


```

%the coefficient of the new variable meu
LHS_C(:,end+1)=0;
%multiply the objective functions by
%the weights and -1, since they are
%maximization, and add them together
%to have a single objective
obj=-1*w1*obj1_n+w2*obj2_n;
%get the RHS to the LHS by negative sign ,
%because it now contains variable meu
LHS_C(:,3)=-1*RHS_C;
%now the RHS is zero
RHS_C(:,1)=0;
%add the new equality constraint of the meu
%as 2 equations, one greater than and one less than
N_LHS_C=cat(1,LHS_C, obj1_2_d,-1*obj1_2_d);
% add the RHS of the two new constraints which is 1 & -1
N_RHS_C=cat(1,RHS_C,[1;-1]);
%solve the new problem using linear programming function
lb=zeros(3,1);
[x,fval]=linprog(obj,N_LHS_C,N_RHS_C,[],[],lb);
fprintf('The optimal objective function value :')
%The new equation is now min, no need to multiply by -1
z=fval
fprintf('The optimal values of the decision variables')
x

```

RUN
Optimization terminated.
The optimal objective function value:
z =
-0.4861
The optimal values of the decision variables
x =
0.0000
0.1944
0.0556

6. CONCLUSIONS AND FUTURE WORKS

In this paper, a computational hybrid algorithm and a MATLAB program based on the Charens - Cooper transformation method and the weighting method to generate Pareto optimal solutions for the FLMO problems are introduced. By comparing the results in sections 4 and 5: the hand solution of the numerical example by the computational hybrid algorithm and the solution by the software is the same.

The scientists and the engineers can apply the presented MATLAB program and the hybrid algorithm to different practical FLMO problems to obtain numerical Pareto optimal solutions.

Several algorithms and codes can be built to solve different kinds of FLMO problems using various methods to obtain numerical Pareto optimal solutions.

REFERENCES

- [1] Abo-Sinna MA, Abou-El-Enien THM. (2005). An algorithm for solving large scale multiple objective decision making problems using TOPSIS approach. *AMSE Journals, Advances in Modelling and Analysis A* 42(6): 31-48.
- [2] Chankong V, Haimes YY. (1983). *Multiobjective decision making: Theory and methodology*. North-

- Holand Series in Science and Engineering, North-Holand, USA,
- [3] El-Sawy AA, El-Khouly NA, Abou-El-Enien THM. (2000). An algorithm for decomposing the parametric space in large scale linear vector optimization problems: A fuzzy approach. *AMSE Journals, Advances in Modelling and Analysis C* 55(2): 1-16.
- [4] Hwang CL, Masud ASM. (1979). *Multiple objective decision making methods and applications*. Springer-Verlag, New York, USA. <https://doi.org/10.1007/978-3-642-45511-7>
- [5] Osman MSA, Hasan SA, Abou-El-Enien THM, Mohamed SM. (2005). Multiple criteria decision making-theory, applications and softwares: A literature review. *AMSE Journals, Advances in Modelling and Analysis B* 48(2): 1-38.
- [6] Sharma S, Bhattacharjee S, Bhattacharya A. (2015). Solution of multi-objective optimal DG placement problems using swine influenza model based optimization (SIMBO). *AMSE Journals, Advances C* 70(1): 46-70.
- [7] Zeleny M. (1982). *Multiple Criteria Decision Making*. McGraw-Hill, New York.
- [8] Sen GD, Sharma J, Goyal GR, Singh AK. (2017). A Multi-objective PSO (MOPSO) algorithm for optimal active power dispatch with pollution control. *IIETA journals, Mathematical Modelling of Engineering Problems* 4(3): 113-119. <https://doi.org/10.18280/mmep.040301>
- [9] Abou-El-Enien THM, Saad OM. (2010). On the solution of a special type of large scale linear fractional multiple objective programming problems with uncertain data. *Applied Mathematical Sciences* 4(62): 3095–3105.
- [10] Abou-El-Enien THM. (2014). Interactive TOPSIS algorithm for a special type of linear fractional vector optimization problems. *International Journal of Information Technology and Business Management* 31(1): 13-24.
- [11] Bhati D, Singh P, Arya R. (2017). A taxonomy and review of the multi-objective fractional programming (MOFP) Problems. *International Journal of Applied and Computational Mathematics*, September 3(3): 2695–2717.
- [12] Pramy FA, Islam MdA. (2017). Determining efficient solutions of multi-objective linear fractional programming problems and application. *Open Journal of Optimization* 6(4): 164-175. <https://doi.org/10.4236/ojop.2017.64011>
- [13] Saad OM, Abou-El-Enien THM. (2008). On the solution of a special type of integer linear fractional multiple objective programming problems. *AMSE Journals, Advances in Modelling and Analysis D* 13(1): 42-55.
- [14] Branch MA, Grace A. (1996). *Optimization Toolbox, User's Guide*. The MathWorks Inc.
- [15] Lopez CP. (2014). *MATLAB optimization techniques*. Apress Academic, Springer, New York, USA,
- [16] Venkataraman P. (2009). *Applied Optimization with MATLAB Programming*. 2ed, John Wiley & Sons, Inc, New Jersey, USA.
- [17] Works M. (2010). *MATLAB Reference Guide*. The MathWorks Inc., Natick.
- [18] Charnes A, Cooper WW. (1962). Programming with linear fractional criteria. *Naval Res. Logist Quart.* 9: 181–186.