



Figure 3. Optimal control input law of robot motion

The above figures show that the trajectory of the robot, as well as the angular velocity and expansion linear velocity of the leg, were all smooth and continuous. Besides, the initial and final velocities were both zero.

6. CONCLUSIONS

In engineering, the motor control of robot attitude motion requires the initial and final control inputs to be zero. However, the common optimization methods like Fourier approximation cannot guarantee the control inputs are zero at the start and end of the robot motion. To solve the problem, this paper combines spline approximation and the PSO into a novel algorithm, and uses it to solve the optimal control problem of attitude motion planning for a hopping robot system under nonholonomic constraints. The proposed algorithm can optimize the motion trajectory of the robot, eliminating the nonzero initial and final values of the control inputs. The algorithm inherits the advantages of the PSO, such as simple structure, limited number of parameters, ease of programming and fast convergence. The research findings shed new light on solving motion control problems of nonholonomic systems.

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REFERENCES

- [1] Khaksar, W., Vivekananthen, S., Saharia, K.S.M., Yousefi, M., Ismail, F.B. (2015). A review on mobile robots motion path planning in unknown environments. 2015 IEEE International Symposium on Robotics and Intelligent Sensors (IRIS), pp. 295-300. <http://dx.doi.org/10.1109/IRIS.2015.7451628>
- [2] Raibert, M.H. (2007). Legged robots that balance. *IEEE Expert*, 1(4): 89-89. <http://dx.doi.org/10.1109/MEX.1986.4307016>
- [3] Bazzi, S., Shammass, E., Asmar, D. (2014). A novel method for modeling skidding for systems with nonholonomic constraints. *Nonlinear Dynamics*, 76(2): 1517-1528. <https://doi.org/10.1007/s11071-013-1225-9>
- [4] Khan, M.U., Shuai, L., Wang, Q., Shao, Z. (2016). Formation control and tracking for co-operative robots with non-holonomic constraints. *Journal of Intelligent & Robotic Systems*, 82(1): 163-174. <https://doi.org/10.1007/s10846-015-0287-y>
- [5] Saska, M., Spurný, V., Vonásek, V. (2016). Predictive control and stabilization of nonholonomic formations with integrated spline-path planning. *Robotics & Autonomous Systems*, 75: 379-397. <https://doi.org/10.1016/j.robot.2015.09.004>
- [6] Roozegar, M., Mahjoob, M.J., Jahromi, M. (2016). Optimal motion planning and control of a nonholonomic spherical robot using dynamic programming approach: simulation and experimental results. *Mechatronics*, 39: 174-184. <https://doi.org/10.1016/j.mechatronics.2016.05.002>
- [7] Fareh, R., Rabie, T. (2016). Tracking trajectory for nonholonomic mobile manipulator using distributed control strategy. *International Symposium on Mechatronics & Its Applications*. <https://doi.org/10.1109/ISMA.2015.7373473>
- [8] Yang, L.L. (2013). The numerical method to nonholonomic motion planning of a hopping robot. *Manufacturing Automation*, 50: 545-553. <https://doi.org/10.3969/j.issn.1009-0134.2013.13.026>
- [9] Janiak, M., Tchoń, K. (2011). Constrained motion planning of nonholonomic systems. *Systems & Control Letters*, 60(8): 625-631. <https://doi.org/10.1016/j.sysconle.2011.04.022>
- [10] Wu, J.W., Shi, S.C., Liu, H., Cai, H.G. (2011). Spacecraft attitude disturbance optimization of space robot in target capturing process. *Robot*, 33(1): 16-21. <https://doi.org/10.3724/SP.J.1218.2011.00016>
- [11] Su, P., He, G.P., Xu, M. (2012). Research on motion simulation of hopping robot based on minimum energy-loss principle. *Machinery Design & Manufacture*, 4: 171-173. <https://doi.org/10.3969/j.issn.1001-3997.2012.04.064>
- [12] Yaghoobi, S., Moghaddam, B.P., Ivaz, K. (2017). An efficient cubic spline approximation for variable-order fractional differential equations with time delay. *Nonlinear Dynamics*, 87(2): 815-826. <https://doi.org/10.1007/s11071-016-3079-4>
- [13] Poli, R., Kennedy, J., Blackwell, T. (2007). Particle swarm optimization. *Swarm Intelligence*, 1(1): 33-57. <https://doi.org/10.1007/s11721-007-0002-0>
- [14] Venter, G., Sobieszczyński-Sobieski, J. (2012). Particle Swarm Optimization. 9-th Aiaa/usaf/nasa/issmo Symposium on Multidisciplinary Analysis & Optimization Conference, 41(8): 1583-1585 <https://doi.org/10.2514/2.2111>