Soret Effect on MHD Unsteady Heat and Mass Transfer of Prandtl Fluid Flow Past an Exponentially Vertical Plate

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ABSTRACT

Prandtl fluid flow behaviour with the influence of magnetohydrodynamics (MHD) heat and mass transfer has been investigated. The fluid flow is propagated through an exponentially vertical plate where the flow model is performed through the boundary layer approximations. The governing equations are transformed into dimensionless nonlinear partial differential equations (PDEs) with the technique of as usual transformations. Non-dimensional momentum, temperature and concentration equations have been solved numerically by explicit finite difference method (EFDM) with the help of computer programming languages Compaq Visual Fortran (CVF) 6.6a. The results of stability convergence test (SCT) is used for selecting the appropriate value of various dimensionless parameters performed on velocity, temperature and concentration profiles along with the skin friction coefficient (Cf), Nusselt number (Nu) and Sherwood number (Sh) for different time intervals. The streamlines and isotherms have been analysed for different interesting parameters. Finally, a comparison of the present study with the previous study has been presented in the tabular form.

1. INTRODUCTION

The thermo physical properties of conventional heat transfer fluids are concerned to explore the extensive investigation. But these fluids are unable to meet the growing challenges of modern technology. In order to solve this problem, Prandtl fluid model has been used. Prandtl fluid is one kind of viscoelastic fluid. Viscoelastisity is the property of materials that exhibit both viscous and elastic characteristics when undergoing deformation. Viscous materials, like water, resist shear flow and strain linearly with time when a stress is applied. Blood flow analysis of Prandtl fluid model in tapered stenosed arteries was introduced by Akbar [1]. Nanoparticle analysis for blood flow of Prandtl fluid model with stenosis has been constructed by Nadeem et al. [2]. Effect logs of double diffusion on MHD Prandtl nano fluid adjacent to 4 stretching surfaces by way of numerical approach have explored by Bilal et al. [3]. Analysis of peristaltic flow for a Prandtl fluid model in an endoscope was adopted by Nadeem et al. [4]. Radiation heat transfer is characteristically different from the other two in that it does not require a medium and, in fact, it reaches maximum efficiency in a vacuum. Biswas et al. [8] have described the steady MHD natural convection heat transfer fluid flow through a vertical surface in the existence of Hall current and radiation. A numerical superintendence with stability exploration of casson nanofluid flow in the effects of variable thermal conductivity and radiation has been presented by Biswas et al. [9].

MHD free convection flow plays an important role in petrochemical industry, heat exchanger design and geophysics, cooling of the nuclear reactors as well as magnetohydrodynamics power generation system. Effects of radiation and chemical reaction on MHD unsteady heat and mass transfer of Casson fluid flow past a vertical plate have discussed by Biswas et al. [10, 11]. Chemical reactions are an integral part of technology, of culture, and indeed of life itself. Chemical reactions must be distinguished from physical changes. Physical changes include changes of state, such as ice melting to water and water evaporating to vapour. Also, some researcher [12-19] have been worked on MHD fluid flow. Dufour and Soret effects on steady MHD free Convective flow past a vertical porous plate embedded in a porous medium with chemical reaction, radiation, heat generation and viscous dissipation has been focused by Lavanya and Ratnam [20].

However, the aim of the present work is to study the Soret and radiation effect on MHD unsteady heat and mass transfer of Prandtl fluid flow through an exponentially vertical surface. In this problem, we have used explicit finite difference method (EFDM) to solve the governing equations. Also, our results are
computed for various physical parameters such as magnetic parameter, Schmidt number, Prandtl fluid parameter and radiation parameter etc. Also, the obtained results are plotted after the stability convergence test (SCT).

2. MATHEMATICAL ANALYSIS

The unsteady two-dimensional laminar flow of Prandtl fluid flow through an electrically conducting viscous incompressible semi-infinite vertical porous permeable surface in the arrival of thermal radiation, heat adsorption and Soret effect is considered. In this paper, the x-axis is chosen along the surface in the vertically upward direction and the y-axis is chosen normal to the surface which is displayed in Figure 1. A uniform magnetic field of strength $B_0$ is applied crosswise to the flow direction and the induced magnetic field strength is disregarded because of magnetic Reynold number $\text{Re}_m$ is taken very small. It is deliberated that, the temperature of the surface is assumed to be $T_w$ and concentration at the plate is $C_w$. From the above assumptions, the dimensional continuity, momentum, energy and concentration equations are follows:

\[
\frac{\partial u}{\partial x} + \frac{\partial v}{\partial y} = 0
\]  

(2)

\[
\frac{\partial u}{\partial t} + u \frac{\partial u}{\partial x} + v \frac{\partial u}{\partial y} = -\frac{\partial p}{\partial x} + \frac{\mu}{\rho} \left( \frac{\partial^2 u}{\partial x^2} + \frac{\partial^2 u}{\partial y^2} \right) + \beta \frac{\partial T}{\partial y} + g \beta_T (T - T_w)
\]

(3)

\[
\frac{\partial C}{\partial t} + u \frac{\partial C}{\partial x} + v \frac{\partial C}{\partial y} = D_m \frac{\partial^2 C}{\partial y^2} + \frac{D_m K_T}{T_m} \frac{\partial^2 T}{\partial y^2}
\]

(4)

The unsteady two-dimensional laminar flow of Prandtl fluid model is defined as follows:

\[
\tau = \frac{A \arcsin \left( \frac{\partial u}{\partial y} \right) + \left( \frac{\partial v}{\partial x} \right)^2}{\sqrt{\left( \frac{\partial u}{\partial y} \right)^2 + \left( \frac{\partial v}{\partial x} \right)^2}}
\]

(1)

where, $A$ and $C$ are material constants of Prandtl fluid model. Under these assumptions the dimensional continuity, momentum, energy and concentration equations are follows:

\[
\frac{\partial u}{\partial x} + \frac{\partial v}{\partial y} = 0
\]  

(2)

Figure 1. Physical model and coordinate system

According to Bilal et al. [3], the extra stress tensor for the Prandtl fluid model is defined as follows:

\[
\frac{\partial u}{\partial x} + \frac{\partial v}{\partial y} = 0
\]  

(2)

Since the solution of the governing equations under the initial and boundary conditions have been based on the finite difference method. It is to be required to make the equations dimensionless the following dimensionless variables are used.

\[
\frac{\partial U}{\partial \tau} + \frac{\partial V}{\partial \psi} = 0
\]  

(8)

\[
\frac{\partial U}{\partial \tau} + \frac{\partial V}{\partial \psi} + \alpha \frac{\partial^2 U}{\partial \psi^2} + \beta \frac{\partial^2 U}{\partial \psi^3} + \frac{\partial^2 U}{\partial \psi^4} + g \beta_T U + G_a \frac{\partial^2 T}{\partial \psi^2} = 0
\]

(9)

\[
\frac{\partial C}{\partial \tau} + \frac{\partial C}{\partial \psi} + \frac{\partial C}{\partial \psi} = \frac{1}{S_c} \frac{\partial^2 C}{\partial \psi^2} + \frac{S_T}{S_c} \frac{\partial^2 T}{\partial \psi^2}
\]

(10)

Also, the associate boundary conditions according to the present problem are,

\[
\begin{align*}
\tau > 0, & \quad U = \text{exp}(b \tau), V = 0, T = \text{exp}(\tau), C = \text{exp}(\tau) \quad \text{at} \quad Y = 0, \\
U = 0, & \quad T \to 0, C \to 0 \quad \text{as} \quad Y \to \infty
\end{align*}
\]

(11)

(12)
Where \( \tau \) is the time constant, Prandlt number: \( P_r = \frac{\nu G_p}{K} \); Grashof number: \( Gr = \frac{\nu G_p(T_m-T_\infty)}{\alpha G_p^2} \); Heat source parameter: 
\[
S = \frac{q_w}{\rho c_p G_p^2} \quad \text{magnetic parameter:} \quad M = \frac{2 B m G_p^2}{\tau T m G_p^2} \quad \text{Schmidt number:} \quad S_c = \frac{\nu}{\rho G_p} \quad \text{Modified Grashof number:} \quad G_m = \frac{\nu G_p(C_w-C_\infty)}{G_p^2} \quad \text{Radiation parameter:} \quad R_a = \frac{4 \pi a r^3}{K T m G_p^2} \quad \text{Prandlt fluid parameter:} \quad \alpha = \frac{1}{\mu G_p} \quad \text{elastic parameter:} \quad \beta = \frac{1}{2 G_p^2} \quad \text{and Soret number:} \quad S_r = \frac{\beta}{G_m} \]

The skin friction, Nusselt number and Sherwood number are found respectively by the following with Non-dimensional form as:
\[
C_f = -\frac{1}{2 \sqrt{2}} (G_\nu) \gamma \left( \frac{\partial U}{\partial Y} \right)_{y=0} \quad \text{and} \quad N_u = \frac{1}{2 \sqrt{2}} (G_\nu) \gamma \left( \frac{\partial T}{\partial Y} \right)_{y=0} \quad (13)
\]

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\]

Three dimensional stream functions exist physically but cannot be represented mathematically. So the Stream function \( \psi(X, Y) \) can be exit two dimensionally with the velocity components as:
\[
U = \frac{\partial \psi}{\partial Y}, \quad V = -\frac{\partial \psi}{\partial X} \quad (14)
\]

3. CALCULATION TECHNIQUE

The region of the flow is divided into a grid or mesh of lines parallel to \( X \) and \( Y \) axis where \( X \)-axis is taken along the plate and \( Y \)-axis is normal to the plate. It is considered that the plate of height \( X_{max} = 125 \) i.e. \( X \) varies from 0 to 125 and regard \( Y_{max} = 125 \) i.e. \( Y \) varies from 0 to 25. There are \( m = 150 \) and \( n = 300 \) grid spacing in the \( X \) and \( Y \) directions respectively as shown in Figure 2. It is assumed that \( \Delta X \), \( \Delta Y \) are constant mesh sizes along \( X \) and \( Y \) directions respectively and taken, \( \Delta X = 0.83 \) (0≤\( X \)≤125) ; \( \Delta Y = 0.83 \) (0≤\( Y \)≤125); With the smaller time-step, \( \Delta t = 0.0005 \) and \( U, T \) and \( C \) denote the values of \( U, T \) and \( C \) at the end of a time-step respectively.

In this case, the associate boundary conditions according to the present problem are,
\[
\tau > 0, \quad U_{x=0}^n = exp(b \Delta t), \quad V_{y=0}^n = 0, \quad T_{x=0}^n = exp(n \Delta t), \quad \bar{C}_{x=0}^n = exp(n \Delta t) \quad \text{at} \ Y = 0)
\]
\[
U_{x=L} = 0, \quad T_{y=1} = 0, \quad \bar{C}_{y=1} = 0 \quad \text{where} \ L \to \infty \quad (19)
\]

4. STABILITY AND CONVERGENCE ANALYSIS

The stability conditions for the present problem are:
\[
\alpha \Delta \frac{2 \Delta t}{\Delta Y^2} + \frac{U}{\Delta X} - \frac{V}{\Delta Y} \left( \frac{\Delta t}{\Delta Y} \right) + \frac{K_p \Delta t}{2} \leq 1 \quad (20)
\]

\[
R_a \frac{2 \Delta t}{\Delta Y^2} + \frac{1}{\Delta X} \frac{2 \Delta t}{P_r (\Delta Y)^2} + \frac{U}{\Delta X} - \frac{V}{\Delta Y} \left( \frac{\Delta t}{\Delta Y} \right) - \frac{S \Delta t}{2} \leq 1 \quad (21)
\]

\[
\frac{1}{S_c \Delta Y^2} + \frac{U}{\Delta X} - \frac{V}{\Delta Y} \left( \frac{\Delta t}{\Delta Y} \right) \leq 1 \quad (22)
\]

Since the initial condition, \( U=V=0 \) at \( \tau = 0 \). So, the convergence criteria of the present problem are \( S_c \geq 0.15, P_r \geq 0.62 \) and \( L \geq 0.87 \) respectively.

5. RESULTS AND DISCUSSION

To obtain the results of the present problem an explicit finite difference method (EFDM) has been used and the approximate solutions are obtained for various parameters for the purpose of result and discussing. The physical situation of velocity, temperature, concentration, skin friction, Nusselt number,
Sherwood number, streamlines and isotherms for vertical plate within the boundary conditions are obtained for the default parameters which are chosen as: $M=1.0$, $Pr=0.63$, $Sc=0.22$, $\beta=0.01$, $S=0.1$, $\alpha=0.01$, $Sr=1$, $Gr_w=5$, $Gr_r=5$, $K_p=0.5$, and $Ra=1.0$ with time $\tau=1$.

The outcome of different values of the elastic parameter ($\beta$), Prandlt fluid parameter ($\alpha$), magnetic parameter ($M$), permeability of porous medium ($K_p$), Schmidt number ($S$) and Prandtl number ($Pr$) on velocity profiles are displayed in Figure 3(a) and Figure 3(b). It is observed that velocity profiles are increasing as elastic parameter ($\beta$) and Prandlt fluid parameter ($\alpha$) but decreasing due to the magnetic parameter ($M$), permeability of porous medium ($K_p$), Schmidt number ($S$) and Prandtl number ($Pr$). Physically, the magnetic parameter ($M$) and permeability of porous medium ($K_p$) which increases a resistive force. For this resistive force, velocity profiles are decreasing with the increasing of magnetic parameter ($M$) and permeability of porous medium ($K_p$).

Figure 3. Illustration of (a) Velocity profiles for different values of $\beta$ and $\alpha$ (b) Velocity profiles for different values of $M$, $K_p$, $S$, and $Pr$.

Figure 4. Illustration of (a) Temperature profiles for different values of $Pr$ and (b) Temperature profiles for different values of $S$ and $Ra$.

Figure 5. Illustration of (a) Concentration profiles for different values of $Sc$ and (b) Concentration profiles for different values of $Sr$ and $Ra$.

From Figure 4(a) and Figure 4(b), it is notified that temperature profiles are decreasing due to the increase of Prandlt number but increasing due to the increases of radiation parameter and heat source parameter. The main things of such
mechanism on temperature profiles as heat source parameter produced energy in the fluid flow which increases the temperature profiles. Also, temperature profiles are increasing for differences values of radiation parameter. Physically, the radiation parameter provides more heat into the fluid, which leads to increases in the thermal boundary layer thickness.

The impact of Schmidt number and Soret number on concentration profiles are displayed in Figure 5(a) and Figure 5(b). Schmidt number ($S_c$) is a dimensionless number which decreases the concentration profiles. It is true by physically that the Schmidt number increases, the density of the fluid as well as concentration buoyancy force in the fluid. Also, the concentration boundary layer thickness increases consequently for the increasing of Soret number which leads the concentration profiles.

Figure 6. Illustration of (a) Streamlines for magnetic parameter $M=0.50$ to $M=1.50$ and (b) Isotherms for magnetic parameter $M=0.50$ to $M=1.50$

Figure 7. Illustration of (a) Streamlines for Prandtl fluid parameter $\alpha=0.01$ to $\alpha=0.03$ and (b) Isotherms for Prandtl fluid parameter $\alpha=0.01$ to $\alpha=0.03$

Figure 8. Illustration of (a) Streamlines for radiation parameter $Ra=1.0$ to $Ra=1.50$ and (b) Isotherms for radiation parameter $Ra=1.0$ to $Ra=1.50$

The impact of magnetic parameter (M) on streamlines and isotherms are represented in Figure 6(a) and Figure 6(b). The momentum boundary layer thickness increases and thermal boundary layer thickness decreases due to increase of
magnetic parameter $M=0.50$ to $M=1.50$. Also, the effect of Prandtl fluid parameter ($\alpha$) on streamlines and isotherms are represented in Figure 7(a) and Figure 7(b). Here, we observe that momentum boundary layer thickness and thermal boundary layer thickness both are increasing due to the increase of Prandtl fluid parameter from $\alpha=0.01$ to $\alpha=0.03$. Further, the influence of radiation parameter (Ra) on streamlines and isotherms are represented in Figure 8(a) and Figure 8(b). Here, we observed that momentum boundary layer thickness and thermal boundary layer thickness both are decreasing due to the increase of radiation parameter (Ra) from $Ra=1.0$ to $Ra=1.50$.

Table 1 represents the numerical values of different parameters such as permeability of porous medium, elastic parameter, radiation parameter, Schmidt number, Prandlt fluid parameter, heat source parameter, Soret number and magnetic parameter on skin friction($C_f$), Nusselt number($N_u$) and Sherwood number ($Sh$). It is showed that the skin friction increases with elastic parameter, radiation parameter, heat source parameter and magnetic parameter but decreases qualitatively with an increase of permeability of porous medium, Schmidt number, Prandlt fluid parameter and Soret number. On the other hand, the Nusselt number is an increasing function of permeability of Prandlt fluid parameter and Soret number whereas this tendency is quite opposite for permeability of porous medium, elastic parameter, radiation parameter, Schmidt number, heat source parameter and magnetic parameter. Also it is noticed that the Sherwood number increases with the increasing of elastic parameter, radiation parameter, Schmidt number, Prandlt fluid parameter, heat source parameter, Soret number and magnetic parameter radiation parameter Lewis number but decreases qualitatively just with the increasing of permeability of porous medium, radiation parameter, Schmidt number, Prandlt fluid parameter, heat source parameter, Soret number and magnetic parameter.

Table 1. Variation of different parameters on local skin friction, Nusselt number and Sherwood number for Prandtl nanofluid.

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6. CONCLUSION

From the present numerical investigation, the following conclusions have been drawn:

1. Velocity profiles are increasing respectively as Prandtl fluid parameter.
2. Skin friction increases with the increase of elastic parameter, radiation parameter, heat source parameter and magnetic parameter but decreases qualitatively with an increase of permeability of porous medium, Schmidt number, Prandlt fluid parameter and Soret number.
3. It is observed that permeability of porous medium and magnetic parameter decreases the velocity distribution.
4. Radiation parameter increases the velocity and temperature profiles.
5. Momentum boundary layer thickness and thermal boundary layer thickness both are decreasing due to the increase of radiation parameter.
6. Temperature profiles are increasing due to increases of radiation parameter and heat source parameter but decrease due to the increasing of Prandtl number.

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