

## **CALCULATION MODEL FOR THERMO-MECHANICAL COUPLING AND 3D NUMERICAL SIMULATION FOR CONCRETE TOWER OF CABLE-STAYED BRIDGE**

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### **ABSTRACT**

Heat transfer theory for concrete tower of cable-stayed bridge will be the basis of the temperature field analysis using the finite element method analysis of the stress field of indirect coupling, accurate analysis of the internal structure of the transient temperature and stress field stacked Jiahousuota stress distribution. In real bridge, for example, solving the temperature stress on the tower, and demonstrated: Solving transient temperature field finite element method can accurately simulate the temperature distribution in Sarasota; the treatment temperature change methods - mechanical coupling problem, can temperature load and other effective combination of load stress field, resulting in accurate stress distribution in the structure.

**Keywords:** Temperature, Mechanical properties, Thermo-mechanical coupling, Cable-stayed bridge.

### **1. INTRODUCTION**

Due to poor heat conduction properties of concrete, its surroundings and solar radiation temperature changes and other factors, to the surface rapidly warming or cooling, heat transfer inside the concrete needs a long time to reach equilibrium, while the concrete structure surface continuous with the surrounding environment to carry out heat exchange, so the concrete structure temperature field and the temporal changes over time showed significant non-linear distribution. Nonlinear transient temperature distribution in the cross section of the field will produce not only displacement, stress and temperature constraints and a large temperature stress from restraint, which appear temperature and stress field coupling effect on the structural discontinuity lee.

Temperature has a great influence on the mechanical properties of concrete, temperature coupled stress fracture behavior occasion of concrete, mainly fracture toughness and fracture energy, attracting the attention of many researchers. Prokopski by testing analysis and comparison of changes in ordinary concrete and refractory concrete fracture toughness in the range of 20 °C -1100 °C, found two concrete fracture toughness are reduced with increasing temperature. Nielsen et al., Respectively, and Menou by experimental analysis of concrete-like material fracture energy, tensile strength and other parameters vary with temperature, that the rough fracture surface is the main cause of the fracture energy varies with temperature. But now a lot of research results were from tests.

### **2. CALCULATION MODEL FOR THERMO-MECHANICAL COUPLING**

As we all know, poor thermal conductivity is a disadvantage of concrete materials [1]~[11], temperature changes caused by solar radiation easily to the surface rapidly heating and cooling, concrete internal equilibrium heat transfer the basic needs of a very long period, while Concrete needs heat exchange with the environment, and therefore the temperature field in concrete structure over time and is nonlinear transient changes in distribution. - Section nonlinear transient temperature distribution will not only displaced, but also have a greater self-restraint stress and temperature temperature constraint stress, which appears temperature and stress field coupling effect on the force structure is extremely unfavorable. Temperature changes have a significant impact on its mechanical properties, temperature field and stress field coupling will accelerate cracked concrete, mainly in the fracture energy and fracture toughness. Prokopski [11]~[14]experimentally analyzed the changes in ordinary concrete and refractory concrete fracture toughness, fracture toughness were found to increase with increasing temperature but will decrease. Nielsen and Menou [15]~[20]and other binding assay analyzes the tensile strength and fracture energy of concrete with changes in temperature, they think rough fracture surface is the main cause of the fracture energy varies with temperature, is obtained according to the heat conduction equation node heat rate vector, and then introduced as a load stress field solving equations, formulas such as (1) as follows:

$$\{K\}\{U\} = \{F^R\} + \{F^A\} \quad (1)$$

$\{K\}$  stands for total stiffness matrix,  $\{U\}$  is nodal displacements matrix;  $\{F^R\}$  is reaction force vector.

$$\{F^A\} = \{F^{nd}\} + \{F^{ac}\} + \sum_{m=1}^N (\{F^{th}\} + \{F^{pr}\}). \quad (2)$$

$\{F^{nd}\}$  stands for the force on the node,  $\{F^{ac}\}$  is acceleration vector,  $\{F^{th}\}$  is thermal unit vector,  $\{F^{pr}\}$  is pressure unit vector.

$\{F_e^{th}\} = \int_{vol} [B]^T [D] \{\varepsilon\}^{th} d(vol)$ ,  $[B]$  stands for strain - displacement matrix,  $\{\varepsilon\}^{th}$  is thermal strain matrix,  $vol$  is volume [147]. When the heat conduction equation and the stress field of Combined Solution of achieving two field coupling process, we have tower temperature stress distribution.

### 3. CABLE-TEMPERATURE FIELD AND TEMPERATURE FIELD COUPLED STRESS CALCULATION

#### 3.1 temperature field calculation

Temperature field boundary conditions include external borders and internal boundaries, the former mainly by solar radiation, which is mainly radiant heat exchange, concrete pylon outside the boundary at any instant, the heat flow to follow the following equation

$$-\lambda \partial \theta / \partial n = q_s q_c q_l \quad (3)$$

In formula,  $q_s$  is solar radiation energy,  $q_s = a_s \bullet I$ ,  $a_s$  is blackness coefficient,  $q_c$  is convective heat exchange;  $q_l$  is radiation heat transfer,

$$q_l = \sigma e \left[ (T + 273)^4 - (T_a + 273)^4 \right],$$

$\sigma = 5.676 \times 10^{-8} \text{ W/m}^2 \text{ K}^4$ ,  $e$  is 0.88, Assume that radiation heat transfer coefficient

$$\beta_\gamma = \sigma e \left[ (T + 273)^2 + (T_a + 273)^2 \right] (T + T_a + 2 \times 273) \quad (4)$$

Then it can express

$$-\lambda \partial T / \partial n = -a_s I + \beta_c (T - T_a) + \beta_\gamma (T - T_a). \quad (5)$$

Hypothesis  $\beta = \beta_c \beta_\gamma$ , Combined heat conduction equation

$$T_a' = T_a + a_s I / \beta. \quad (6)$$

$I = I_a + I_d$ ,  $I_a$  is the intensity of the sun's radiation,  $I_d$  is scattering intensity.

Atmospheric temperature

$$T_a(t) = (T_{a\max} + T_{a\min}) / 2 + \sin[(t-9)\pi/12] (T_{a\max} - T_{a\min}) / 2$$

Formula to solve,  $T_{a\max}$ ,  $T_{a\min}$  is the maximum daily temperature and minimum daily temperatures. Temperature boundary conditions within the boundary of tower:

$$\lambda \partial T / \partial n + \beta_\gamma (T - T_a) + q_s = 0 \quad (7)$$

$\beta_\gamma (T - T_a)$  is convective heat exchange,  $T_a$  is inside temperature, The average of the measured values of available alternatives, can also be determined empirically. Therefore, the temperature inside the tower can be expressed by the following boundaries formula:

$$T_a' = T_a - q_s / \beta_c \quad (8)$$

$\beta_c$  Considers wind conditions, is  $5.7 \text{ W/m}^2 \text{C}$ ;  $q_s$  is radiation Heat Transfer. When radiation heat  $q_s$  transfer requires the solution of two surfaces in between tower demand angle factor  $F_{ij}$ . The calculation method may be hidden.

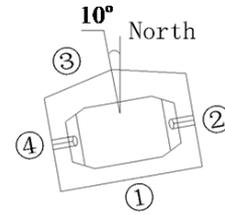


Figure 1. Orientation of tower

Bradenton is located orientation pylon four faces at different times of the day different sunshine effect shown in Figure.1. Morning (1) (2) two side subject to solar radiation, mainly as heating (2) surface; afternoon (3) (4) affected both sides of the sun, (4) surface influenced by solar radiation. Figure.2 for the tower at 13:00 am the temperature field contours.

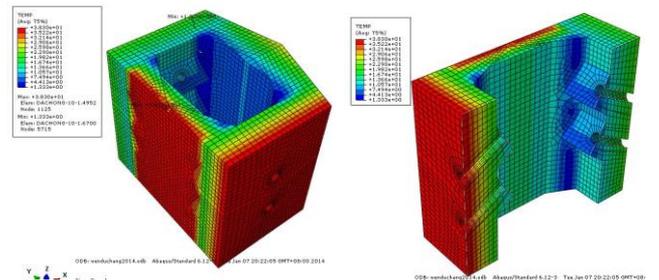


Figure 2. Temperature distribution

#### 3.2 Temperature stress calculation

Without considering the impact of stress singularity at constant normal stress loads (dead weight+cable force) around the hole Sarasota X direction is 1.537Mpa, positive

stress Y direction is 1.14Mpa, the normal stress X direction is 1.02Mpa .

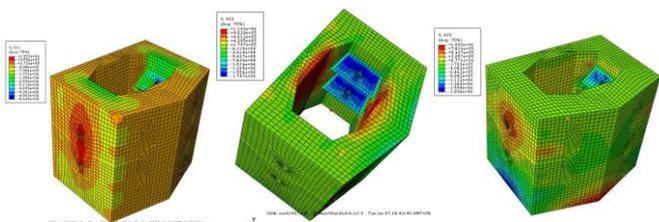


Figure 3. Stress contours

In order to accurately calculate the temperature - stress field coupling, the calculated transient temperature distribution along the tower wall thickness distribution of the maximum temperature difference of temperature distribution and empirical formulas were used as temperature load is coupled to the solid model to solve the stress distribution in the temperature stress calculation, obtained by calculating the maximum temperature stress and dead loads (gravity loads and cable tension) is a linear superposition of the stress field, to get the actual structure of the stress distribution, as shown in Figure.3 ~ Figure.6 . Then superimposed with constant load on the pylon maximum transverse tensile stress is 2.038MPa.

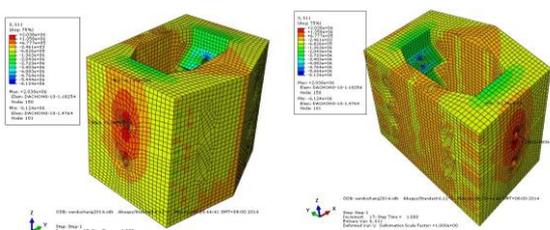


Figure 4. X direction normal stress

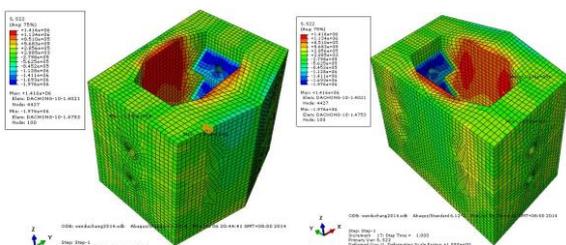


Figure 5. Y direction normal stress

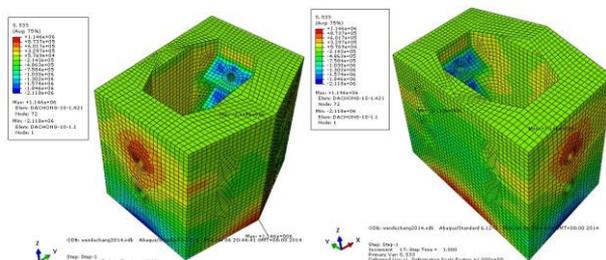


Figure 6. Z direction normal stress

From the above analysis we can get this conclusion:

1. according to the distribution of temperature stress Tower, using the transient temperature field - coupled stress to

analyze the stress distribution under the tower of the stress state capable of precise reaction tower in a real environment subject to various loads structures.

2. through heat conduction equation, combined with Abaqus temperature distribution structure to analyze, calculate numerical example can be seen in comparison with the experimental results using thermal conductivity - Transient effects of temperature and the temperature difference between the results of the finite element method coupling calculation can be a true reflection of Bradenton.

#### 4. CONCLUSIONS

This chapter introduces the overall form structure support projects in Guangxi big red bridge, by Madis Civil calculate the maximum cable tension cable-stayed bridge in various combinations during the operational phase, and then combined with ABAQUS and FRANC3D tower segments were local Finite element analysis of crack propagation and calculates the relationship between the stress intensity factor and the tower surface fractal dimension and load between the final analysis Sarasota temperature field - mechanical properties under stress field coupling tower, the main conclusions are as follows:

1. Fractal theory using the finite element means under conditions different levels of load calculation and analysis of the pylon, finite element results tables around the outside of the cable guide hole tower prone to tensile stress concentration phenomenon and led to cracks, damage and failure Bradenton It is actually a process of increasing dimension, the fractal dimension of the larger tower higher level of security, the higher the risk, so you can use the fractal dimension theory carve tall tower of safety evaluation.

2. According to the distribution tower temperature stress using transient temperature field - coupled stress analysis stress method tower, the stress distribution under a reaction tower capable of accurately in a real environment by various load structure; and by heat conduction equation, combined with Abaqus temperature distribution structure is analyzed, for example, calculated and measured results can be seen as relatively thermal conductivity - coupling calculation results of FEM can be a true reflection of the Tower of transient temperature field and the temperature difference between the effects.

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