



Enhancing the Efficiency of Finned Photovoltaic Thermal Collectors Using Al_2O_3 , CuO , and TiO_2 Nano-Fluids: A Comprehensive Study on Thermal and Electrical Performance Optimization

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ABSTRACT

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Energy has been essential in economic and human development worldwide over the past few decades. However, using conventional energy, especially from fossil fuels, has led to negative impacts such as air pollution, climate change, and dependence on non-renewable energy sources. Indonesia's position along the equator offers significant potential for harnessing solar energy. However, the electrical performance of photovoltaic (PV) panels tends to decline as their operating temperature rises. To address this, photovoltaic thermal collectors (PV/T), thermal collectors placed beneath the panels' surface, are employed to lower the PVs' operating temperature. This approach aims to enhance the cooling and overall efficiency of solar cells. This research will study the cooling of PV panels using nano-fluid with variations of Al_2O_3 , CuO , and TiO_2 . The findings indicate that varying the type of nanofluid can enhance the heat transfer rate within the photovoltaic thermal collector (PV/T) system. The thermal efficiencies recorded for the PV/T system using Al_2O_3 , CuO , and TiO_2 as coolants were 69.71%, 73.11%, and 71.75%, respectively. Correspondingly, the electrical efficiencies achieved were 10.12%, 13.26%, and 12.17%. From this study, it can be seen that CuO nano-fluid has a better cooling configuration than others.

1. INTRODUCTION

The rapid growth and advancement of the modern population have driven an increased demand for energy worldwide [1]. Currently, fossil fuels such as coal and petroleum, which are non-renewable and harmful to the environment, account for approximately 80% of the global energy supply [2]. By 2030, global energy demand will increase by 1.5% annually [3]. In 2019, fossil fuels accounted for 42% of Indonesia's final energy consumption. Due to this increasing demand, fossil energy supplies are decreasing [4]. To meet this increasing energy demand, efforts can be made to replace non-renewable energy with renewable energy [5]. Solar energy is a promising renewable resource with great potential for development, as it is accessible nationwide and available daily [6]. Solar energy is environmentally friendly because it does not produce air pollution and remains available as long as there is life [7]. Among the existing technologies, PV panels are the right technology for solar energy utilization. Indonesia has a lot of potential for renewable energy, especially solar energy, because it has an average radiation intensity of $4.8 \text{ kW/m}^2/\text{day}$ [8, 9]. Although solar energy is emitted in the form of radiation, not all of it reaches the Earth's surface [10]. The energy emitted is heat and light, and the PV

panel captures solar energy and converts it into electrical power and heat [11].

The advancement of technology, solar cells have developed into three generations, namely the first generation of solar cells made of silicon, the second generation of solar cells from thin films (Thin Film Solar Cell), and the third generation of solar cells that are sensitized by dyes (Dye Synthesized Solar Cell) [12]. The first generation made of silicon has the best efficiency level, but the price of production and maintenance is expensive. Then, thin film solar cells produced countercurrent silicon (amorphous silicon). After that, DSSC (Dye-Sensitized Solar Cell) has several advantages such as chemical flexibility, ease of synthesis, and environmental friendliness [13]. For now, silicon solar cells are most widely used because they have higher efficiency than other types. Monocrystalline silicon solar cells have an efficiency of 17%-18%, and polycrystalline silicon solar cells have an efficiency of 12%-14% [14]. The efficiency of solar cells may also decrease as the open circuit voltage parameters and power output decrease due to temperature increase. As the temperature of photovoltaic (PV) panels rises, their efficiency and heat transfer capabilities decline. Implementing cooling methods for PV panels can help improve their efficiency [15].

Accurate temperature regulation is critical to maintaining

the operational performance of photovoltaic (PV) panels. Empirical data indicate that PV panel efficiency deteriorates by approximately 0.5% for every 1°C increment in temperature [16]. Consequently, implementing effective cooling strategies is imperative to counteract thermal-induced efficiency losses and sustain optimal photovoltaic performance. A cooling system on PV panels will increase electrical efficiency, extend life, and prevent cell damage [17]. Several PV panel cooling processes exist. The photovoltaic thermal collector (PV/T) system operates on the forced convective heat transfer principle, achieved by circulating a working fluid through pipes installed beneath the photovoltaic (PV) panels. This mechanism facilitates the efficient removal of heat from the PV module, enhancing its thermal management and overall performance [18]. The majority of PV panels have thermal collectors installed behind them. As the temperature of the photovoltaic (PV) panel rises, the heat transfer rate to the thermal collector correspondingly increases. Consequently, the collector acts as an efficient coolant, reducing the PV panel temperature by maximizing heat extraction, facilitating enhanced thermal energy generation. [19].

The working fluid is essential to the energy transfer's cooling or heating process. The working fluid flows to move the absorbed heat [20]. This working fluid can be air or water. However, working fluids in water are most often used because they perform better than air [21]. Another type is nano-fluid, a mixture of nano-sized metal particles dispersed into a base fluid. Due to their ability to improve PV/T performance, nanofluids have attracted the attention of researchers over the past few decades [22]. Nanofluids, containing nanoparticles under 100 nm, demonstrate enhanced thermal conductivity due to improved dispersion stability. This property significantly boosts heat transfer efficiency, enabling the development of more compact and practical photovoltaic thermal (PV/T) systems without compromising electrical output [23].

This research aimed to improve the thermal regulation of finned photovoltaic/thermal (PV/T) collectors by employing Al₂O₃, CuO, and TiO₂ nanofluids as the circulating working fluids. These nanofluids are intended to effectively lower the operational temperature of solar cells, thereby reducing

thermal losses and enhancing overall photovoltaic efficiency. A comprehensive comparative study is performed to assess the cooling capabilities and efficiency improvements provided by each type of nanofluid and determine the most effective nanofluid formulation to optimize both thermal and electrical performance of finned PV/T collectors under realistic working conditions.

2. STATE OF THE ART

Integrating nanofluids into photovoltaic-thermal (PVT) systems is a cutting-edge strategy to improve solar energy efficiency through more effective heat management. As summarized in Table 1, various types of nanofluids such as Al₂O₃/water, CuO/water, and TiO₂/water exhibit improved heat transfer characteristics, which directly reduce the operating temperature of PV panels and increase electrical output. For example, Al₂O₃/water can lower the panel temperature by 28.1% and increase the electrical efficiency by 7.38%. At the same time, hybrid nanofluids such as Al₂O₃-CuO/water combine the advantages of thermal conductivity and fluid stability. These findings confirm the importance of selecting the proper nanofluid formulation to optimize system performance. The comparative analysis in Table 1 also shows that nanoparticle composition and base fluid type significantly influence performance parameters, which can serve as a reference in developing next-generation PVP systems that are more efficient and sustainable.

Incorporating nanofluids such as Al₂O₃, CuO, and TiO₂ into photovoltaic thermal systems offers a comprehensive approach to enhance solar energy efficiency significantly. By leveraging their superior heat transfer properties and advanced thermal management capabilities, these nanomaterials contribute to maintaining optimal operating temperatures, thereby improving solar systems' thermal and electrical performance. This integration optimizes energy conversion and supports the advancement of sustainable solar technologies, positioning nanofluids as key enablers in pursuing more efficient and reliable renewable energy solutions.

Table 1. State of the art

Nanofluid Type	Base Fluid	Key Findings	Performance Metrics	References
Al ₂ O ₃ /water	Water	Improves thermal conductivity and heat transfer; lowers PV temperature.	Up to 28.1% temp. reduction, 7.38%↑ electrical efficiency	[24-26]
CuO/water	Water	Enhances convective heat transfer and improves cooling efficiency.	Significant increase in heat removal rate.	[27, 28]
TiO ₂ /water	Water	Enhances solar water distillation productivity and PVT heat transfer.	Boosts thermal output, improves PVT productivity.	[29, 30]
Al ₂ O ₃ -CuO/water (Hybrid)	Water	Combines properties for higher stability and thermal conductivity than single-component nanofluids.	Higher thermal performance, better fluid stability.	[31-34]
Various nanoparticles	Ethylene Glycol, Oil, etc.	Used in hybrid configurations to explore optimized thermophysical properties.	Ongoing trials to determine optimal concentration.	[35, 36]
Al ₂ O ₃ , CuO, TiO ₂ (comparative)	Water	Comparative studies show each material has unique thermal and electrical advantages in PVT systems.	Tailored selection improves system efficiency.	[37-39]

3. EXPERIMENTAL METHODS

3.1 Experimental setup

The configuration of finless, triangle fin, and rectangular fin collectors is implemented. The configuration and working principle of the Photovoltaic/Thermal (PV/T) system are schematically depicted in Figure 1. A pump starts the system by drawing water out of the reservoir and sending it via a conduit to the collector under the PV panel. The practical application of the PV/T system is demonstrated in Figure 2, showcasing its setup in an experimental environment. The system comprises a polycrystalline photovoltaic panel, collector, pump, nanofluid reservoir, flow meter, heat exchanger tank, thermocouple data logger, multimeter, solar power meter, and rheostat slide. This experimental investigation was conducted in July 2024 at Universitas Sebelas Maret, Surakarta, Indonesia, providing real-world insights into the performance and operational characteristics of the PV/T system.

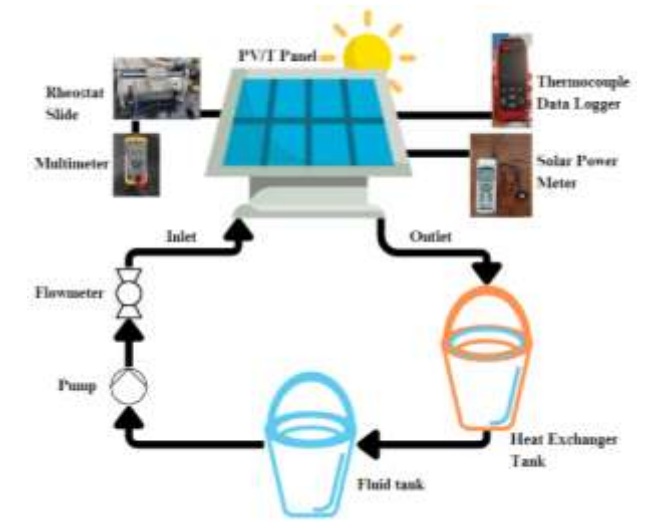


Figure 1. Scheme of the system component

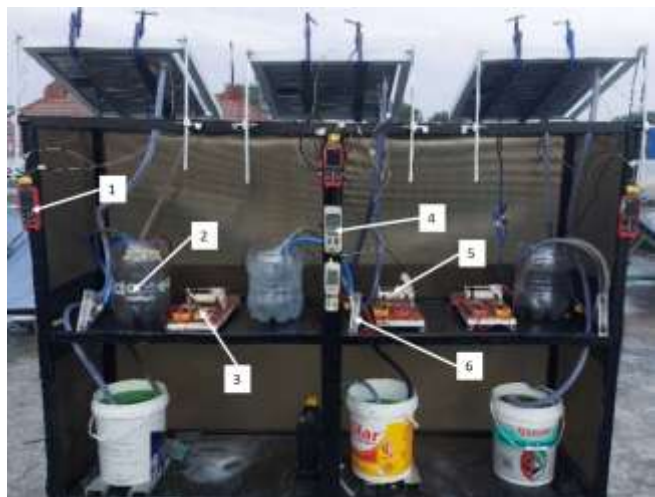


Figure 2. Research tool suite

- List:
- 1. Thermocouple data logger
 - 2. Water pump
 - 3. Multimeter
 - 4. Solar power meter

- 5. Rheostat slide
- 6. Flowmeter

3.2 System component

3.2.1 Photovoltaic panel

The solar panel employed in this study is a 50 Wp (Watt-peak) polycrystalline solar panel manufactured by Sunwatt. This type of solar panel offers increased efficiency because it uses polycrystalline cells, which can work in high temperatures, and has a strong square design with high durability. The Sunwatt 50 Wp Solar Panel is shown in Figure 3 and Table 2.



Figure 3. Sunwatt 50 Wp solar panel

The photovoltaic (PV) panel used in this study has a maximum power output of 50 W, corresponding maximum current and voltage values of 2.77 A and 18.0 V, respectively. Under open-circuit conditions, the panel produces a voltage of 21.24 V and a current of 3.11 A, indicating its capacity to generate power even without a connected load. The panel's overall energy conversion efficiency is 17.6%, which reflects its effectiveness in converting incident solar radiation into usable electrical energy. With physical dimensions of 670 × 530 × 30 mm, the panel is compact and suitable for integration into hybrid PV/T systems. These specifications provide a foundational understanding of the panel's electrical behavior and serve as key inputs for performance analysis and system modeling.

3.2.2 Thermal collector

The collector pipe is designed according to the shape of the solar panel to expand the contact so that it absorbs more heat. In addition, the flow configuration is a series flow. The collector pipe used in this study is a collector pipe with a rectangular shape, as shown in Figure 4 below. Collector pipes with rectangular shapes are chosen because they have better thermal efficiency than other shapes. The specifications and dimensions of the square collector pipe utilized in this study are detailed in Table 2, providing essential parameters for the experimental setup and subsequent analysis of thermal performance.

Table 2. Collector pipe specifications

Specification	Information
Material	Aluminum
Cross Section Size	0.030 m × 0.015 m
Thick	0.001 m
Fin Thickness	0.0005 m
Total length	4.61 m

Table 3. List of components [24-27]

Name of Component	Key Specifications	Function in PV/T System	Illustration
Water Pump	SAKKAI SKP 106, 45 W power, flow capacity up to 3500 L/h	Circulates the working fluid within the PV/T system	
Flowmeter	Measures up to 7 L/min; operated at 3 L/min in this study	Measures fluid flow rate to monitor thermal transfer performance	
Thermocouple data logger	TASI TA612C, 4 Channel, K Type Thermometer, USB	Records the inlet and outlet temperatures of the collector and PV surface temperatures	
Multimeter	HELES UX-838TR	Measures voltage (V) and current (I) generated by PV panels	
Solar power meter	Lutron SPM-1116SD, real-time logging to micro-SD	Measures solar radiation intensity in real time	
Rheostat slide	Variable resistor, 2 A, 50 Ohm	Controls the electrical current in the PV circuit to simulate different load conditions	

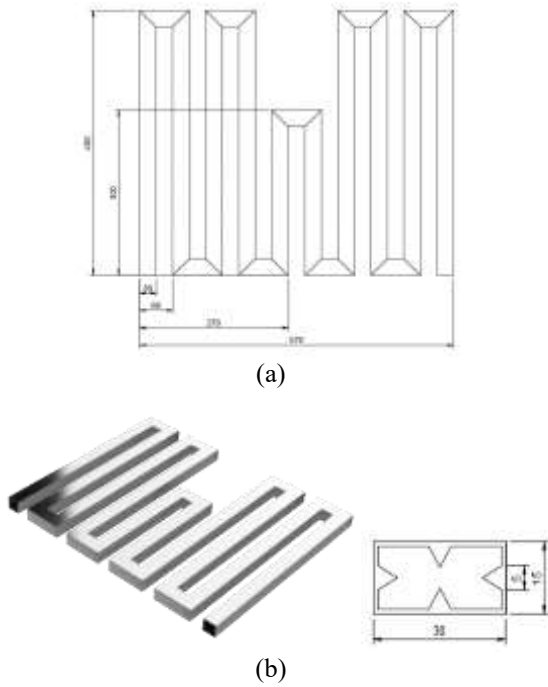


Figure 4. Collector pipe with four fins

Table 3 lists the essential components employed in the PV/T experimental setup. These include instruments for fluid circulation, temperature measurement, electrical monitoring, and solar radiation analysis. Each element was selected based on suitability and compatibility with the system's operational requirements. The table also outlines the specifications and functions of each device to ensure clarity and replicability of the experimental procedure.

3.3 PV efficiency analysis

Analyzing the efficiency of photovoltaic (PV) systems is essential to evaluate how effectively solar energy is converted into usable electrical and thermal energy. This efficiency is governed by various electrical and thermal parameters, which can be quantified through theoretical models and experimental data. Table 4 presents the key equations for assessing PV performance, from short-circuit current to thermal efficiency. Each parameter is critical in determining how well a solar cell transforms incident solar radiation into electrical and thermal outputs. A clear understanding of these relationships provides a systematic and quantitative foundation for optimizing the design and operation of PV systems, especially in hybrid photovoltaic/thermal (PV/T) applications.

Table 4. Equations of PV efficiency

Parameter	Symbol	Description	Equation	Number
Short Circuit Current	I_{sc}	Maximum current when electrical resistance is near zero [40]	Determined experimentally from the I-V curve when voltage = 0	-
Diode (I-V) Equation	I	Fundamental equation describing PV cell behavior using Shockley's diode model [41]	$I = I_{ph} - I_0 \left(e^{\frac{qV}{k_B T}} - 1 \right)$	(1)
Open Circuit Voltage	V_{oc}	Maximum voltage when no current flows through the circuit [42]	$V_{oc} = \frac{k_B T}{q} \ln \left(1 + \frac{I_{ph}}{I_0} \right)$	(2)
Fill Factor (FF)	FF	Indicates how efficiently the cell converts power from available current and voltage	$FF = \frac{I_m V_m}{I_{sc} V_{oc}} = \frac{P_{max}}{I_{sc} V_{oc}}$	(3)
Electrical Efficiency	η_{pv}	Ratio of maximum output power to incident solar radiation power [43]	$\eta_{pv} = \frac{P_{max}}{P_{light}} = \frac{I_{sc} V_{oc} \times FF}{I_{rad} \times A}$	(4)
Thermal Efficiency	η_{th}	Efficiency of heat recovery in a PV/T system	$\eta_{th} = \frac{Q_u}{I_{rad} \times A} = \frac{\dot{m} C_p (T_e - T_i)}{I_{rad} \times A}$	(5)

Table 5. Heat transfer theory

Parameter	Symbol	Description	Equation	Number
Conduction Heat Transfer	Q_{cond}	Heat transfer through a solid medium between the panel and the collector pipe	$Q_{cond} = k A \frac{(T_1 - T_2)}{L}$	(6)
Convective Heat Transfer	Q_c	Heat transfer due to fluid motion at the surface interface	$Q_c = h_c A_s (T_s - T_m)$	(7)
Convective Heat Transfer (LMTD method)	Q_c	More accurate convective heat transfer in heat exchangers using LMTD [44]	$Q_c = h_c A \Delta T_{lm}$	(8)
Logarithmic Mean Temp. Diff	ΔT_{lm}	Average practical temperature difference for convective heat exchange [45]	$\Delta T_{lm} = \frac{T_i - T_e}{\ln[(T_s - T_e)/(T_s - T_i)]}$ $= \frac{\Delta T_e - \Delta T_i}{\ln(\Delta T_e / \Delta T_i)}$	(9)
Useful Heat Transfer Rate	Q_u	Heat is absorbed by the working fluid in the collector pipe	$Q_u = \dot{m} C_p (T_e - T_i)$	(10)
Mass Flow Rate	\dot{m}	Mass flow rate of the working fluid	$\dot{m} = \rho \dot{V}$	(11)
Thermal Efficiency	η_{th}	Ratio of sound thermal energy to incident solar energy	$\eta_{th} = \frac{Q_u}{G \times A_m} = \frac{\dot{m} C_p (T_e - T_i)}{G \times A_m}$	(12)
Reynolds Number	Re	Dimensionless number indicating flow regime (laminar or turbulent)	$Re = \frac{\rho v D_H}{\mu}$	(13)
Nusselt Number	Nu	Dimensionless number indicating convection enhancement	$Nu = \frac{h_c D_H}{k}$	(14)

Table 6. Thermophysical parameter equations

Parameter	Symbol	Description	Equation	Number
Nanofluid Density	ρ_{nf}	Density calculated as a weighted average of the base fluid and nanoparticles	$\rho_{nf} = (1 - \phi)\rho_{bf} + \phi\rho_{np}$	(15)
Nanofluid Viscosity	μ_{nf}	Viscosity for low-volume fractions (e.g., 2.5%) based on Einstein's model	$\mu_{nf} = (1 + 2.5\phi)\mu_{bf}$	(16)
Specific Heat Capacity	cp_{nf}	Heat capacity calculated from volume-fraction-weighted average of base fluid and nanoparticles	$cp_{nf} = c_{bf}(1 - \phi) + C_{np}\phi$	(17)
Thermal Conductivity	k_{nf}	Effective conductivity using the Maxwell model for spherical particles	$k_{nf} = \left[\frac{k_{np} + 2k_{bf} + 2\phi(k_{np} - k_{bf})}{k_{np} + 2k_{bf} - \phi(k_{np} - k_{bf})} \right] k_{bf}$	(18)

3.4 Heat transfer in the working fluid

Heat transfer analysis is fundamental in evaluating the thermal performance of photovoltaic/thermal (PV/T) systems. Heat transfer within these systems occurs primarily through conduction and convection and, in more complex models, through logarithmic mean temperature difference (LMTD) methods for enhanced accuracy in heat exchanger analysis. Table 5 outlines the key parameters and equations involved in modeling heat transfer processes, including conduction through solid interfaces, convective heat exchange between surfaces and working fluids, and the calculation of useful heat gain. Additionally, the table includes essential dimensionless numbers such as the Reynolds and Nusselt numbers, which are critical in characterizing flow regimes and convective heat transfer performance. Understanding these theoretical foundations allows for precise thermal modeling and optimization of PV/T system design, ensuring more effective energy conversion and heat recovery under varying operational conditions.

3.5 Thermophysical properties of nanofluids

Accurate characterization of thermophysical properties is essential for evaluating the performance of nanofluids in photovoltaic/thermal (PV/T) systems. These properties significantly influence heat transfer, fluid flow, and system efficiency. Table 6 presents key equations used to estimate the effective thermophysical parameters of nanofluids, including density, viscosity, specific heat capacity, and thermal conductivity. These formulations incorporate the effects of nanoparticle concentration (volume fraction) and are derived from established theoretical models such as Einstein's equation for viscosity and the Maxwell model for thermal conductivity. By accounting for the combined behavior of base fluids and dispersed nanoparticles, these equations provide a foundation for accurately modeling nanofluid-enhanced PV/T systems and optimizing their thermal management performance.

4. RESULT AND DISCUSSION

4.1 Temperature of PV panel

The efficiency of photovoltaic (PV) panels tends to decrease as their operating temperature rises. To counter this, a finned photovoltaic thermal (PV/T) collector cooling system is implemented to lower the panel temperature effectively. This system circulates a working fluid inside the collector tubes, which in this study comprises various nanofluids containing nanoparticles such as Alumina (Al_2O_3), Copper Oxide (CuO),

and Titanium Dioxide (TiO_2) at a nanoparticle volume fraction of 0.2%. The thermophysical characteristics of these nanofluids, calculated through Eqs. (15)-(18), are detailed in Table 7. Additionally, Figure 10 illustrates how the PV panel's operating temperature increases with rising solar radiation intensity, underlining the critical role of thermal management in maintaining PV panel performance.

Table 7. Thermophysical properties of nanofluids

Nano-Fluid	Density (kg/m ³)	Dynamic Viscosity (mPa.S)	Specific Heat (J/kg.K)	Thermal Conductivity (W/m.K)
Water	997.047	0.0008910	4182	0.60960
CuO (0.2%)	1008.053	0.0008955	4171.32	0.61307
TiO_2 (0.2%)	1003.513	0.0008955	4172.026	0.61257
Al_2O_3 (0.2%)	1002.973	0.008955	4172,188	0.61310

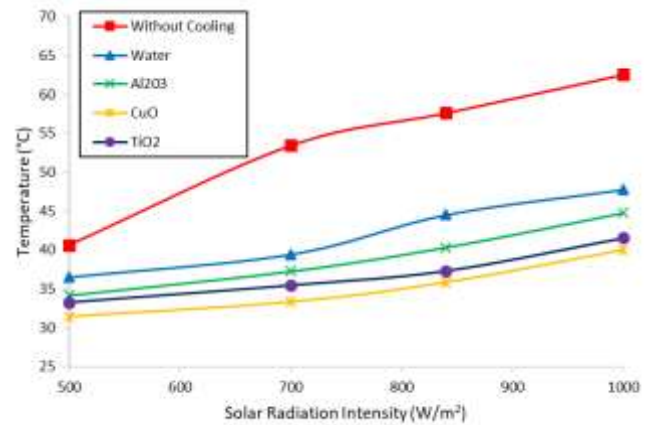
**Figure 5.** Effect of solar radiation intensity on the working temperature of finned PV panels

Figure 5 presents research data illustrating the correlation between solar radiation intensity and the operating temperature of finned photovoltaic (PV) panels. As solar radiation intensity increases, the working temperature of all studied PV panel variations rises correspondingly. Panels without cooling exhibit the highest temperatures compared to those with PV/T cooling systems. At a solar radiation intensity of 500 W/m², the operating temperatures for uncooled PV panels, water-cooled PV/T panels, and PV/T panels using Al_2O_3 , CuO, and TiO_2 nanofluids are approximately 40.65°C, 36.53°C, 34.15°C, 31.45°C, and 33.25°C, respectively. When the solar radiation intensity increases to 1000 W/m², these temperatures rise to 62.54°C, 47.79°C, 44.78°C, 40.01°C, and

41.56°C, respectively. Notably, the nanofluids Al_2O_3 , CuO , and TiO_2 reduce the temperature of finned PV/T panels by 17.76°C, 22.53°C, and 20.98°C, respectively, compared to uncooled PV panels. A comparative graph of PV panel temperature versus time is provided in Figure 6 to depict these thermal performance trends.

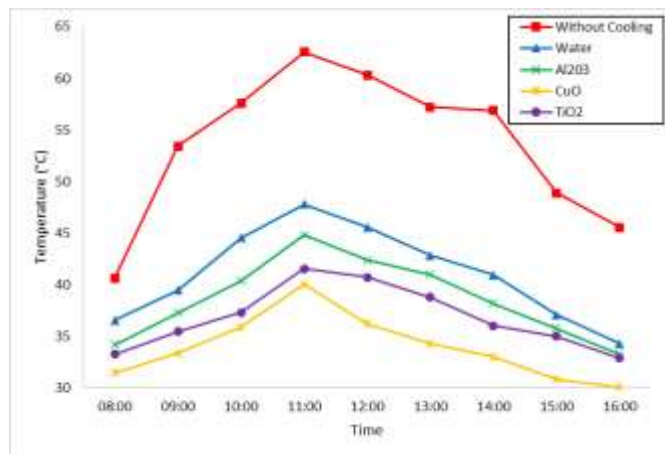


Figure 6. Time and temperature relationship graph of PV panel

The data was collected to analyze the influence of solar radiation intensity on the temperature of photovoltaic (PV) panels. The findings reveal a strong correlation between the intensity of solar radiation and the panel temperature. As the solar radiation intensity increases, the PV panel's temperature rises accordingly, negatively impacting its efficiency. This temperature increase on the PV panel surface results from the continuous absorption of solar radiation. Consequently, higher solar radiation intensities lead to elevated PV panel temperatures [25]. Another study by Talib K. Murtadha explained that PV panels without cooling have a temperature of about 59°C. In comparison, PV panels that use nano fluid cooling in Al_2O_3 / TiO_2 have a temperature of 48°C when the intensity of solar radiation reaches 906,2 W/m^2 [26]. A photovoltaic thermal (PV/T) system was employed to lower the PV panels' surface temperature effectively. By using the collector integrated into the system, the operating temperature of the PV panels during daylight hours was reduced compared to the panels operating without any cooling mechanism.

4.2 Panel output power

Electrical power generated by solar cells is determined by the product of the voltage and current they produce [27]. The maximum output power of photovoltaic (PV) panels is achieved when the multiplication of current and voltage reaches its highest value for each variation studied. This maximum power represents the most significant amount of energy the PV panel delivers per unit of time (seconds). The relationship between the maximum power output and solar radiation intensity is illustrated in Figure 7, providing insight into the performance characteristics of the panels under varying illumination conditions.

Figure 7 depicts the influence of increasing solar radiation intensity on the maximum power output (P_{\max}) of photovoltaic (PV) panels. The data indicate that as solar radiation intensity rises, the power generated by the PV panels increases consistently for both uncooled and cooled systems. This trend aligns with fundamental photovoltaic theory, which posits that

an increase in incident solar radiation enhances photon absorption, generating more electrons and resulting in higher electrical power output, specifically, at a solar radiation intensity of 1000 W/m^2 , the finned PV panels yield maximum power values of 31.13 W for uncooled panels, 33.13 W for water-cooled panels, 36.82 W for panels cooled with Al_2O_3 nanofluid, 48 W for CuO nanofluid, and 44.40 W for TiO_2 nanofluid, respectively.

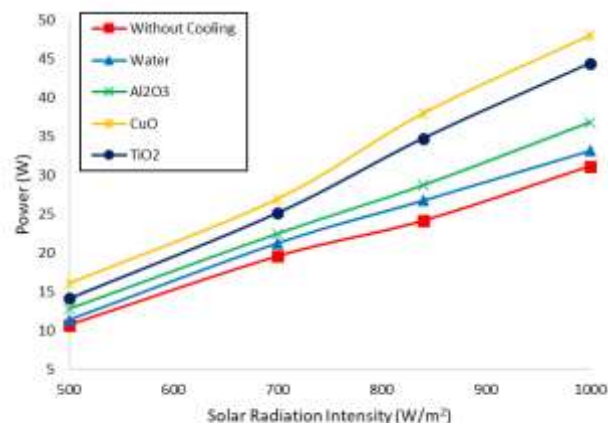


Figure 7. Graph of the effect of solar radiation intensity on maximum power (P_{\max})

The findings of this study are consistent with previous research investigating the relationship of nanofluid as a working fluid. For instance, Talib K. Murtadha and Ali Adil Hussein demonstrated that the incorporation of Al_2O_3 nanofluid as a cooling medium increased the maximum power output to approximately 43.80 W, compared to 39.50 W observed in uncooled PV panels under a peak solar radiation intensity of around 880 W/m^2 . This reinforces the efficacy of nano-fluid cooling in enhancing PV panel performance under high solar irradiance conditions [28]. Research by Ali H.A. Al-Waeli et al. showed that the maximum power value of Al_2O_3 and CuO nano-fluid cooling has a difference of 18 W with those that only use water cooling alone [29].

4.3 I-V and P-V curves

Evaluating the current-voltage (I-V) and power-voltage (P-V) curves is fundamental to understanding the performance of photovoltaic (PV) panels and identifying their optimal operating condition, known as the Maximum Power Point (M_{PP}). The I-V curve represents the relationship between the current output and the voltage applied to the PV panel, while the P-V curve demonstrates how the power output changes with voltage. This study includes an examination of both curves to assess the efficiency and performance of the PV panels under various conditions. The highest efficiency was recorded at a solar radiation intensity of 1000 W/m^2 , indicating that radiation intensity is a critical factor for performance assessment. Figures 8 and 9 illustrate the voltage, current, and power data for the finned PV/T panels.

Figures 8 and 9 show the performance parameters of finned PV/T panels under a solar radiation intensity of 1000 W/m^2 . The maximum voltages recorded for panels with different cooling variations—no coolant, water, Al_2O_3 , CuO , and TiO_2 —are 15.47 V, 16.45 V, 17.20 V, 18.22 V, and 17.69 V, respectively. Lowering the operating temperature of the PV panels increases the maximum current output.

Correspondingly, the maximum currents obtained for the uncooled, water-cooled, Al₂O₃ nanofluid, CuO nanofluid, and TiO₂ nanofluid cooled panels are 1.75 A, 1.93 A, 2.12 A, 2.68 A, and 2.42 A, respectively. These variations' maximum power outputs (P_{max}) are 31.13 W, 33.13 W, 36.82 W, 48 W, and 44.40 W, respectively.

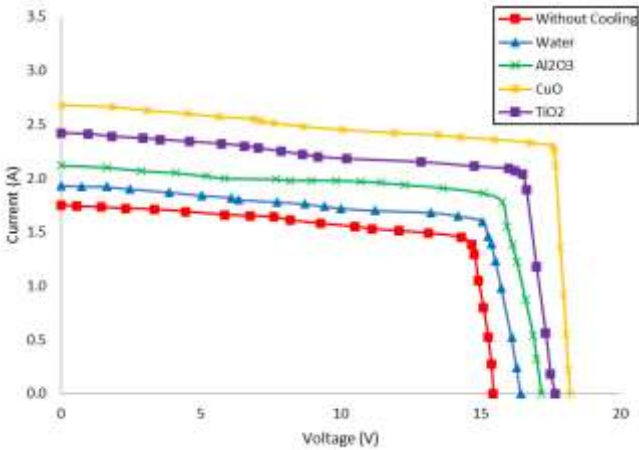


Figure 8. Graph of the relationship between current and voltage at the intensity of 1000 W/m² on the finned PV/T

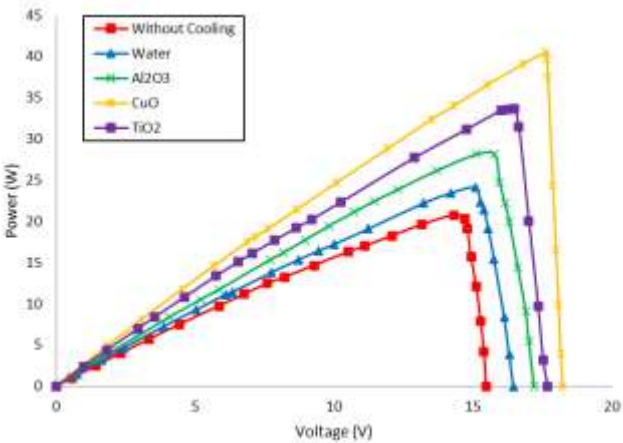


Figure 9. Relationship graph between power and voltage at the intensity of 1000 W/m² on the finned PV/T

The results align with the study by Wang et al., who conducted both numerical simulations and experimental evaluations of nano-fluid-based photovoltaic-thermal (PV/T) collectors. Their research demonstrated that applying Al₂O₃ nano-fluid as a coolant in PV/T panels led to a 5.47% improvement in thermal efficiency and a marginal increase of 0.026% in electrical efficiency [30].

4.4 Efficiency of panel

The electrical efficiency of a photovoltaic (PV) panel is a crucial metric that indicates the panel's capability to convert incident solar radiation into electrical energy. This efficiency is calculated as the ratio of the maximum power output (P_{max}) to the total solar radiation power received by the panel. For photovoltaic-thermal (PV/T) systems, the electrical efficiency can be determined using the expression provided in Eq. (5). The results of this electrical efficiency calculation are shown in Figure 10.

Figure 10 presents the relationship between solar radiation intensity and the electrical efficiency of photovoltaic (PV)

panels. At an irradiance level of 1000 W/m², the electrical efficiencies for different finned PV/T panel configurations—uncooled, water-based, and those using Al₂O₃, CuO, and TiO₂ nanofluids—are observed at 9.26%, 9.85%, 10.95%, 14.28%, and 13.21%, respectively. The electrical efficiency exhibits an increasing trend within the solar intensity range of 500 W/m² to 1000 W/m², with the CuO nanofluid-based PV/T panels achieving the highest efficiency enhancement.

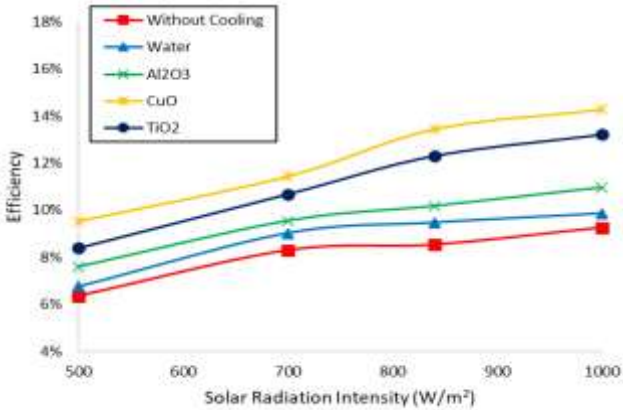


Figure 10. The relationship between solar radiation intensity and efficiency

Increasing the temperature of the PV panel can cause its performance to decrease. With every 1°C temperature increase, the electrical efficiency of the PV panel decreases by 0.05%, and the power decreases by 0.5% [16]. Research conducted by Shankar Amalraj et al. [31] indicates that an increase in solar radiation intensity enhances the electrical efficiency of photovoltaic (PV) panels, as more solar energy becomes available for conversion into electricity. Among the different cooling fluids studied, the PV panels cooled with CuO nanofluid achieved the highest electrical efficiency, reaching up to 16%, which surpasses the efficiencies attained by those cooled with Al₂O₃ and water, which are approximately 14% and 13%, respectively.

Thermal efficiency is the ratio of the heat energy generated by the photovoltaic-thermal (PV/T) system to the total heat energy incident on the system, as expressed in Eq. (12). Various factors influence the thermal performance of PV/T systems, including the operating temperature, the cooling fluid's flow rate, and the intensity of solar radiation. Figure 11 illustrates the thermal efficiency outcomes observed in the PV/T system evaluated in this study.

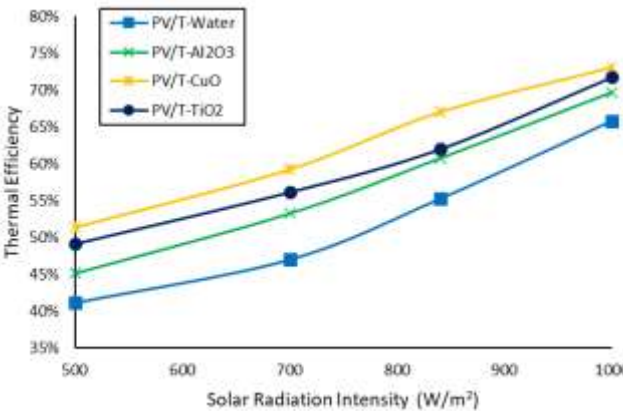


Figure 11. Graph of the relationship between solar radiation intensity and thermal efficiency on finned PV/T

Figure 11 illustrates the thermal efficiency of finned photovoltaic-thermal (PV/T) systems at a solar radiation intensity of 1000 W/m², with values recorded at 65.82%, 69.71%, 73.11%, and 71.75% for water, Al₂O₃, CuO, and TiO₂ cooling fluids, respectively. Higher thermal efficiency indicates a more effective conversion of heat energy for various applications. Incorporating nanofluids in PV/T systems significantly enhances heat transfer performance, improving overall thermal efficiency [32].

In this study, the CuO nanofluid demonstrated superior thermal performance compared to Al₂O₃ and TiO₂ nanofluids, primarily due to the inherently higher thermal conductivity of CuO nanoparticles. This enhanced thermal conductivity enables more effective heat dissipation from the photovoltaic cells, substantially lowering their operating temperature. Maintaining a reduced cell temperature is essential for minimizing thermal degradation and ensuring sustained improvements in photovoltaic conversion efficiency.

Nonetheless, the study reveals a nuanced trade-off between thermal efficiency (η_{th}) and electrical efficiency (η_{el}). While CuO nanofluid achieved the highest thermal efficiency by effectively extracting heat from the system, the corresponding improvement in electrical efficiency was comparatively moderate. This disparity is explained by the complex thermal-electrical performance dynamics inherent in photovoltaic devices, where maximal heat removal does not necessarily equate to proportional gains in electrical output. Therefore, an optimal nanofluid choice requires a comprehensive evaluation of thermal and electrical metrics to maximize overall system efficacy under operational conditions.

5. CONCLUSIONS

In each test and data collection, data processing has been carried out with variations of PV panels without cooling, PV/T-water, PV/T - Al₂O₃, PV/T-CuO, and PV/T- TiO₂. The conclusions obtained from this research are as follows:

1. Incorporating nanoparticles such as Al₂O₃, CuO, and TiO₂ into the cooling system effectively reduces the operating temperature of photovoltaic (PV) panels. At a solar radiation intensity of 1000 W/m², the temperature decreases observed were approximately 14.75°C, 17.76°C, 25.53°C, and 20.98°C, respectively.
2. Integrating Al₂O₃, CuO, and TiO₂ nanofluids into the finned photovoltaic-thermal (PV/T) system enhanced the performance of the PV panels compared to the uncooled finned PV/T panels. This improvement was evident in both the electrical power output and the overall conversion efficiency of the panels. The maximum power generated by uncooled PV panels, water, Al₂O₃, CuO, and TiO₂ is 31.13 W, 33.13 W, 36.82 W, 48 W, and 44.40 W, respectively. In addition, Al₂O₃, CuO, and TiO₂ nanofluids have higher electrical efficiency than uncooled PV panels or water, namely 10.95%, 14.28%, and 13.21%. At the same time, PV panels without cooling and water have efficiencies of 9.26% and 9.85%. As for the thermal efficiency of PV panels using cooling in water, Al₂O₃, CuO, and TiO₂ are 65.82%, 69.71%, 73.11%, and 71.75%, respectively.
3. Among the nanofluids investigated, CuO demonstrated superior thermal conductivity, resulting in the most effective temperature reduction of solar cells and consequently enhancing their photovoltaic performance.

The results underscore the critical interplay between thermal and electrical efficiencies, emphasizing the necessity of optimized nanofluid selection to balance these performance metrics for maximum overall system efficiency.

4. The findings highlight the potential of integrating nanofluid-based cooling strategies in PV/T systems to significantly mitigate thermal-induced energy losses in solar cells, thereby advancing the applicability of solar hybrid technologies in sustainable energy solutions. However, the moderate improvement in electrical efficiency despite high thermal extraction indicates that further research is essential to explore the complex thermal-electrical dynamics in PV/T systems.

Future work should focus on optimizing nanoparticle concentration, exploring hybrid nanofluids, and investigating long-term stability and environmental impacts to enhance the practical deployment of nanofluid-cooled PV/T collectors. Additionally, real-world testing under varied climatic conditions will be crucial for validating laboratory findings and promoting broader adoption of these advanced thermal management approaches.

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NOMENCLATURE

I_{rad}	intensity of sunlight, W/m^2
P	power, W
P_{max}	rated maximum power, W
P_{light}	solar radiation power, W
P_{out}	power output, W
V	voltage, V
V_{oc}	open circuit voltage, V
V_{max}	maximum voltage generated, V
I	current, A
I_{sc}	short circuit current, A
I_{max}	maximum current generated, A
I_{ph}	photogenerated current, A
I_0	saturation current diode, A
e	Euler's number
k_B	Boltzmann Constant, J/K
q	electrical charge, C
T	temperature, K
T_i	temperature in, K
T_e	temperature exit, K
T_s	temperature surface, K
FF	fill factor
A	PV panel surface area, m^2
Re	Reynolds number
Nu	Nusselt number
v	velocity, m/s
D_H	hydraulic diameter, m
\dot{Q}	Heat transfer rate, Joule/s
h	heat transfer coefficient, $\text{W}/(\text{m}^2 \cdot \text{K})$
\dot{m}	mass flow rate, kg/s
C_p	specific heat, $\text{J/kg} \cdot \text{K}$
K	thermal conductivity, $\text{W/m} \cdot \text{K}$
W	mass, kg
L	thickness medium, m

Greek symbols

η	efficiency, %
ρ	density, kg/m^3
ϕ	concentration, %
μ	dynamic viscosity, $\text{kg/m} \cdot \text{s}$
ΔT	temperature difference

Subscripts

np	nanoparticle
bf	base fluid
nf	nanofluid
sc	short current

oc	open circuit
ph	photogeneration
e	exit
i	in
th	thermal
rad	radiation