A DEVIATION FROM STANDARD QUALITY APPROACH FOR CHARACTERISATION OF SURFACE WATER QUALITY

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ABSTRACT

Classification of water bodies into various classes of water use is a multi-criteria decision-making problem. Water Quality Index (WQI) and Analytic Hierarchy Process (AHP) were successfully used to assess overall water quality, but are not able to evaluate level of acceptability of water for specific use. Our objective is to develop a method of water quality assessment to evaluate the level of acceptability of a water body for specific use and to provide degree of potential effect of individual parameter on its overall quality. Here, AHP was modified and used to rank water bodies based on their quality. Modified AHP gave acceptable ranking of water bodies; but it failed to identify the reasons for what a waterbody got its corresponding rank. Therefore, a new approach of water quality assessment, named 'Deviation from Standard Quality (DSQ)' was developed. Calculation of positive or negative deviation from the desired threshold of water quality parameters is the key method of this approach. It denotes whether water could be used directly for the desired purpose or for which parameters and to what extent purification is required. We found inclusion or exclusion of any parameter had low sensitivity in evaluating ranking of the waterbodies by the DSQ method. This method was statistically validated. Empirical validation was done considering the field data obtained from Saraswati sub-watershed, Hugli, West Bengal, Keywords: alternative, analytic hierarchy process, deviation, index, parameter, water quality, waterbody, wateruse.

1 INTRODUCTION

Assessment of existing water quality is the first step of wise use of waterbodies; determination of the designated use based on the result of water quality assessment is the next step. Designated use of a waterbody should be the highest attainable use and should consider social demand for its existing or desired use. If the existing or desired use is not attainable as per the authorized standards, immediate restoration is needed. Therefore, determination of the level of acceptability of a waterbody for a specific use is required.

Since 1960s, Water Quality Index (WQI) served as an important tool in water quality assessment [1–3]. The first attempt to categorise water according to its degree of purity was made by Horton [4] and a general WQI was proposed by Brown *et al.* [5]. Thereafter, a number of water quality indices (WQIs) were developed worldwide [6–9]. Review of different WQIs was carried out by various authors [2, 3, 10, 11]. Most of the attempts in developing WQIs took the approach of expert opinion that included a subjective constant [12, 13]. Many researchers took initiatives to develop WQIs with objective approach, like statistical indices those are not considered personal opinions regarding comparative weights of different parameters to be analysed [14–16]. The statistical methods developed till today had some other limitations. The 'objective water quality index' proposed by Harkins [14] was not suitable for



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determining potential pollution in water. Stoner [17] attempted to prepare water quality indices for two specific uses: public water supply and irrigation, but failed to provide information on distribution and concentration of each parameter and the degree of treatment required for remedial measures.

Use of AHP, a widely used approach in multi-criteria decision making proposed by Saaty [18] came up as an alternative way to reduce subjectivity and increase conciseness in water quality assessment [19–21]. Karbassi *et al.* [22] used AHP to determine weights of different parameters of water quality. The authors [23–25] applied AHP in natural resources allocation and evaluation of environmental impacts. In lieu of AHP, some authors [16, 26–29] used fuzzy AHP that could deal with vague data set in the process of decision making.

Thus, WQI and analytic hierarchy process (AHP) were successfully used to assess overall quality of water, but were not capable enough of evaluating water quality for specific use. Our objective of this study is to develop a method of water quality assessment that is able to evaluate level of acceptability of a waterbody for specific use and provide degree of potential effect of individual parameter on its overall quality.

2 MATERIALS AND METHODS

2.1 Study area

The study area selected was the sub-watershed of Saraswati river basin that lied within the domain of Chandannagar and Srirampore sub-division of Hugli district, West Bengal (Fig. 1). Historically, the river Saraswati had a great importance on the economy of this region [30]. However, the present channel of Saraswati lies low as a dead river. The DVC (Damodar Valley Corporation) canal that is flowing from north-west to east of the study area has been serving as the main life-line for agricultural and domestic activities in rural areas, apart from groundwater use. Existence of both urbanized settlements with high population density, some medium scale industries (at the eastern part) and rural settlements with medium population density, extensive agriculture, orchards farming (at the western part) side-by-side give the unique characteristics to the study area.

2.2 Selection of parameters and Collection of water samples

Two issues were considered for the selection of parameters; first, the targeted specific uses of water: water that could be consumed directly, i.e. potable water (class P) and water that could only be consumed after conventional treatment followed by disinfection, i.e. non-potable water (class NP); secondly, available instruments or laboratory equipment to measure the parameters. Method of stratified purposeful sampling was followed for the selection of sample sites. A total of 22 samples from all kinds of water bodies present in the area were collected in sterile bottles on May, 2014. They were tested for the selected 15 parameters. Six of them were measured in situ using digital oxygen meter for measuring dissolve Oxygen (DO) and temperature and OAKTON multi-parameter tester-35 to measure temperature, pH, electric conductivity (EC), Total dissolved solids (TDS) and salinity. The other nine parameters viz. turbidity, fluoride, ammonia, residual chlorine, nitrate, iron, total hardness, chlorides, and phosphorous were tested in laboratory using Jal-TARA water testing kit. All experiments were completed within 48 hours of collection. The locations of the water sample

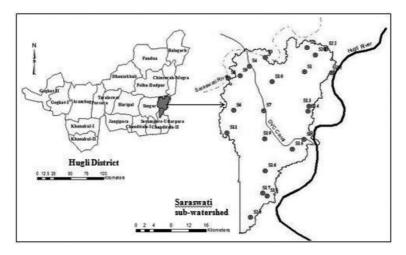


Figure 1: Location map of the study area.

sites with its corresponding coordinates collected on-site with the help of hand-held GPS. The base map of the study area was derived by overlying the vector of Saraswati sub-water-shed that was delineated in Soil and Water Assessment Tool (SWAT) using SRTM-DEM over raster image of Arc-Globe online, Fig. 1.

2.3 Water quality assessment using modified analytic hierarchy process

AHP is an objective mathematics that can process the subjective and personal preferences of an individual or group in the process of multi-criteria decision making [31, 32]. Use of AHP in water quality assessment is helpful because it can derive relative priorities of (n) number of alternatives for several criteria having different types of scales [33] and does not need a complete database [34].

Here, AHP was modified to exclude weight factor and used to get relative ranking of waterbodies based on their water quality. A theoretical clarification denoting the modifications are discussed herein after.

2.3.1 Developing a complete hierarchy

When each level of a hierarchy is connected to all elements in the next higher level, it is defined as a complete hierarchy [18, 31]. For our study, a complete hierarchy for priorities of water samples was developed (Fig. 2). The first hierarchy level had a single criterion, i.e. class NP. The second hierarchy level had seven sub-criteria: DO, pH, TDS, fluoride, nitrate, iron and chloride (Table 1.) Usually, their priorities were estimated from a pair-wise comparison matrix with respect to the criteria of the first level; but here, we assumed that they have equal priority for class NP. We did it intentionally for two reasons. Firstly, we choose those parameters that had already selected as important criteria for class C designated use by Central Pollution Control Board, India (Table 1) and secondly, to make the whole process free from the main disadvantage of AHP technique: 'dependency on expert knowledge' [34]. The collected water samples were placed as alternatives in the third level of hierarchy. Their priorities according to their relative goodness for each sub-criterion were derived from pair-wise comparison matrix to obtain the overall priorities in the final step.

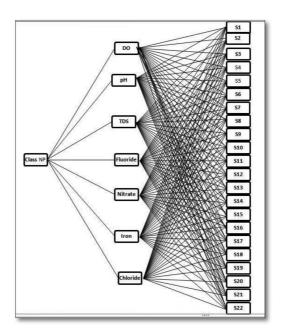


Figure 2: The complete hierarchy of AHP for priorities of water samples.

Table 1: Desirable limits of parameters for Class P and Class NP use of water.

Parameters	Class P*	Class NP*	
Temp. (°C)	N.M.*	N.M.	
DO (mg/l), min	6	4	
pH	6.5-8.5 NO Relaxation	6.5-9.0	
EC (µS), micromhos/cm, max	300	N.M.	
TDS (ppm) mg/l, max	500-2,000	1,500	
Salinity (ppm)	N.M.	N.M.	
Turbidity (NTU)	5 to 10	N.M.	
Fluoride, as F (mg/l), max	1.0-1.5	1.5	
Ammonia (mg/l), max	0.5-No Relaxation	N.M.	
Residual Chlorine (mg/l) min	0.2-1.0	N.M.	
Nitrate, as NO ₃ (mg/l), max	45 -No Relaxation	50	
Iron, as Fe (mg/l), max	0.3-No Relaxation	0.5	
Total Hardness as CaCo ₃ (mg/l), max	300-600	N.M.	
Chlorides, as Cu (mg/l), max	250-1,000	600	
Phosphorous (mg/l)	N.M.	N.M.	

Source: drinking water standards of BIS and Central Pollution Control Board, India

^{*}Note: NM= Not Mentioned, Class P= Potable water use, Class NP= Non-potable water use

2.3.2 Making clusters and selecting pivots

When alternatives are greater than 15, it is recommended to use clusters and pivots in pairwise comparison [18, 35]. Here, the number of alternatives was 22. All alternatives were sub-divided into three or four clusters for each criterion. In each cluster, one common alternative was selected as the pivot.

2.3.3 Preparing the guiding scores and scale of comparison

AHP has three modes of scale for ranking the alternatives: relative, absolute and benchmarking [18, 33]. For water quality analysis, suitable mode is 'absolute' [32, 33]. Following the fundamental scale of absolute numbers proposed by Saaty [35], the sets of guiding rules were prepared (Table 2). Here, modification was done for the definitions of absolute numbers

Table 2: Parameters, intensity of difference in values and sets of guiding scores.

Parameters/ Sub-criteria	Intensity of Difference	Score	Parameters/ Sub-criteria	Intensity of Difference	Score
Dissolve Oxygen (mg/l), min	≤ 0.2	2	Fluoride, as F (mg/l), max	≤ 0.4	3
	>0.2-0.5	3		>0.4-0.8	5
	>0.5-1.0	4		>0.8-1.2	7
	>1.0-1.5	5		>1.2	9
	>1.5-2.5	6	Nitrate, as NO ₃	≤ 2.5	2
	>2.5–3.5	7	(mg/l), max	>2.5–5	3
	>3.5-4.5	8		>5-10	4
	>4.5	9		>10-20	5
pН	≤ 0.15	2		>20-30	6
	>0.15-0.45	3		>30-40	7
	>0.45-0.85	4		>40-50	8
	>0.85-1.15	5		>50	9
	>1.15–1.45	6	Iron, as Fe (mg/l), max	≤ 0.2	3
	>1.45–1.75	7		>0.2-0.8	5
	>1.75-2.0	8		>0.8-1.5	7
	>2.0	9		>1.5	9
Total Dissolve Solids (ppm) mg/l, max	≤ 15	2	Chlorides, as Cu (mg/l), max	≤ 10	2
	>15-30	3		>10-20	3
	>30-45	4		>20-30	4
	>45-60	5		>30-40	5
	>60-75	6		>40-50	6
	>75–90	7		>50-60	7
	>90–105	8		>60-70	8
	>105	9		>70	9

Score	Definition	Explanation
1	Equal	Two alternatives are of same quality
3	Slightly better	One is slightly better than other
5	Better	One is better than other
7	Much better	One is much better than other
9	much more better	One is much more better than other
2,4,6,8	Intermediate values	

Table 3: The fundamental scale of absolute number modified after Saaty, TL.

Source: (Saaty, 2004)

mentioned in Saaty's nine points scale (Table 3). It would help consistent judgements in preparing the comparison matrix for each parameter.

2.3.4 Construction of the pair-wise comparison matrices

Here, a total of 25 matrices were developed. Numerical differences between two consecutive alternatives were estimated and decision was made according to the scales of intensity of difference, individually for each matrix of a sub-criterion, Tables 2 and 3.

2.3.5 Synthesized judgement, checking consistency, aggregation of clusters

Standardized matrix was prepared dividing each cell of the original comparison matrix by its corresponding column sum and mean of each row that represented relative weights of the alternatives was calculated. The Eigen Value Method was used to calculate the Principal Eigen value and eigen value of each alternative was calculated dividing the element of priority vector by weight vector. Matrix multiplication was performed; it gave priority vector for each cluster. Then, primary priorities were calculated for each alternative of a cluster. For cluster1, the primary priorities of all alternatives were directly considered as their overall priority. Primary priorities of cluster2 were linked up with cluster1 by multiplying them with the ratio of the priorities of the pivot in cluster1 and cluster2. Thus, overall priorities were calculated for (n) number of clusters.

2.3.6 Estimation of final rankings

The set of overall priority of each sub-criterion was considered as their local priority. "The historical AHP approach adopts an additive aggregation with normalization of the sum of local priorities to unity: $\mathbf{p}_i = \sum_j wj.lij$. Where, $\mathbf{p}_i = \mathrm{global}$ priority of the alternative i, $\mathbf{l}_{ij} = \mathrm{local}$ priority, $\mathbf{w}_j = \mathrm{weight}$ of the criterion j" [36, 37]. But here, we assumed that every sub-criterion had similar importance in maintaining quality for a specific use of water. Therefore, in this case, $\mathbf{w}_i = 1$; so, $\mathbf{p}_i = \sum lij$. The local priorities of each sub-criterion were simply added to estimate global priorities of the alternatives and they ranked in decreasing order.

2.4 Water quality assessment for specific water use: an alternative approach

In order to reach our objectives, a new approach of water quality assessment, named as 'Deviation from Standard Quality (DSQ)' was developed. Calculation of positive or negative deviation from the desired threshold of water quality parameter is the key method of this

approach. Considering the reverse nature of some parameters, two separate formulae, eqns (1) and (2), were prepared which are given below:

For the parameters where larger value represents worse condition and vice-versa:

$$Q_i = (X_d - X_i) / (X_{max} - X_{min})$$
 (1)

For the parameters where larger value represents better condition and vice-versa:

$$Q_i = (X_i - X_d) / (X_{max} - X_{min})$$
 (2)

Where, X_d is the desirable standard value for a particular parameter, X_i is the observed value of that parameter, X_{max} and X_{min} are the maximum and minimum observed value, respectively.

This approach deals with a bi-polar scale of acceptability. The composite deviation of zero represents the threshold for acceptability of a water sample for a particular purpose of use; positive increase of composite deviation denotes better condition and acceptability increases while negative increase indicates worse condition and degree of non-acceptability increases. Composite deviation of a particular water sample was calculated by summing up the deviations of all parameters selected for assessing water quality for a particular class of water use and it was used to get the final rankings of waterbodies as well as to evaluate acceptability for that specific use.

In this study, to assess water quality with DSQ method for class P 12 parameters, i.e. DO, pH, EC, TDS, turbidity, fluoride, iron, residual chlorine, total hardness, chlorides, nitrate, ammonia and for class NP seven parameters, i.e. DO, pH, TDS, fluoride, iron, nitrate, and chlorides were selected, Table 1. equation (2) was used to calculate deviations from desired limits in case of DO, pH and residual chlorine while for other parameters eqn. (1) was used.

3 RESULTS AND DISCUSSION

From literatures [38, 39], it was cleared that AHP had been accepted as a standard method in multi-criteria decision-making process, worldwide. Consistency index developed for each normalized matrix was checked with its corresponding consistency ratio, and it was observed that all matrices were consistent in judgements. Therefore, the set of priorities with respect to their superiority in quality derived through modified AHP could be used to rank the alternatives. Here, output of modified AHP supported our field experiences also. We found river Saraswati in water logged condition; water hyacinth grew extensively. It lost its identity as river to local people and was used as a wastewater disposal channel. The water samples, S3 and S5, collected from river Saraswati got the lowest rank 22nd and 20th, respectively (Table 4). The water sample S19, which was from a road-side waterbody linked to industrial wastewater channel got 21st rank, Table 4. These three water samples (S3, S5 and S19) got same ranks as above through DSQ method for class P and class NP, Table 4, both. For statistical verification, spearman's rank-order correlation was calculated and a very high degree of association (0.87) was found between the two sets of ranking resulting from modified AHP and DSQ method.

Quantitative information of global priority resulted from modified AHP could not evaluate the level of acceptability of waterbody for a specific use. Beside, local priority could not exhibit potential effect of a parameter on overall water quality. Whereas by the DSQ method, quantitative deviation of a parameter gave the reasons for what a waterbody got its corresponding rank and which parameters, to what extent needed purifying treatment. In assessing water quality for class P by the DSQ method, we found 18 samples had composite deviation greater than zero (Fig. 3). Among them, S12 had the maximum positive composite deviation (3.332),

Table 4: Relative rank of water samples by modified AHP and DSQ method.

		Modified AHP_class NP		DSQ_class P		DSQ_class NP	
Alternative	Source	Global Priority	Rank	Composite Deviation	Rank	Composite Deviation	Rank
S1	Pond	2.397	11	1.374	15	6.43	8
S2	Pond	0.784	19	1.184	16	5.568	18
S3	Saraswati River	0.037	22	-3.681	22	1.402	22
S4	Canal	5.54	3	3.033	3	7.152	2
S5	Saraswati River	0.578	20	-0.582	21	4.799	20
S6	Pond	2.044	14	1.618	10	6.486	7
S7	Canal	2.678	10	2.251	6	6.128	11
S8	Canal	6.923	1	0.708	18	6.524	6
S9	Tube well	2.16	12	2.126	7	6.062	15
S10	Tube well	3.148	7	2.021	8	6.106	12
S11	Tube well	1.448	18	1.39	14	5.601	17
S12	Tap water	5.511	4	3.332	1	7.185	1
S13	Tube well	1.597	17	-0.144	19	5.101	19
S14	Tap water	2.963	8	2.544	5	6.566	5
S15	Tube well	5.927	2	3	4	6.652	4
S16	Tap water	4.286	5	3.282	2	6.984	3
S17	Tap water	1.722	16	1.423	13	6.104	14
S18	Tube well	2.101	13	1.517	12	5.848	16
S19	Road-side waterbody	0.572	21	-0.321	20	4.316	21
S20	Tube well	2.011	15	1.645	9	6.192	9
S21	Tap water	2.703	9	1.592	11	6.105	13
S22	Well	4.03	6	0.9	17	6.135	10

^{*}Note: Class P= Potable water use, Class NP= Non-potable water use

ranked first and acceptable for class P use, but needed purification treatments specifically for the three parameters, i.e. EC (-0.023), ammonia (-0.2) and residual chlorine (-0.25) that had negative deviation. Remaining four samples had negative composite deviation and therefore not acceptable for class P. The sample S3 had the highest negative composite deviation

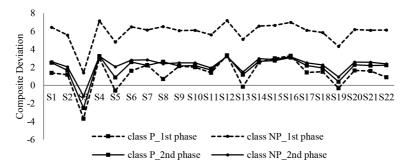


Figure 3 Composite deviation of water samples from the desired threshold of acceptability for Class P and NP in 1st and 2nd phase of analysis.

(-3.681), and ranked the lowest, i.e. 22nd. It had nine parameters with negative deviation; among them ammonia (-1) had the maximum negative deviation followed by EC (-0.988), iron (-0.947), turbidity (-0.7), TDS (-0.605), DO (-0.563), fluoride (-0.556), total hardness (-0.484) and nitrate (-0.438). This information would help in remedial measures.

A second phase of analysis was carried out to refine the result of first phase analysis as well as to check the sensitivity of the DSQ method to a parameter. In case of pH and chloride, no obtained value ever crossed the determined threshold of class P and class NP. So pH and chloride were excluded in the second phase of analysis and composite deviations were recalculated. This time, only nine samples could cross the threshold of acceptability for class P (Fig. 3). In case of class NP, during the first phase of analysis, all samples had composite deviation above zero (Fig. 3). Two samples, S3 and S19 which got the lower most rank in the first phase of analysis, got negative composite deviation in second phase of analysis (Fig. 3). The findings would help in prioritizing the process of quality management over a targeted region.

Spearman's rank-order correlation was calculated between the two sets of rankings in first and second phase of analysis. The Rho values for class P (0.9819) and class NP (0.9537) indicated a very good association between the two sets of ranking. It signified that inclusion or exclusion of any parameter has very low sensitivity on estimation of overall ranking by the DSQ method. Overall, class P needs better quality of water than class NP. The result of the DSQ method in both first and second phase of analysis revealed that all samples had lower degree of acceptability for class P use than class NP use of water (Fig. 3).

4 CONCLUSION

This article proposed modification in the AHP technique and a new approach entitled DSQ method to assess water quality for specific water use. Modified AHP differs from AHP by excluding subjective constant and suggesting the sets of guiding for consistent judgements in developing comparison matrix. Application of AHP in the final assessment of water quality is rare approach. It only gave rankings of water samples without providing significant information on role of individual parameter on overall quality and not suitable for assessing quality for specific water use. While the DSQ method is an objective technique, flexible to set desired standard for n number of parameters and therefore applicable for water quality assessment for specific use. It provides level of acceptance of a waterbody for its desired use and quantitative information on the status of individual parameter incorporated for qualitative assessment. This study suggested that the DSQ method can be used not only for water quality assessment for specific use but also can be applied for other types of pollution assessment,

such as, air pollution. In future, experimental application of the DSQ method in qualitative assessment of various natural resources over different spatial units would establish this method as a suitable alternative tool for pollution assessment.

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