynomial kernel. Where, σ is width of kernel function. γ determines the distribution of the data in high-dimensional space. λ is weight coefficient. It meets $0 \leq \lambda \leq 1$.

4.2 Input of model

In the current study, the time span of short-term traffic flow prediction is not shorter than 10 min. The shorter the time span, the more valuable the model. So, we deal with traffic flow data into 5 min time span. The input of the prediction model designed in this paper is:

hyperparameter which need to be optimized. The mathematical model of the parameter optimization algorithm proposed in this paper as follows:

$$P = \{\sigma_{best}, \lambda_{best}, \gamma_{best}\} \quad (14)$$

We design the parameter optimization algorithm of RVM with GA and PSO. First, initialize two populations randomly and run GA and PSO respectively based on the two populations to generate next generation population. A population represents many P . Then, choose the better one of the two populations by calculating the individual fitness in each iteration. Use the population which is chosen as input for the next iteration. Where, the update formula of σ_{best} as follows:

$$\sigma_{best} = \begin{cases} \sigma_{gabest}, & fitness_{ga} \geq fitness_{ps0} \\ \sigma_{psobest}, & fitness_{ga} \leq fitness_{ps0} \end{cases} \quad (15)$$

The update formulas of γ_{best} and λ_{best} are similar to Eq. (15). Because both GA and PSO optimize parameter with iteration, the parameter optimization algorithm designed by us takes advantages of GA and PSO simultaneously. Input $\{\sigma_{best}, \lambda_{best}, \gamma_{best}\}$ obtained by updating of σ_{best} , γ_{best} and λ_{best} as parameters of RVM to calculate the accuracy $p_{Accuracy}$ of prediction model. Define $p_{Accuracy}$ as the objective function of the parameter optimization problem. We get:

$$\begin{aligned} \max p_{Accuracy} &= \text{RVM}\{\sigma_{best}, \lambda_{best}, \gamma_{best}\} \\ \text{s. t. } &\begin{cases} 2^{\sigma_{min}} \leq \sigma_{best} \leq 2^{\sigma_{max}} \\ \gamma_{min} \leq \gamma_{best} \leq \gamma_{max} \\ 0 \leq \lambda_{best} \leq 1 \end{cases} \end{aligned} \quad (16)$$

where, $2^{\sigma_{min}}$ and $2^{\sigma_{max}}$ mean variation range of σ_{best} . Generally, $2^{\sigma_{min}}=-8$ and $2^{\sigma_{max}}=8$. γ_{min} and γ_{max} mean variation range of γ_{best} . Generally, $\gamma_{min}=0$ and $\gamma_{max}=+\infty$. Terminate iteration of parameter optimization algorithm until the termination condition is met. The termination condition as follows:

$$\begin{aligned} \min\{fitness_{ga}, fitness_{ps0}\} &\leq fitness_{min} \\ \text{or } T &\leq T_{max} \end{aligned} \quad (17)$$

where, $fitness_{min}$ is minimum fitness (i.e. acceptable minimum error of prediction model). T is times of iteration. T_{max} is maximum times of iteration.

4.3.1 Details of GA

For parameter optimization algorithm of RVM, Binary encoding is the most common coding method. GA evaluates each P by fitness function to guide parameter optimization into a good direction. We use mean-square error (MSE) of RVM as fitness function.

After calculating fitness, choose individuals in population by Roulette Wheel Selection. Then, use selected individuals to generate a new population with crossover and mutation [25].

4.3.2 Details of PSO

PSO evaluates each P by MSE of RVM similarly as GA. Find individual extremum and global extremum by the results of calculating fitness [26]. Then update the speed and position of each particles by Eq. (18) and Eq. (19).

$$v = v_i + c_1 r_1 (p_{best} - x_i) + c_2 r_2 (G_{best} - x_i) \quad (18)$$

$$x = x_i - v_i \quad (19)$$

where, v is updated velocity of particle. x is updated position of particle. v_i is current velocity of particle. x_i is current position of particle. c_1 and c_2 are called learning factor and determine the learning step. r_1 and r_2 are random numbers from zero to one. p_{best} is individual extremum. G_{best} is global extremum.

4.4 Time-consuming analysis of parameter optimization algorithm

GA and PSO in parameter optimization algorithm designed in this paper can be divided into three parts—population initiation, population update and fitness calculation. The structure of parameter optimization algorithm is shown in Figure 1.

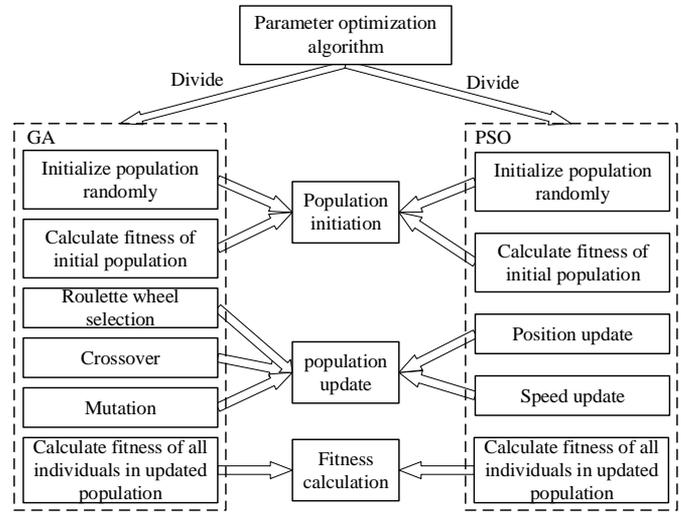


Figure 1. The structure of parameter optimization algorithm

As Figure 1 shows that population initiation includes two parts—initialize the population randomly and calculate fitness of the initial population. Population update includes five parts—roulette wheel selection, crossover, mutation, speed update and position update. Fitness calculation is responsible for calculating the fitness of all individuals in the updated population.

Run parameter optimization algorithm designed in this paper twenty times to collect the time consumed by each part in the algorithm. Where, $T_{max}=20$ and population size is 10. The results are shown in Figure 2.

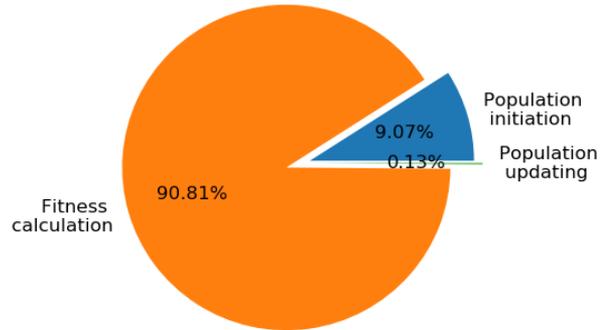


Figure 2. Time consumed by each part in parameter optimization algorithm

The Figure 2 shows that fitness calculation consumes the most time and accounts for more than 90% of the total time. The time spends on population update with complex calculation logic only accounts for about 0.1% of the total time. So, for fitness calculation is the most time-consuming, we parallel parameter optimization algorithm to reduce runtime of calculation fitness by Spark.

4.5 Parallel design

Spark is a fast and universal computing engine designed for processing largescale data [27]. Spark can operate algorithms which require iterative calculation such as data mining algorithms and machine learning algorithms better than other computing engines. Parallel design of SPGAPSO-CKRVM depends on Resilient Distributed Datasets (RDD) in Spark

mainly [28]. The overall process of SPGAPSO-CKRVM is shown in the Figure 3.

Step 1. Initialize parameters of Spark such as default.parallelism, executor.cores and num-executors. Default.parallelism is the default number of partitions in RDD. Executor-cores controls the number of cores occupied by each executor. Num-executors is total number of executors. Read experimental data from external files and normalize experimental data based on extremum to compress the data into [0, 1]. Normalized calculation as follows:

$$X_{norm} = \frac{X - X_{min}}{X_{max} - X_{min}} \quad (20)$$

After normalizing data, generate multiple groups of $\{\sigma_{best}, \lambda_{best}, \gamma_{best}\}$ randomly as the initial population and create RDD with the initial population.

Step 2. Divide the initial population into multiple subpopulations. Calculate the individual fitness of each subpopulation in parallel by *map()*. According to laziness of RDD, trigger the calculation of *map()* by *collect()* to convert subpopulations to lists. Then, operate SP-GA with some subpopulations and operate SP-SPO with others.

Step 3. In SP-GA, choose individuals based on the calculation results of individual fitness and principle of roulette wheel selection. The probability that an individual is selected as:

$$P(x_i) = \frac{fitness(x_i)}{\sum_{j=1}^N fitness(x_j)} \quad (21)$$

It means that the better the individual, the greater probability that the individual is selected. Then, use selected individuals to generate a new population with crossover and mutation.

In SP-PSO, update the speed and position of each particle according to Eq. (18) and Eq. (19) to generate a new population. Then, recalculate individual fitness in parallel by the method in Step2. Compare the individual fitness of individual in the two next-generation populations and keep the better one.

Step 4. Decode the results obtained in STEP 3 to $\{\sigma, \lambda, \gamma\}$. Use the $\{\sigma, \lambda, \gamma\}$ as parameters of RVM to verify $p_{Accuracy}$ of the model. If $p_{Accuracy}$ less than $fitness_{min}$, output the $\{\sigma, \lambda, \gamma\}$ as $\{\sigma_{best}, \lambda_{best}, \gamma_{best}\}$. If $p_{Accuracy}$ more than $fitness_{min}$, repeat Step 3.

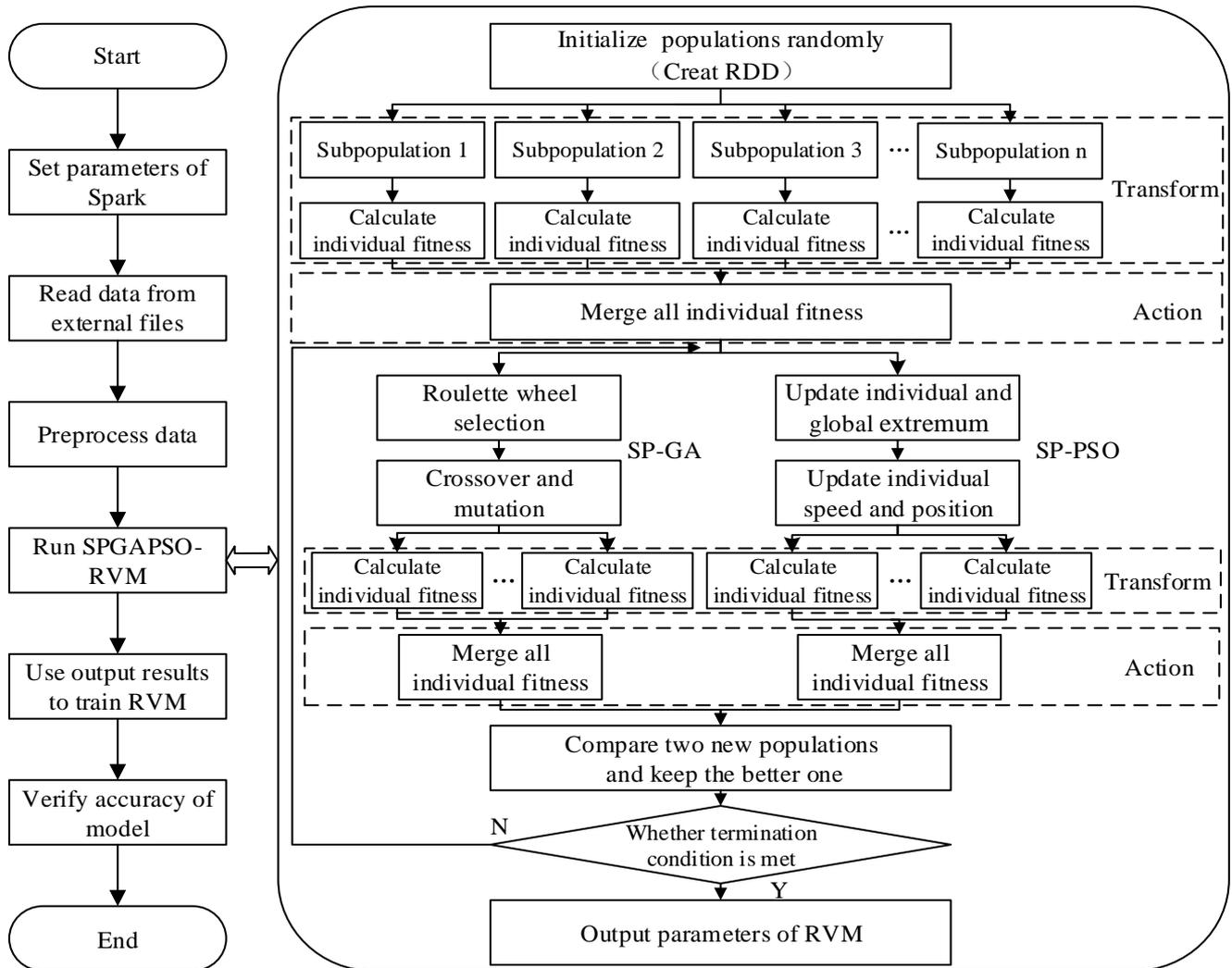


Figure 3. Algorithm flow chart of SPGAPSO-CKRVM

5. EXPERIMENTS AND RESULTS ANALYSIS

5.1 Experimental data

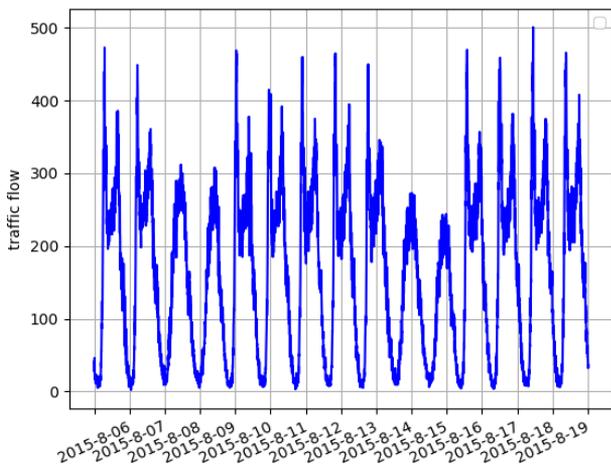
The traffic flow data employed in the experiments were collected by the Intelligent Transportation Research Center at university of Alberta which used ground induction coils to collect data from Whitemud Drive motorway in Canada. Collection frequency of the data is 20s. The traffic flow data were obtained from 6 August 2015 to 27 August 2015 to construct a training set to train SPGAPSO-CKRVM and predict the traffic flow at 0:00 to 24:00 on 28 August 2015. The information for the selected traffic sections in the experiments is as follows:

Sections 1: The eastbound lane of Whitemud Drive, station ID 1027

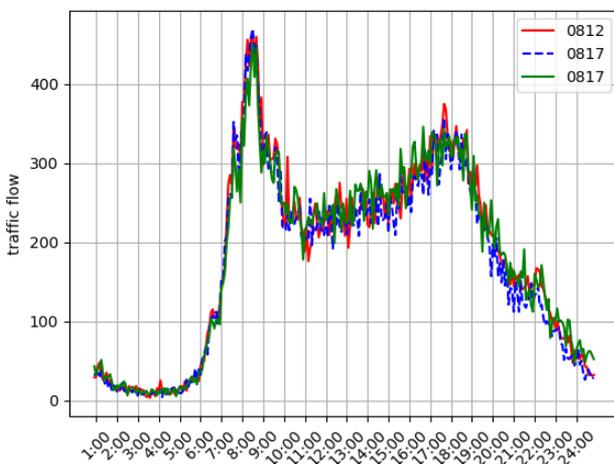
Sections 2: The westbound lane of Whitemud Drive, station ID 1036

Sections 3: The ramp of the westbound lane of Whitemud Drive, station ID 1042

Use historical trend method and exponential smoothing method to repair data missed by fault of equipment [29]. Part of the experimental data after repairing as shown in Figure 4. As the Figure 4a shows, the experimental data has obvious continuity, periodicity, and tidal nature. As the Figure 4b shows, daily peak of traffic flow is from 7:00 to 9:00 and from 16:00 to 19:00.



(a) Data from August 6 to 19 at station ID 1027



(b) Data of three days at station ID 1027

Figure 4. Part of the experimental data

5.2 Experimental environment and related parameter

We verify SPGAPSO-CKRVM with an 8-node Spark cluster built by virtual machines. The cluster includes CentOS-6.10-x64, Spark2.1.1-bin-hadoop2.7, hadoop-2.7.2.tar, pyspark-2.3.2 and py4j-0.10.8.1. The parameters of SPGAPSO-CKRVM are shown in Table 1.

Table 1. The parameters of SPGAPSO-CKRVM

Parameter	Value
Population size	10
Maximum times of iterations	20
Minimum fitness	10^{-5}
Crossover rate	0.6
Mutation rate	0.2
Learning factor	1.5
Particle velocity	[-0.2,0.2]
Particle position	[-8,8]

5.3 Experimental results analysis

Because traffic congestion, travel delay, and road accidents mostly occur in daily peak of traffic flow, predicting the traffic flow in daily peak is more meaningful than predicting the traffic flow in other time [30-32]. For traffic flow prediction, a kernel function which predicts traffic flow in daily peak accurately should be considered to have greater performance. First, we use accuracy (i.e. 1-MAPE) to verify kernel function performance. In addition, we define Peak Hour Accuracy (PHA) (i.e. accuracy of predicting traffic flow from 7:00 to 9:00 and from 16:00 to 19:00) to verify kernel function performance. The experimental results are shown in Table 2.

Because the traffic data of ramp is more random and difficult to predict than the traffic data of general road, the accuracy of all kernel functions on Sections 1 and Sections 2 are greater than that of Sections 3. As shown in Table 2, the performance of combined kernel functions (i.e. No.5 and No.6 kernel functions) are generally better than the performance of the single kernel functions (i.e. kernel functions from No.1 to No.4.). Except in Sections 1, the accuracy of No.6 kernel function is always greater than that of No.5 kernel function. In all Sections, PHA of No.6 kernel function is always greater than that of No.5 kernel function. Therefore, we use No.6 kernel function as the kernel function of RVM for subsequent experiments.

Different prediction models based on machine learning and deep learning, namely the proposed SPGAPSO-CKRVM, SPGAPSO-SVM, GA-CKRVM, PSO-SVR, LSTM, CNN-LSTM, CNN-GRU, CNN-Bi-LSTM were applied herein. Where, SPGAPSO-SVM represents SVM optimized by the same parameter optimization algorithm as SPGAPSO-CKRVM. GA-CKRVM represents RVM based on combined kernel function optimized by GA. PSO-SVR represents a model based on SVM optimized by PSO. CNN-GRU represents a deep model based on CNN and GRU. Table 3 lists the RMSE, MAE and MAPE for the different prediction models.

As shown in Table 3, PSO-SVR has the worst performance. Deep learning models based on RNN such as LSTM, CNN-LSTM, CNN-GRU and CNN-Bi-LSTM are significantly better than models based on SVM. SPGAPSO-SVM and GA-CKRVM are slightly better than the above models in certain sections. In all sections, SPGAPSO-CKRVM is always superior to other comparison models. Figure 5 clearly illustrate

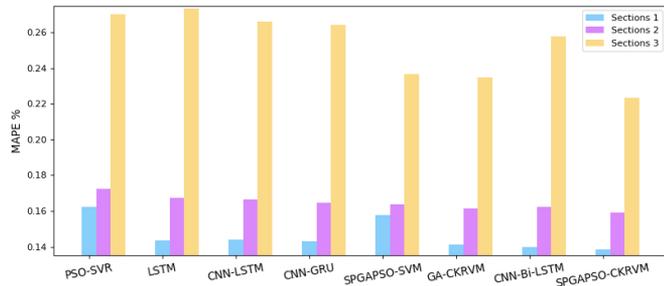
MAPE and RMSE of the various prediction models on different traffic sections.

Table 2. Experimental results of kernel function performance

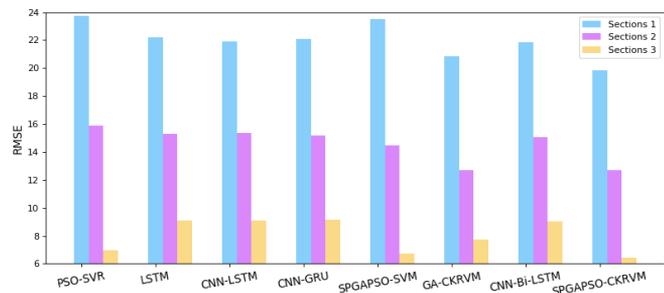
NO.	kernel function	Sections 1		Sections 2		Sections 3	
		Accuracy	PHA	Accuracy	PHA	Accuracy	PHA
1	$\exp\left(-\frac{\ x-x_i\ }{2\sigma^2}\right)$	0.8084	0.8717	0.7964	0.8576	0.7131	0.8187
2	$\exp\left(-\frac{\ x-x_i\ ^2}{2\sigma^2}\right)$	0.8520	0.9292	0.8355	0.9057	0.7452	0.8515
3	$x^T x_i$	0.8529	0.9282	0.8310	0.9011	0.7472	0.8508
4	$\gamma(xx_i + 1)^d + c$	0.8514	0.9272	0.8367	0.9056	0.7544	0.8502
5	$\exp\left(-\frac{\ x-x_i\ }{2\sigma^2}\right)\lambda + (1-\lambda)[\gamma(xx_i + 1)^d + c]$	0.8529	0.9301	0.8368	0.9059	0.7554	0.8521
6	$\exp\left(-\frac{\ x-x_i\ ^2}{2\sigma^2}\right)\lambda + (1-\lambda)[\gamma(xx_i + 1)^d + c]$	0.8535	0.9333	0.8387	0.9061	0.7555	0.8538

Table 3. Experimental results of algorithm accuracy

Algorithm	Sections 1			Sections 2			Sections 3		
	MSE	RMSE	MAPE	MSE	RMSE	MAPE	MSE	RMSE	MAPE
PSO-SVR [33]	564.06	23.75	0.1624	251.54	15.86	0.1724	48.86	6.99	0.2701
LSTM	493.13	22.21	0.1435	234.37	15.31	0.1689	82.88	9.10	0.2702
CNN-LSTM [15]	483.18	21.92	0.1438	235.89	15.36	0.1663	82.43	9.08	0.2659
CNN-GRU [34]	487.46	22.07	0.1429	229.62	15.15	0.1648	84.10	9.17	0.2852
SPGAPSO-SVM	551	23.47	0.1577	210	14.49	0.1638	45.08	6.71	0.2368
GA-CKRVM [23]	433.53	20.82	0.1412	161.56	12.71	0.1616	62.24	7.76	0.2347
CNN-Bi-LSTM [16]	477.35	21.84	0.1396	227.11	15.07	0.1622	81.79	9.04	0.2600
SPGAPSO-CKRVM	392.43	19.81	0.1383	161.1	12.69	0.1589	41.09	6.41	0.2232



(a) MAPE of various prediction models



(b) RMSE of various prediction models

Figure 5. Experimental results of algorithm accuracy

The experiment of algorithm scalability is used to test whether it is possible to increase the algorithm efficiency by adding additional nodes. We calculate speedup to evaluate the effect of parallelization. Run SPGAPSO-CKRVM ten times based on a single node, double nodes, four nodes and eight

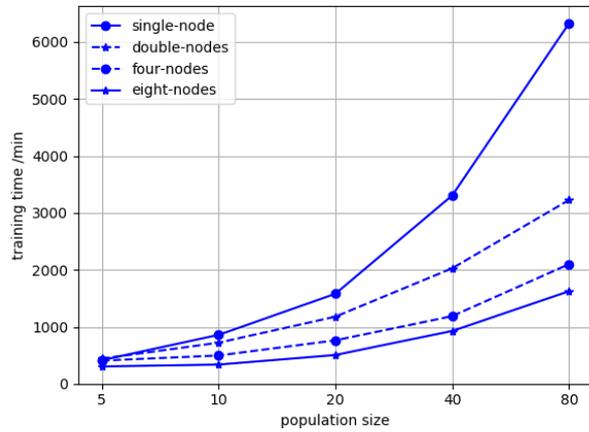
nodes respectively. Record the experimental results and calculate speedup of SPGAPSO-CKRVM. Speedup defined as follows:

$$S_n = \frac{T_1}{T_n} \quad (22)$$

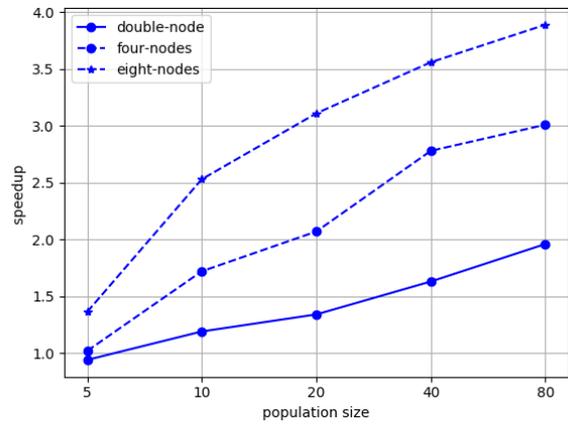
where, T_1 is sequential calculation time of model. T_n is parallel calculation time of model based on n nodes. Ideally, speedup is equal to the number of nodes. The experimental results are shown in Figure 6.

Population size determines the calculation of SPGAPSO-CKRVM. As the Figure 6a shows, the training time of SPGAPSO-CKRVM increases linearly with the calculation increasing gradually. The gap of training time of SPGAPSO-CKRVM based on different number of nodes is small when the calculation is little. As the calculation increasing, the training time of SPGAPSO-CKRVM based on eight-nodes is much lower than the training time of SPGAPSO-CKRVM based on four-nodes, double-nodes and single-node. The reason is that each calculation node is responsible for few calculations when the number of calculation nodes is large.

As the Figure 6b shows, the acceleration effect of the cluster is not obvious when the calculation is little. The reason is that the basic operations such as starting cluster, dividing tasks and allocating resources of the cluster are time-consuming. At this moment, the cluster has not achieved deserved effect. As the calculation increasing, the advantages of parallel calculation are becoming more and more obvious. The speedup is increasing and approaching gradually the ideal value. The experimental results verify that SPGAPSO-CKRVM proposed in this paper has good scalability.



(a) Training time of SPGAPSO-CKRVM with different number of nodes



(b) Speedup of SPGAPSO-CKRVM with different number of nodes

Figure 6. Experiment results of algorithm scalability

6. CONCLUSIONS

To construct a prediction model for traffic flow, RVM based on a combined kernel function and heuristic algorithms were employed. Parameter optimization algorithm of RVM was parallelized by Spark. SPGAPSO-CKRVM is proposed. The real data of Whitemud Drive in Canada were utilized to verify the prediction model. Experimental results show that the model called on SPGAPSO-CKRVM is superior to other methods in accuracy. In addition, SPGAPSO-CKRVM has less time consumption of parameter optimization than other models. Further research will include:

- Consider more factors affecting traffic flow such as average speed, lane occupancy rate and traffic flow on the adjacent roads.

- We use the original GA and PSO in this paper. For parameter optimization of RVM, most of heuristic algorithms have the problem that the convergence speed is too fast in early period of iterations, which leads to decrease of the population diversity in later period of iterations. In further research, we will try to combine RVM with complex heuristic algorithms such as Adaptive Genetic Algorithm (AGA) and Quantum Particle Swarm Algorithm (QPSO).

- Although the testing speed of RVM is extremely fast, the training speed is not ideal. We will use parallelization techniques to reduce training time of RVM.

- We will research the combination of RVM and deep learning algorithms. Deep learning algorithms such as DBN and CNN are used to extract traffic data features and RVM is used to predict traffic flow to construct a deep prediction model.

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