

MHD Powell–Eyring fluid flow with non-linear radiation and variable thermal conductivity over a permeable cylinder

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ABSTRACT

In this article, we have investigated the influence of magneto-hydro-dynamic (MHD) Powell–Eyring fluid flow in the presence of non-linear radiation, space dependent internal heat source and variable thermal conductivity over a permeable cylinder with suction/injection effects. We have considered Soret, Dufour and non-linear chemical reaction effect on heat and concentration equations. Using similarity transformation, the governing PDEs are changed into non-linear coupled ODEs and solved by R-K fourth order with shooting method. The impact of various parameters such as Powell- Eyring fluid parameters (K), Dufour parameter (Du), radiation parameter (R), small scale parameter (ϵ), Prandtl number (Pr), curvature parameter (γ), Schmidt number (Sc), chemical reaction parameter (Kn), Eckert number (Ec), relative temperature ratio parameter (θ_w), Soret parameter (Su), magnetic field parameter (M) and (A^*) and (B^*) are specific and temperature heat source on axial momentum, heat and concentration profiles have been analyzed graphically and skin friction coefficient, local Nusselt number and local Sherwood number can be discussed tabulated.

1. INTRODUCTION

Non-Newtonian fluids have greatest importance role in the theory of fluid mechanics. Fluids which shear stress and shear rate are non-linear called non-Newtonian fluid. Tooth paste, food oil, blood etc. are non-Newtonian fluids. The Powell-Eyring model, firstly in the phenomena of power-law model, it is assumed from kinematic theory of liquid rather than the experiential relation. Khan et al. [1] investigated MHD fluid flow with variable properties. Krishna et al. [2] studied unsteady Powell-Eyring fluid flow past an inclined stretching sheet. Mahanthesh et al. [3] examined unsteady 3-D MHD Eyring-Powell fluid past a convectively heated stretching sheet. Several researchers investigated (Akbar et al. [4], Javed et al [5], Hayat et al. [6-10] and Gaffar et al. [11]) 2D and 3D flow for MHD and radiative Powell-Eyring fluid towards a stretching sheet with various boundary condition.

Heat transfer phenomena has significant applications of plastic sheets, spinning of fibers, polymer, plasma studies, MHD power generator, petroleum industries, cooling of nuclear reactors, glass fiber production and paper production etc. Radiation effects may be important role in controlling heat transfer.

MHD (magneto-hydro-dynamic) is the study of the magnetic properties of electrically conducting fluids. Magneto-fluids include salt water or electrolytes, liquid metals and plasmas. Several researchers (Madhu et al. [12], Makinde [13], Jain et al. [14-18], Dasa et al. [19] and Chauhan et al. [20-22]) proposed heat transfer phenomena for the impact of various physical condition with various geometries and surface conditions.

Keeping all these specifics in mind, we intend to study the boundary layer flow and heat transfer of MHD Powell–Eyring fluid flow in the presence of non-linear radiation, space dependent internal heat source and variable thermal conductivity over a permeable cylinder with suction/injection effects. We have considered Soret, Dufour and non-linear chemical reaction effect on heat and concentration equations.

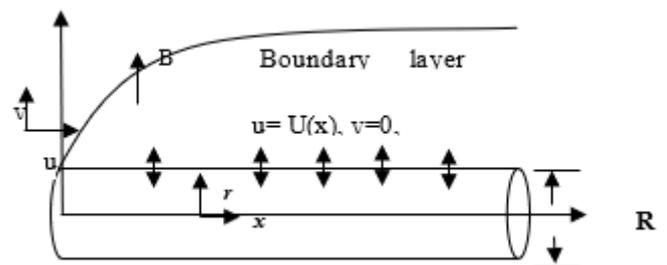


Figure 1. Physical diagram of the problem

2. MATHEMATICAL FORMULATION

2D boundary layer flow for Power-Eyring fluid over a permeable cylinder is considered. The axis of the cylinder is taken along the x axis and r is taken along radial direction. The coordinate system and flow regime is illustrated as exposed in the Figure 1. The Cauchy stress tensor in Power-Eyring fluid is given by

$$\tau_{ij} = \mu \frac{\partial u_i}{\partial x_j} + \frac{1}{\beta} \sinh^{-1} \left(\frac{1}{\gamma} \frac{\partial u_i}{\partial x_j} \right) \quad (1)$$

where μ : viscosity coefficient, β and γ : material fluid parameters. The governing equations can be written as Khan et.al [1].

$$\frac{\partial(ru)}{\partial x} + \frac{\partial(rv)}{\partial r} = 0 \quad (2)$$

$$u \frac{\partial u}{\partial x} + v \frac{\partial u}{\partial r} = U_e \frac{\partial U_e}{\partial x} + \left(v + \frac{1}{\rho\beta c} \right) \frac{\partial^2 u}{\partial r^2} - \frac{1}{2\rho\beta c^3} \left(\frac{\partial u}{\partial r} \right)^2 \frac{\partial^2 u}{\partial r^2} + \frac{1}{r} \left(v + \frac{1}{\rho\beta c} \right) \frac{\partial u}{\partial r} - \frac{1}{6r\rho\beta c^3} \left(\frac{\partial u}{\partial r} \right)^3 - \frac{\sigma B_0^2}{\rho} (u - U_e) \quad (3)$$

$$u \frac{\partial T}{\partial x} + v \frac{\partial T}{\partial r} = \frac{1}{r\rho C_p} \frac{\partial}{\partial r} \left(k(T)r \frac{\partial T}{\partial r} \right) - \frac{1}{\rho C_p} \left(\frac{\partial q_r}{\partial r} \right) + \bar{D} \left(\frac{\partial^2 C}{\partial r^2} + \frac{1}{r} \frac{\partial C}{\partial r} \right) + \frac{q'''}{\rho C_p} \quad (4)$$

$$u \frac{\partial C}{\partial x} + v \frac{\partial C}{\partial r} = D_m \left(\frac{\partial^2 C}{\partial r^2} + \frac{1}{r} \frac{\partial C}{\partial r} \right) + \bar{S} \left(\frac{\partial^2 T}{\partial r^2} + \frac{1}{r} \frac{\partial T}{\partial r} \right) - k_n (C - C_\infty)^n \quad (5)$$

The boundary conditions are

$$u(x, a) = U_w, \quad v(x, a) = -V_w, \quad T(x, a) = T_w = T_\infty + T_0 \frac{x}{l}, \quad (6)$$

$$C(x, a) = C_w = C_\infty + C_0 \frac{x}{l} \quad \text{at } r = a$$

$$u(x, a) \rightarrow U_e, \quad T(x, a) \rightarrow T_\infty, \quad C(x, a) \rightarrow C_\infty \quad \text{at } r \rightarrow \infty$$

$$\text{where } U_w = \frac{xU_0}{l}, \quad U_e = \frac{xU_\infty}{l},$$

Rosseland approximation can be considered, the radiative heat flux, q_r becomes (Ska et.al [23])

$$\frac{\partial q_r}{\partial y} = \frac{\partial}{\partial y} \left(\frac{-4\sigma}{3k^*} \frac{\partial T^4}{\partial y} \right)$$

σ : Stefan–Boltzmann constant: k^* absorption coefficient and the equation (4) become

$$u \frac{\partial T}{\partial x} + v \frac{\partial T}{\partial r} = \frac{1}{\rho C_p} \frac{\partial}{\partial r} \left(k(T)r \frac{\partial T}{\partial r} \right) + \bar{D} \left(\frac{\partial^2 C}{\partial r^2} + \frac{1}{r} \frac{\partial C}{\partial r} \right) + \frac{k_\infty U_w}{\rho C_p x v} [A^* f'(T_s - T_\infty) + B^*(T - T_\infty)] + \frac{1}{\rho C_p} \frac{16\sigma}{3k^*} \frac{\partial^2 T^4}{\partial y^2} \quad (7)$$

where t : time, C_p : Specific heat, $K(T) = k_\infty(1 + \varepsilon\theta)$: thermal conductivity depending of temperature (ref. [24]) ρ : fluid density, T : fluid temperature, C : fluid concentration.

The similarity transformations (Khan et.al [1]) as given below are introduced:

$$u = \frac{U_0 x}{l} f'(\eta), \quad v = -\frac{a}{r} \sqrt{\frac{\nu U_0}{l}} f(\eta), \quad \theta(\eta) = \frac{T - T_\infty}{T_s - T_\infty},$$

$$\eta = \frac{r^2 - a^2}{2a} \sqrt{\frac{U_0}{\nu l}} \quad \text{and} \quad \phi(\eta) = \frac{C - C_\infty}{C_s - C_\infty} \quad (8)$$

$$2(1+K)\gamma f'' - f'^2 + (1+K)(1+2\gamma\eta) f''' + A^2 + f f'' - \frac{4}{3} K \lambda_2 \gamma (1+2\gamma\eta) f'^3 - K \lambda_2 (1+2\gamma\eta)^2 f''' f'^2 - M(f' - A) = 0 \quad (9)$$

$$2(1+\varepsilon\theta)\gamma\theta' - \text{Pr}(\theta f' - f\theta') + (1+2\gamma\eta)(1+\varepsilon\theta)\theta'' + (1+2\gamma\eta)\varepsilon\theta'^2 + \frac{4R}{3}((\theta_w - 1)\theta + 1)^3 \gamma\theta' + A^* f' + B^* \theta + \frac{4R}{3}((\theta_w - 1)\theta + 1)^3 (1+2\gamma\eta)\theta'' + \text{Pr} Du (2\gamma\phi' + (1+2\gamma\eta)\phi'') + 4R(\theta_w - 1)((\theta_w - 1)\theta + 1)^2 (1+2\gamma\eta)\theta'^2 = 0 \quad (10)$$

$$\phi''(1+2\gamma\eta) + 2\phi'\gamma + Su Le((1+2\gamma\eta)\theta'' + \theta\gamma') - Le(f'\phi - f\phi') - Le K_n \phi^n = 0 \quad (11)$$

Boundary conditions are following as:

$$f = S, \quad f' = 1, \quad \theta = 1, \quad \phi = 1 \quad \text{at } \eta = 0 \\ f' \rightarrow A, \quad \theta \rightarrow 0, \quad \phi \rightarrow 0 \quad \text{at } \eta \rightarrow \infty \quad (12)$$

where prime denotes with respect to η , f : dimensionless stream function, θ : dimensionless temperature ϕ :

dimensionless concentration, $K = \frac{1}{\mu\beta\gamma}$: material fluid

parameters, $\lambda_2 = \frac{U_0^3 x^2}{2l^3 c^2 \nu}$: dimensionless fluid parameter,

$\gamma = \sqrt{\frac{\nu l}{U_0 a^2}}$: curvature parameter, $R = \frac{4\sigma T_\infty^3}{k^* k_\infty}$: radiation

parameter, $S = \frac{rV_w}{a} \sqrt{\frac{l}{\nu U_0}}$: suction /injection parameter,

$Du = \frac{\bar{D}}{\nu} \left(\frac{C_w - C_\infty}{T_w - T_\infty} \right)$: Dufour number, $Su = \frac{\bar{S}}{\nu} \left(\frac{T_w - T_\infty}{C_w - C_\infty} \right)$: Soret

number, k_∞ : thermal conductivity, ε : small scale parameter,

$\text{Pr} = \frac{\mu C_p}{k_\infty}$: Prandtl number, $\theta_w = \frac{T_w}{T_\infty}$: relative temperature

ratio parameter, $A = \frac{U_\infty}{U_0}$: ratio parameter, $M = \frac{\sigma B_0^2 l}{\rho U_0}$:

magnetic field parameter, $Le = \frac{\nu}{D_m}$: Lewis number,

$Kn = \frac{l k_n (C_s - C_\infty)^{n-1}}{U_0}$: chemical reaction parameter. T_w :

surface temperature of cylinder and T_∞ : ambient fluid temperature.

Skin friction coefficient, local Nusselt number and local Sherwood number can be defined as follows:

$$C_f = \frac{\tau_w}{\frac{1}{2}\rho(u_w)^2} \quad (13)$$

$$Cf Re_x^{1/2} = (1+K)f''(0) - K \frac{\beta}{3} [f'''(0)]^3$$

$$Nu = \frac{xq_w}{k(T_w - T_\infty)} \quad (14)$$

$$Nu Re_x^{-1/2} = -\left(1 + \frac{4}{3}R\right)\theta'(0)$$

$$Sh = \frac{xj_w}{D_B(C_w - C_\infty)} \quad (15)$$

$$Sh Re_x^{-1/2} = -\phi'(0)$$

where, $Re_x = \frac{xu_s}{\nu}$ is the local Reynolds number.

Table 1. Comparison table of $-f''(0)$ for different values M

Comparison of $-f''(0)$ for different values M in the absence of the parameters $S=A=K=\gamma=\lambda_2=0$					
M	Anders on et al. [25]	Prasad et al. [26]	Mukhopadhyay et al. [27]	Palani et al [28]	Present study
0.0	1.0000	1.0001	1.00017	1.0000	1.00000
0.5	1.2249	1.2247	1.22475	1.2247	1.22474
1	1.4140	1.4144	1.41445	1.4142	1.41421
1.5	1.5810	1.5811	1.58114	1.5811	1.58113
2	1.7320	1.7322	1.73220	1.7320	1.73205

Table 2. Comparison table of $-\theta'(0)$ for different values Pr

Pr	Comparison of $-\theta'(0)$ for different values Pr in the absence of the parameters $S=A=K=\gamma=\lambda_2=\varepsilon=R=Ec=Du=A^*=B^*=0, \theta_w=1$					
	Nadeem et al [30]	Khan et. al [31]	Golra et. al [31]	Wang [32]	Narayana et.al [29]	Present study
0.7	0.454	0.454	0.454	0.454	0.4539	0.4540
2.0	0.911	0.911	0.911	0.911	0.9114	0.9113

3. RESULTS AND DISCUSSION

In this paper, calculations were carried out for different values of the parameters. The following default parameter values are adopted for computation: $A=0.1, \lambda_2=0.1, n=1, S=0.5, K=0.1, Du=0.1, R=0.5, \varepsilon=0.1, Pr=1.5, \gamma=0.1, Le=5, Kn=0.1, \theta_w=1.5, Su=0.1, M=0.5, A^*=0.1, B^*=0.1$ have been analyzed on axial f', θ and ϕ profiles. Figures (2-4) show the behavior of M on f', θ and ϕ profiles. Indicates

that the dimensionless velocity f' is decreased and opposite behaviors show on θ and ϕ profiles as the value of M increases. Figures (5-7) represent the influence of K on f', θ and ϕ profiles. It is noticed that an increase in the value of K, f' increases and θ and ϕ profiles decrease. With increases in the value of A, f' profile increases whereas θ and ϕ profiles decrease, as shown in figures (8-10). Figures (11-13) show the f', θ and ϕ profiles against the similarity variable η for various values of γ . We observe from these figures that the f', θ and ϕ profiles increase as γ increases. Figures (14-15). An increase in the value of Pr is observed to decrease the θ and ϕ profiles. Prandtl number signifies the ratio between velocity diffusivity to energy diffusivity. Fluids with small value of Pr will possess large energy conductivities so that temperature can diffuse from the surface faster than for large value of Pr fluids. Figures (16-18) explain the effect of θ_w, R, ε on θ profile. It is observed that, θ profile increases for increasing the values of θ_w, R, ε . This is due to the fact that an increase in radiation parameter provides more heat to fluid that causes an enhancement in the heat and thermal boundary layer thickness. Figure (19) shows the impact of Du on θ profile. An increase in the value of Du is observed to increase the θ profile. It has been experimentally verified that the diffusion of energy is caused by a composition gradient. This fact is known as the Dufour effect. Figures (20-21) show the impact of Kn and Su on ϕ profile. Rising the value of Kn and Su are observed to enhance ϕ profile. Kn increases the rate of interfacial mass transfer. Kn reduces the local concentration, thus increases its concentration gradient and its flux. Figures (22-23) show the impact of Le and n on ϕ profile. An increase in the value of Le and n are observed to suppress ϕ profile. It is due to the fact that Le is the ratio of velocity to mass diffusivities which means that when Le increases, mass diffusivity decreases and there is a reduction in concentration. Figures (24-25) display the effect of A^* & B^* on θ profile. It is observed that, θ profile increases for increasing the values of A^* & B^* . Heat source parameters act like a heat producer, which gain the heat to the flow and enhances the temperature profiles. Table-1 Moreover, the present results for the skin friction coefficient $-f''(0)$ for different values of magnetic field parameter M in the absence of the parameters $S=A=K=\gamma=\lambda_2=0$ are compared with the available results of Anderson et al. [25], Prasad et al. [26], Mukhopadhyay et al. [27] and Palani et al [28]. . Table-2 Moreover, the present results for the Nusselt number $-\theta'(0)$ for different values Pr in the absence of the parameters $S=A=K=\gamma=\lambda_2=\varepsilon=R=Ec=Du=A^*=B^*=0, \theta_w=1$. Under some special conditions, present results have an excellent. Table-3 for various values of the physical parameters, Namely A, Du, K, R, ε , Pr, γ , Le, Kn, θ_w, M on $C_f Re_x^{-1/2}, Nu Re_x^{-1/2}$ and $Sh Re_x^{-1/2}$. From these tables, we noticed that with the increases in M, K, and γ parameter the value of $C_f Re_x^{-1/2}$ decreases whereas increases in the value of K $Nu Re_x^{-1/2}$ and $Sh Re_x^{-1/2}$ increases.

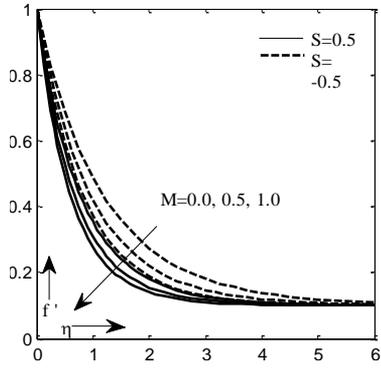


Figure 2. Impact of M on f'

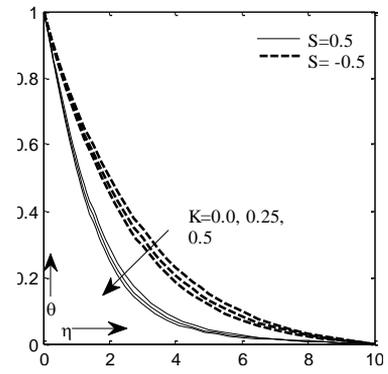


Figure.6 Impact of K on θ

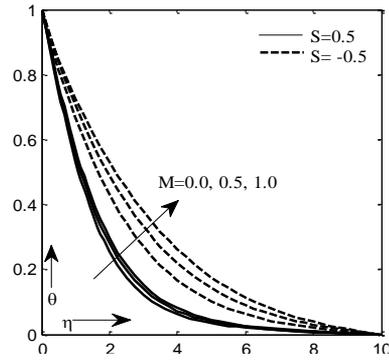


Figure 3. Impact of M on θ

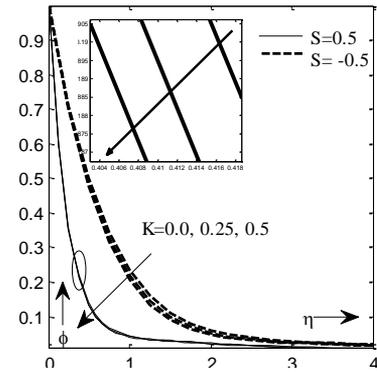


Figure 7. Impact of K on ϕ

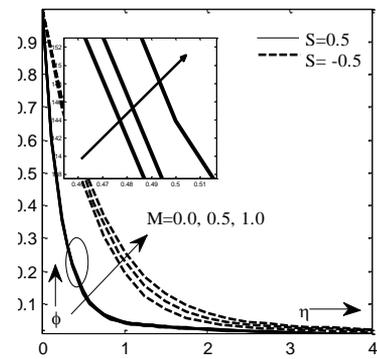


Figure 4. Impact of M on ϕ

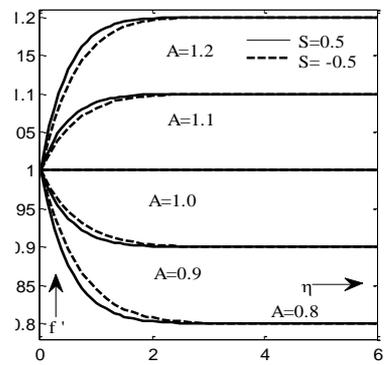


Figure 8. Impact of A on f'

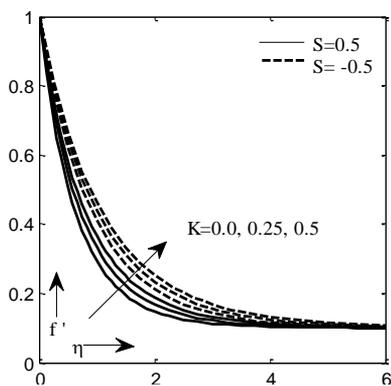


Figure 5. Impact of K on f'

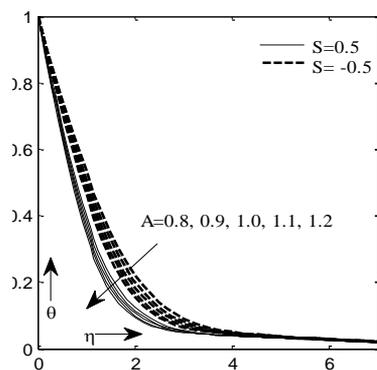


Figure 9. Impact of A on θ

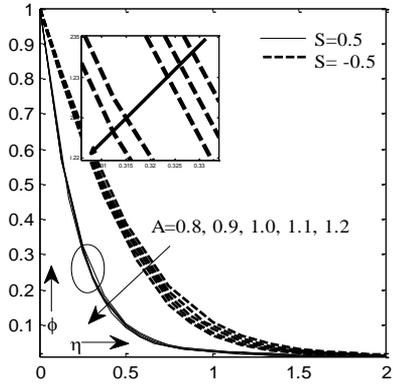


Figure 10. Impact of A on ϕ

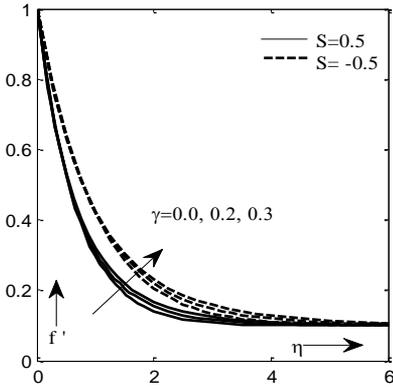


Figure 11. Impact of γ on f'

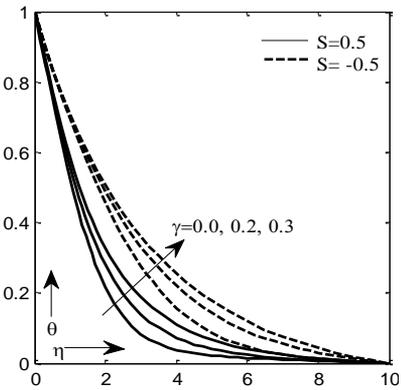


Figure 12. Impact of γ on θ

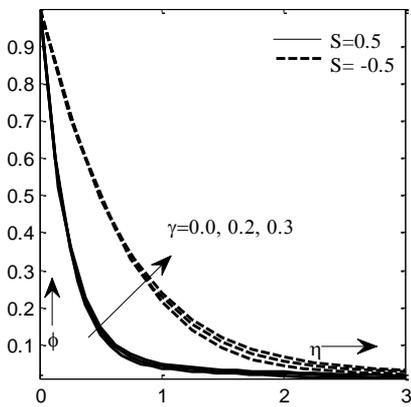


Figure 13. Impact of γ on ϕ

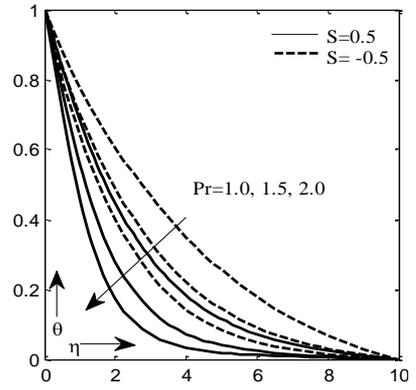


Figure 14. Impact of Pr on θ

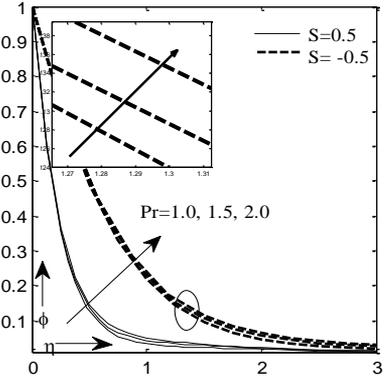


Figure 15. Impact of Pr on ϕ

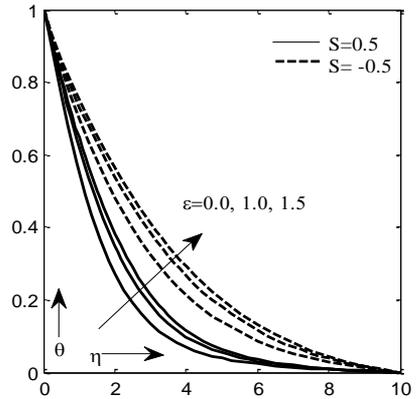


Figure 16. Impact of ϵ on θ

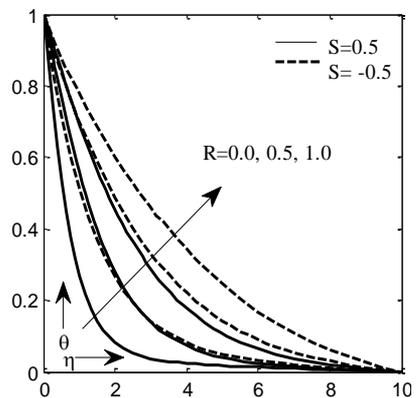


Figure 17. Impact of R on θ

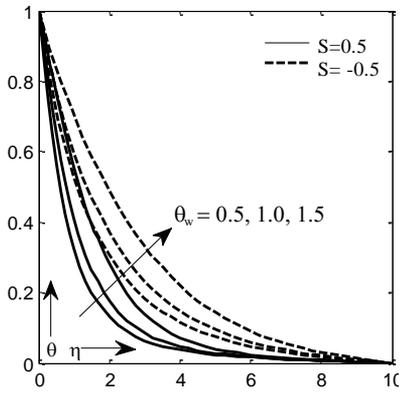


Figure 17. Impact of θ_w on θ

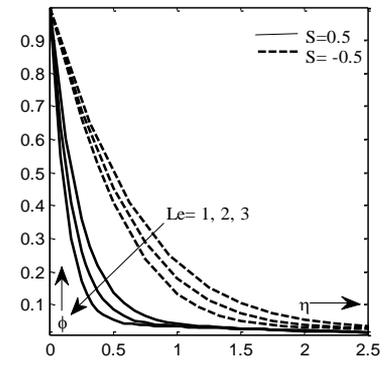


Figure 22. Impact of Le on ϕ

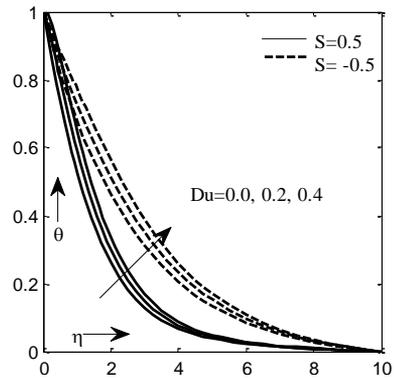


Figure 19. Impact of Du on θ

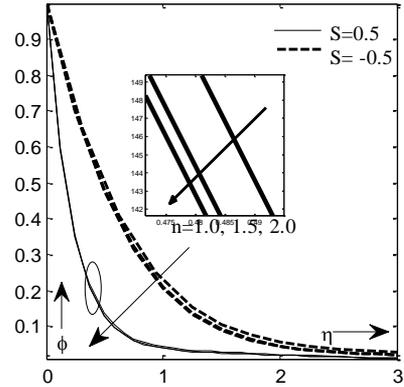


Figure 23. Impact of n on ϕ

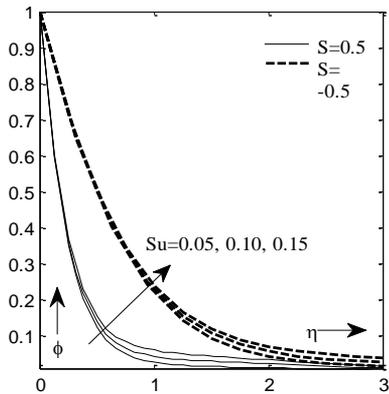


Figure 20. Impact of Su on ϕ

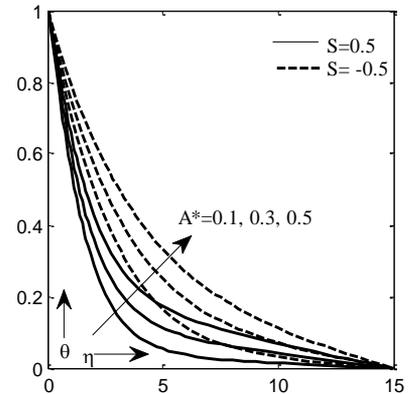


Figure 24. Impact of A^* on θ

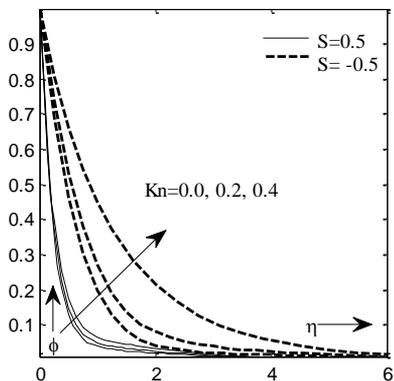


Figure 21. Impact of Kn on ϕ

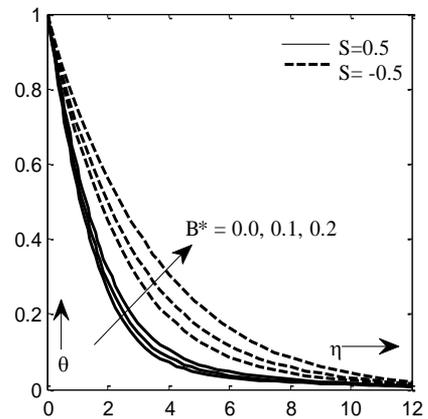


Figure 25. Impact of B^* on θ

Table-3

ε	M	K	γ	Le	Pr	R	θ_w	A	Du	Kn	$-C_f Re_x^{1/2}$	$Nu Re_x^{-1/2}$	$Sh Re_x^{-1/2}$
0											1.502219	0.760348	4.060689
1											1.502219	0.630711	4.079398
2											1.502219	0.544944	4.090668
0											1.305153	0.782987	4.099390
1											1.671311	0.714417	4.032911
2											1.958593	0.669742	3.983482
		0.00									1.444668	0.729452	4.048704
		0.25									1.584964	0.764166	4.081678
		0.50									1.714564	0.791543	4.106555
			0.0								1.462141	0.754909	4.048982
			0.2								1.541780	0.737558	4.078769
			0.3								1.580782	0.734518	4.096150
				1							1.502228	0.946534	1.220979
				2							1.502228	0.890381	2.035235
				3							1.502220	0.839389	2.752226
					1.0						1.502219	0.510620	4.095830
					1.5						1.502219	0.744390	4.063113
					2.0						1.502219	0.941818	4.033682
						0.0					1.502219	1.064623	3.859308
						0.5					1.502219	0.744390	4.063113
						1.0					1.502219	0.698245	4.097192
							0.5				1.502219	1.735235	3.857031
							1.0				1.502219	1.256816	3.962370
							1.5				1.502219	0.744390	4.063113
								0.8			0.413809	1.026136	4.294352
								1.0			0.000000	1.087361	4.359780
								1.2			0.451286	1.144335	4.424770
									0.0		1.502219	1.016664	3.997736
									0.2		1.502219	0.461815	4.131562
									0.4		1.502218	0.137283	4.278673
										0.0	1.502219	0.736785	4.168052
										0.2	1.502219	0.75252	3.950635
										0.4	1.502219	0.771101	3.692596

4. CONCLUSION

The present article includes the analysis of magneto-hydrodynamic (MHD) Powell–Eyring fluid flow in the presence of non-linear radiation, space dependent internal heat source and variable thermal conductivity over a permeable cylinder with suction/injection effects. We have considered Soret, Dufour and non-linear chemical reaction effect on heat and concentration equations. The effects of different physical key parameters such as magnetic parameter, suction parameter, thermal radiation parameter, and Prandtl number etc are plotted and discussed.

The conclusions of the present investigation are made as follows:

- a) The results show that as the M increases the f' to the fluid suppresses the whereas opposite behavior is found for θ and ϕ profiles.
- b) Increasing the value of K and A reduce the heat transfer coefficient between the cylinder surface and the fluid however, increasing following parameters, R, γ , A*, B*, Ec, M increases it.

- c) Increasing the value of K, A, Le, n suppress ϕ profile whereas increases the value of M, Kn, Su, Pr, γ enhances the ϕ profile.

- d) Increasing the value of M, K, and γ parameters, decreases the value of $C_f Re_x^{1/2}$

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NOMENCLATURE

K	material fluid parameters
R	radiation parameter
S	suction /injection parameter
Du	Dufour number
Su	Soret number
k_{∞}	thermal conductivity
Pr	Prandtl number
A	ratio parameter
M	magnetic field parameter
	Lewis number

Le chemical reaction
 Kn

Greek symbols

θ	Dimensionless temperature
ϕ	Dimensionless concentration.
λ	fluid parameter
γ	curvature parameter
ε	small scale parameter
θ_w	relative temperature ratio parameter