



Figure 18. Complete 30-Section 225liter capacity spherical tank developed



Figure 19. Body-filed 30-Section 225liter capacity spherical tank developed



Figure 20. Grey-Coated 30-Section 225liter capacity spherical tank developed

5. CONCLUSIONS

This paper has developed mathematical and procedural frameworks that will facilitate the development of spherical storage tanks. The effect of the number constituent sections on the sphericalness obtainable was also illustrated by developing a 225-litre capacity spherical storage tank using ten and twenty sections respectively. It is hoped that the framework developed will encourage the development and usage of spherical tanks when they are needed and not approximate them to cylindrical tanks with hemispherical caps.

ACKNOWLEDGMENT

The authors acknowledge with gratitude, the efforts of the Engineering Personnel of the Design, Modeling and Simulation Department as well as the Technical Staff of the Manufacturing Department of the Engineering Materials Development Institute Akure Nigeria for the valuable roles they played in fabricating the spherical tank.

REFERENCES

- [1] Paliwal, D.N. (1988). Design of steel storage tanks with spherical bottoms. *International Journal of Pressure Vessels & Piping*, 35(5): 383-401. [http://dx.doi.org/10.1016/0308-0161\(88\)90134-2](http://dx.doi.org/10.1016/0308-0161(88)90134-2)
- [2] Shin, S.H., Ko, D.E. (2016). A study on forces generated on spherical type LNG tank with central cylindrical part under various static loading. *International Journal of Naval Architecture and Ocean Engineering*, 8(6): 530-536. <http://dx.doi.org/10.1016/j.ijnaoe.2016.07.001>
- [3] Hutchinson, J.W. (2016). Buckling of spherical shells revisited. *Proc. R. Soc. A*, 472(2195): 1-25. <https://doi.org/10.1098/rspa.2016.0577>
- [4] Afkar, A., Camari, M.N., Paykani, A. (2014). Design and analysis of a spherical pressure vessel using finite element method. *World Journal of Modelling and Simulation*, 10(2): 126-135.
- [5] Zhang, S.H., Wang, B.L., Shang, Y.L., Kong, X.R., Hu, J.D., Wang, Z.R. (1994). Three-dimensional finite element simulation of the integral hydrobulge forming of a spherical LPG tank. *International Journal of Pressure Vessels & Piping*, 65: 47-52. [http://dx.doi.org/10.1016/0308-0161\(94\)00158-F](http://dx.doi.org/10.1016/0308-0161(94)00158-F)
- [6] Sivy, M., Musil, M. (2018), Design of the spherical liquid storage tanks for earthquake resistance. *ANNALS of Faculty Engineering Hunedoara – International Journal of Engineering Tome XVI*.
- [7] Lee, H.S., Yoon, J.H., Park, J.S., Yi, Y.M. (2005). A study on failure characteristic of spherical pressure vessel. *Journal of Materials Processing Technology*, 164-165: 882-888. <https://doi.org/10.1016/j.jmatprotec.2005.02.208>
- [8] Baaji, B., Saraswathamma, K., Madabhusi, R., Sutar, S. (2016). Design and analysis of spherical pressure vessels with pressure and thermal effects. *International Journal of Mechanical Engineering and Automation*, 3(6): 239-248.
- [9] Roylance, D. (2001). *Pressure Vessel. A Monograph in the Department of Materials Science and Engineering Massachusetts Institute of Technology Cambridge, MA 02139.*
- [10] Mercy, D., Girirajkumar, S.M. (2017). Modeling and analysis of a real time spherical tank process for sewage treatment plant. *International Journal of Applied Mathematics & Information Sciences*, 11(5): 1491-1498. <http://dx.doi.org/10.18576/amis/110528>
- [11] Gere, J.M. (2004). *Mechanics of materials*. 6th Edition, Thomson Learning, Inc. <http://dx.doi.org/10.1007/978-1-4899-3124-5>
- [12] Avinash, K.K., Mathews, M. (2015). Internal model control design for nonlinear spherical tank level process. *IJETS*, 2(8): 12-18.
- [13] Krishnapriya, K., Devi, M.R., Roshini, U., Jayachitra,

- A. (2017). Analyzing the performance of interacting spherical tank system using internal model controller (IMC) and Metaheuristic algorithm. *International Journal of Advanced Research in Computer and Communication Engineering*, 6(4): 36–42.
- [14] Yuan, S.J., Wang, F.Z., Wang, Z.R. (1997). Safety analysis of 200 m³ LPG spherical tank manufactured by the dieless hydro-bulging technology. *Journal of Materials Processing Technology*, 70: 115-219. [http://dx.doi.org/10.1016/S0924-0136\(97\)02920-8](http://dx.doi.org/10.1016/S0924-0136(97)02920-8)
- [15] Bharathi, M., Selvakumar, C., Kalpana, A. (2014). Model based controller design for a spherical tank. *IOSR Journal of Electrical and Electronics Engineering (IOSR-JEEE)*, 9(2): 74-79. <http://dx.doi.org/10.9790/1676-09267479>
- [16] Muthumari, S., Rakesh Kumar, S. (2017). Design of robust controller for hemi-spherical tank system using volumetric observer. *International Journal of Applied Engineering Research*, 12(17): 6477-6481.

NOMENCLATURE

$\tau_{r\theta}$, $\tau_{\theta r}$, $\tau_{r\theta}$	Shear Stresses in different planes in N/m ²
$\tau_{\theta r}$, $\tau_{\theta\theta}$, $\tau_{\theta\theta}$	Normal Stress in N/m ²
σ_{rr}	Normal Stress in N/m ²
n_1	Number of Sections
n_2	Number of Minor Circles
X_0	Equivalent base (arc) length of each section of the sphere in mm
R	Great Circle Radius in mm
α	Angle subtended by an arc of the section in degrees
L	Length of an Arc of a constituent great circle
C_0, C_n	Equivalent Chord Length in mm
β	Angle subtended by a minor arc