Diffusion Model for Simulating the Kinetics of Boronizing Process in the Case of FeB/Fe₅B Bilayer Configuration

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1. INTRODUCTION

Boronizing is a thermochemical treatment in which the boron atoms are diffused into the surface of a treated material at high temperatures generally between 1223 K and 1373 K [1, 2], with an aim of forming a boronized layer, the diffused boron atoms in the iron matrix lead to the formation of two kinds of iron (FeB and Fe₅B) in case of steels or Armco iron [2], the formed boronized layer confers to the material a high surface hardness (>1700HV) which is maintained at high temperatures [3]. This thermochemical treatment provides to the material a good resistance to abrasive and adhesive wear.

Boronizing can be carried out by different methods. The medium of boronizing can be solid (paste or powder), liquid or gas [3, 4].

With the use of this treatment and based on many studies, for a low potential we have only the formation of a single boronized layer constituted of Fe₅B phase. In the case of a higher activity of boron, we have a bilayer configuration (FeB +Fe₅B) [5, 6]. From the experimental standpoint, the Fe₅B and FeB layers have a saw-toothed morphology in case of carbon steels, low alloy steels and Armco iron [7].

Generally, in the industrial applications, a single layer Fe₅B is preferred because it is less brittle and forms a surface having a high compressive stress.

The bilayer configuration (FeB+Fe₅B) can be converted into a single layer (Fe₅B) by the diffusion annealing process [1-7] to improve its surface properties.

The quality of the boronized layer depends on the chemical composition of both the base material and the boronizing medium [7, 8].

Generally, the presence of some alloying elements in the treated material modifies strongly the structure of the boride layer by diminishing its thickness and slowing down the diffusion rate of boron atoms [1-9].

For the boronizing in powders, the samples are placed in the container filled with powders mixture containing a boron source, an activator and a diluent and they are put into the muffle furnace.

The significant advantages of this process are easy handling, simplicity, and the possibility of changing the chemical composition of the powder [7-10].

We can use the liquid boronizing process in molten salts with or without electrolysis.

In the gaseous medium, the gases supplying boron are boron halides (diborane and trimethyl) [10].

The growth kinetics of boride layers requires a mathematical model to simulate the boron diffusion and to calculate the boronized layer thickness in each phase.

The literature, there are various models [2, 11] used for modeling the boronizing kinetics of steels. Some of these models allow modeling the growth kinetics of Fe₅B and/or FeB layers. Furthermore, the majority of these models are based on the mass balance equations at the considered interfaces.

Theoretically, Brakman et al. [12], have proposed a simple model to study the boronizing process in powders. This model accounts for the specific difference in volume between the FeB and Fe₅B phases.

Zuno-Silva et al. [13] and Campos et al. [14] have suggested
a mathematical model based on the second Fick’s law to study the kinetics of the single layer (Fe₂B). Recently, Keddam et al. [2] proposed a diffusion model basing on the integral method to investigate the boronizing kinetics of AISI D2 steel. This model takes also into account the incubation times during the formation of boronized layers. A diffusion model was proposed by Mebarek et al. [15] in order to calculate the boride incubation time.

Campos et al. [16], Mebarek et al. and Genel et al. [9-17] applied the artificial intelligent method for modeling the boronizing kinetics.

In other model [12, 18], a fuzzy neural and neural network was used as an alternative approach for predicting the values of boronized layer thickness. This approach considered, as a simple tool, was employed to improve the previous model (the artificial network model) by using a few conditions to resolve the kinetics equations.

Recently, the LS-SVM [19] and the Neural-Fuzzy [18] methods were also used for estimating the boronizing kinetics. These two approaches were able to predict in a satisfactory way the boronized layer thickness.

In this study, a mathematical model of the boron diffusion was suggested to simulate the boronizing kinetics of AISI D2 steel in the case of powder method. The present diffusion model was based on solving the mass balance equations at the two growing interfaces (FeB/Fe₂B) and (Fe₂B) by ignoring the effect of boride incubation times on the kinetics.

The proposed model considered that the boron concentration profile was nonlinear in each phase. The influence of surface boron concentration on the growth kinetics of FeB and Fe₂B layers was investigated. The mass gain associated with the formation of iron borides was also estimated.

Finally, the present model has been validated experimentally by comparing the boride layers’ thicknesses with the predicted ones.

2. MATHEMATICAL MODEL OF THE DIFFUSION

Based on the second Fick’s law and the mass balance equations, we developed a model to simulate the kinetics of the bilayer configuration.

The knowledge of thermodynamic properties of the Fe-B phase diagram is significant for the boronizing process of AISI D2 steels and associated ferrous materials.

To solve a problem of the boron diffusion, the knowledge of the kinetic data and thermodynamic data are necessary.

From the Fe-B phase diagram, we note the existence of the following phases, α-Fe for the temperature range T≥1184.6 K, γ-Fe, FeB and Fe₂B.

Moreover, it can be seen that the solubility of boron in the phase γ-Fe is extremely low at high temperatures (T≥1184.6 K).

The diffusion of boron in the iron matrix can be described with the Fick’s second law.

\[
\frac{\partial C_i}{\partial t} = D_i \frac{\partial^2 C_i(x, t)}{\partial x^2} \tag{1}
\]

With:
- \( C_i(x,t) \) is the boron concentration in-depth \( x \) after a time \( t \) of diffusion.
- \( D_i \) is the boron diffusion coefficient in phase \( i \), with \( i = \{ \text{FeB, Fe}_{2}\text{B} \} \).

Figure 1 illustrates a schematic representation of the variation of the boron concentration at a given temperature and under a high boron potential which allows obtaining the two-phase configuration (FeB and Fe₂B).

The present diffusion model for studying the growth kinetics of FeB and Fe₂B considered that:
- The flux of boron atoms is perpendicular to the material surface.
- The temperature of the sample is constant during the process.
- The boron concentration at the material surface does not change with the time and the treatment temperature.
- The iron borides grow according to a parabolic law of time.
- The boride layer is very thin compared to the thickness of the sample.
- The diffusion of Fe can be neglected.

To calculate the shift of the interface (FeB/Fe₂B) and (Fe₂B/Fe), the mass balance equations given by the following formulas are used:

\[
\frac{1}{2}(C_1 + C_{FeB/Fe}_2) + \Delta C_1 \frac{d\lambda_1}{dt} = (\Delta j_1)_x = \lambda_1 \tag{2}
\]

\[
\frac{1}{2}(\Delta C_2 + \Delta C_3) \frac{d\lambda_2}{dt} + \frac{d\lambda_3}{2} = (\Delta j_3)_x = \lambda_2 \tag{3}
\]

With:

\[
\Delta C_1 = C_{FeB/Fe} - C_{FeB/Fe}_2 \quad \Delta C_2 = C_{FeB/Fe}_2 - C_{FeB/Fe}_3 \quad \Delta C_3 = C_{FeB/Fe}_3 - C_{FeB/Fe}
\]

\[
\Delta j_i = j_1 - j_2, \quad \Delta j_2 = j_3 - j_2 \text{ with } (1=FeB, 2=Fe}_2\text{B, 3=Fe)}
\]

The flux \( j_i \) of the boron atoms in the phase \( i \) with depth \( x \) which is related to the concentration gradient is given by Eq. (4):

\[
J_i = -D_i \frac{\partial C_i(x, t)}{\partial x} \tag{4}
\]
With \( i = (FeB, Fe_2B, Fe) \) and \( D_i \) the associated boron diffusion coefficient.

The thickness of the boronized layer is given by the following equation:

\[
\lambda_{FeB} = k_{FeB} \sqrt{t} \quad \text{and} \quad \lambda_{Fe_2B} = k_{Fe_2B} \sqrt{t}
\]  

(5)

In Eq. (5), \( k_{FeB} \) and \( k_{Fe_2B} \) are the respective values of growth rate constants for FeB and \( Fe_2B \) phases. \( \lambda_{FeB} \) and \( \lambda_{Fe_2B} \) represent the positions of the interfaces \( (FeB/Fe) \) and \( (Fe_2B/Fe) \) respectively.

The growth rate constant can be calculated from the resolution of the nonlinear Eqns. (2) and (3) by means of the Newton-Raphson numerical method.

The boron concentration in the iron matrix during the boronizing is given by Eq. (6). This formula represents a general solution of the second Fick’s law (1):

\[
C_i(x, t) = a_i + b_i \text{erf} \left( \frac{x}{2 \sqrt{D_i t}} \right)
\]

(6)

\( C_i(x, t) \): is the boron concentration in the iron matrix depending on the time and diffusion distance \( x \) where \( i \) denotes the iron phase.

where, erf is a Gauss error function, \( a_i \) and \( b_i \) are the constants to be determined according to the initial conditions and boundary conditions:

Initial condition:
for \( t=0 \) and \( x=0 \), \( C_i(x, 0)=0 \)

Boundary condition (\( t>0 \)):
- for \( x=0 \),
\( C_{FeB}(0, t) = C_{FeB}^{FeB} \) (the boron concentration at the surface).
- At the \( (FeB/Fe) \) interface:
\[
C_{FeB}(\lambda_{FeB}, t) = C_{FeB}^{FeB/FeB}, \quad C_{Fe_2B}(\lambda_{Fe_2B}, t) = C_{Fe_2B}^{Fe_2B/FeB}
\]

At the \( (Fe_2B/Fe) \) interface:
\[
C_{Fe_2B}(\lambda_{Fe_2B}, t) = C_{Fe_2B}^{Fe_2B/Fe}, \quad C_{Fe}(\lambda_{Fe_2B}, t) = C_{Fe}^{Fe_2B/Fe}
\]

for \( x=\infty \), \( C_{Fe}(\infty, t) = 0 \)

For our simulation, we used the input data, the diffusion coefficient in each phase, the surface boron concentration and boron concentrations at the considered interfaces.

The boron diffusion coefficients in the iron borides and the Fe phase were taken from references [2, 20] which are given by the following expressions:

\[
D_{FeB} = 1.7151 \times 10^{-4} \exp \left( - \frac{187.24 \times 10^3}{RT} \right)
\]  

(7)

\[
D_{Fe_2B} = 8.6579 \times 10^{-5} \exp \left( - \frac{177.39 \times 10^3}{RT} \right)
\]  

(8)

For 1184.6 K \( \leq T \leq 1273 \) K:

\[
D_{Fe}^{Fe} = 4.4 \times 10^{-9} \exp \left( - \frac{81.5 \times 10^3}{RT} \right)
\]  

(9)

For \( T < 1184.6 \) K:

\[
D_{Fe}^{Fe} = 8.3 \times 10^{-9} \exp \left( - \frac{62.7 \times 10^3}{RT} \right)
\]

(10)

With \( R=8.314 \) J/mol K

The value of the boron concentration at the surface used in the simulation is \( C_i=16.48 \) wt.%. For the two interfaces \( (FeB/Fe) \) and \( (Fe_2B/Fe) \), we used the values taken from the literatures [20, 21] which are the following:

\[
C_{Fe}^{FeB} = 16.23 \text{ wt.\%}, \quad C_{Fe}^{Fe_2B} = 16.23 \text{ wt.\%}
\]

And

\[
C_{Fe}^{Fe_2B} = 8.83 \text{ wt.\%}; \quad C_{Fe}^{Fe_2B} = 35 \times 10^{-4} \text{ wt.\%}
\]

3. EXPERIMENTAL VALIDATION OF THE MODEL

The validation of the present model is based on the experimental data provided by Campos-Silva et al. [22].

In their experimental work, the AISI D2 steel was used as the substrate to be boronized, its chemical composition is depicted in Table 1.

**Table 1. Chemical composition of AISI D2 steel**

<table>
<thead>
<tr>
<th>% C</th>
<th>% Si</th>
<th>% Mn</th>
<th>% Cr</th>
<th>% Mo</th>
<th>% V</th>
</tr>
</thead>
<tbody>
<tr>
<td>1.40-1.60</td>
<td>0.10-0.60</td>
<td>0.10-0.60</td>
<td>11.0-13.0</td>
<td>0.70-1.20</td>
<td>0.50-1.10</td>
</tr>
</tbody>
</table>

The boride layers were produced by applying the powder-pack boronizing in the range of 1223 K to 1273 K for different treatment times.

The thickness determined in their experiments for the boronized layers was the average of many measurements made in various points on the treated samples.

4. RESULTS AND DISCUSSIONS

A computer code was written in Matlab R2015b to simulate the boronizing kinetics. The outputs of our program are the growth rate constant for each phase, the boride layer thickness and the boron concentration in each phase \( (FeB, Fe, Fe_2B) \).

The data collected from the previous section were used as an input data for the computer simulation program, the kinetics data and boron activation energies for \( FeB \) and \( Fe_2B \) in AISI D2 steel were taken from the reference [2]. Boron diffusion coefficients in the \( \alpha-Fe \) and \( \gamma-Fe \) phase were found in the paper [20].

4.1 Growth rate constant calculation

Figure 2 describes the temperature dependence of growth rate constant at each interface during the growth of bilayer \( (FeB/Fe_2B) \) on AISI D2 steel in the temperature range of 1223-1273 K.

According to Figure 2, the growth rate constant in each phase \( (FeB \) and \( Fe_2B) \) follows an exponential law as a function of the boriding temperature.

A good agreement is noted between the experimental data and the simulation results.
Figure 2. Variation of the growth rate constant in each phase versus the boriding temperature

4.2 The boronized layer thickness

Figures 3 and 4 show the evolution of the square of layers thicknesses of FeB and Fe$_2$B layers grown at the surface of AISI D2 steel as a function of treatment time.

At first sight, it can be seen that the boronized layer thickness develops according to the parabolic law and the simulated curves coincide with the experimental data.

Figure 3. Evolution of square of FeB layer thickness as a function of treatment time

4.3 Effect of boron concentration on the boride layer thickness

We calculate the growth rate constant by varying the boron concentration at the material surface. The growth kinetics of the boronized layer in each phase depends on the value of surface boron concentration and the treatment temperature. It is noticed that the increase in the temperature of the process activated the phenomenon of boron diffusion inside the material.

Figure 5 and Figure 6 depicted the variation of the growth rate constant as a function of the surface boron concentration and we get from this result that the growth rate constant in each phase depends on the boron concentration and the process temperature.

In the case of the FeB layer, we note that the growth rate constant increases with the increasing of the temperature and the boron concentration at the material surface.

For the Fe$_2$B layer, it is seen that its growth rate constant is decreased when increasing the value of surface boron concentration at a given boriding temperature.

This is interpreted by the augmentation of the layer thickness of FeB which corresponds to the decrease in the Fe$_2$B boride layer thickness.

From Figures 5 and 6, it is demonstrated that the surface boron concentration exerts a strong influence on the kinetics of FeB layer and less for the Fe$_2$B layer.

Figure 4. Evolution of square of Fe$_2$B layer thickness as a function of treatment time

Figure 5. Growth rate constant according to the temperature and the surface boron concentration for the FeB layer
Figure 6. Growth rate constant according to the temperature and the surface boron concentration for the Fe₂B layer

4.4 Boron concentration for each phase

The developed computer simulation program allows us to follow the boron distribution through each boride layer.

To calculate the boron concentration in the Fe₂B and FeB phases, we used the following equations while considering the initial and the boundary conditions:

\[ C_{FeB}(x,t) = C_{B}^{S/FeB} + \frac{C_{B}^{FeB/FeB} - C_{B}^{S/FeB}}{\text{erf} \left( \frac{x}{2\sqrt{D_{B}^{FeB}t}} \right)} \times \text{erf} \left( \frac{\lambda_{FeB}}{2\sqrt{D_{B}^{FeB}t}} \right) \]  \hspace{1cm} (11)

\[ C_{B}^{FeB/FeB} + \frac{C_{B}^{FeB/FeB} - C_{B}^{FeB/FeB}}{\text{erf} \left( \frac{\lambda_{FeB}}{2\sqrt{D_{B}^{FeB}t}} \right) - \text{erf} \left( \frac{\lambda_{FeB}}{2\sqrt{D_{B}^{FeB}t}} \right)} \times \left[ \text{erf} \left( \frac{x}{2\sqrt{D_{B}^{FeB}t}} \right) - \text{erf} \left( \frac{\lambda_{FeB}}{2\sqrt{D_{B}^{FeB}t}} \right) \right] \]  \hspace{1cm} (12)

Figure 7. Boron concentration in the FeB phase for T=1172 K and surface boron surface concentration of 16.48 wt.%

\[ G(t)_{FeB} = 2p \left( C_{B}^{S/FeB} - C_{B}^{FeB/FeB} \right) \sqrt{\frac{D_{B}^{FeB}t}{\pi}} \]  \hspace{1cm} (13)

For the estimation of the mass gain associated to Fe₂B phase we used the following equation:

\[ G(t)_{Fe_{2}B} = 2p \left( C_{B}^{Fe_{2}B/FeB} - C_{B}^{Fe_{2}B/FeB} \right) \sqrt{\frac{D_{B}^{Fe_{2}B}t}{\pi}} \]  \hspace{1cm} (14)

With:

- \( G_{FeB} \) and \( G_{Fe_{2}B} \) are the mass gain per unit surface of FeB and Fe₂B phase.
- \( p \) is the specific volume of pure iron (=7.86 g.cm⁻³).

Figure 8. Boron concentration in the FeB phase for T=1172 K and surface boron surface concentration of 16.48 wt.%
5. CONCLUSION

In this work, a diffusion model based on the Fick second law and the mass balance equations at the two growing interfaces (FeB/Fe:B) and (Fe:B/Fe) was considered. It was applied to investigate the kinetics of formation of FeB and Fe:B layers on AISI D2 steel in the temperature range of 1223-1273 K.

The created computer program was able to calculate the boronized layer thickness, estimate the boron concentration in each phase and calculate the mass gain in each phase. The formation rates of the Fe:B and FeB layers had a parabolic character for all temperatures. The developed diffusion model has been validated by using the experimental data provided by Campos et al. [22].

A good agreement was then noticed between the experimental data and the simulation results. Moreover, the surface boron concentration had a strong influence on the growth of FeB layer; nevertheless, this effect was less pronounced for the Fe:B layer. The estimated values of mass gain at the material surface were greatly affected by the time duration because of a high mobility of boron in each boride layer (FeB and Fe:B) at a given temperature.

Finally, the modeling of the growth kinetics of boronized layers can provide a simple tool to study the influence of process parameters on the diffusion rate of boron atoms at the surface of AISI D2 steel.

REFERENCES


231-243.


